

# Site response modeling in liquefiable soil deposits

**Steve Kramer**

*University of Washington*

**Aaron Hartvigsen**

*Geoengineers, Bellingham, WA*

**Sam Sideras**

*University of Washington*

**Pelin Ozener**

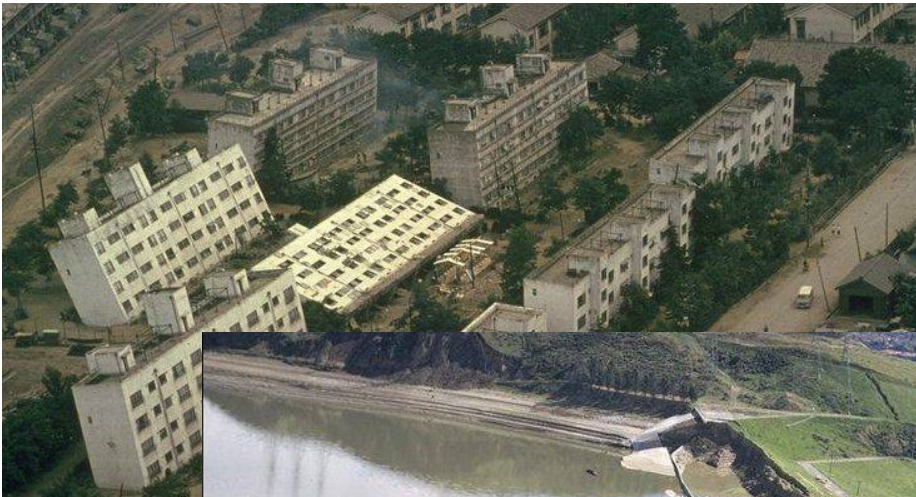
*Yildiz Technical University*

# Outline

- Behavior of liquefiable soils
- Characteristics of ground motions affected by liquefaction
- Analysis of vertical arrays
- Effects of liquefaction on ground motions
- Summary and conclusions

# Soil Liquefaction

Widely recognized for potential to cause ground failure

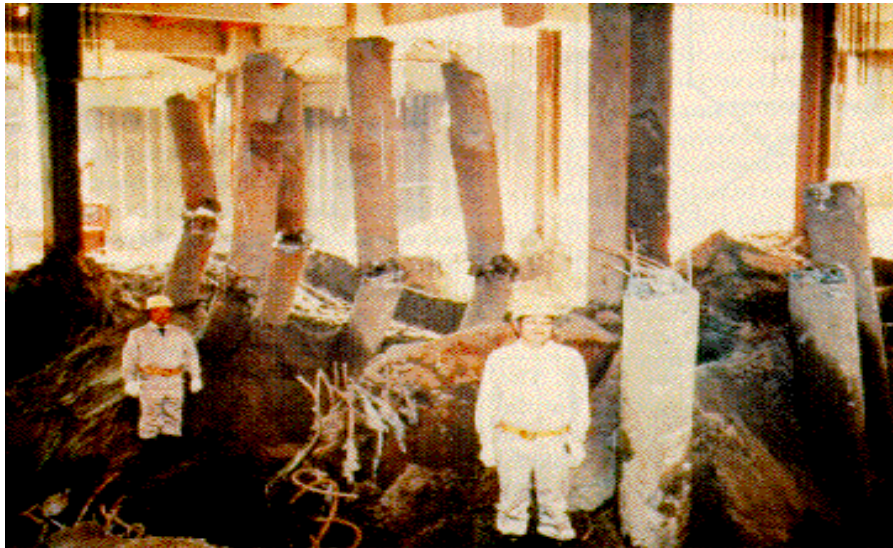


Imaz



# Soil Liquefaction

Ground response is also important





# Soil Liquefaction

Laboratory testing

*Cyclic triaxial*



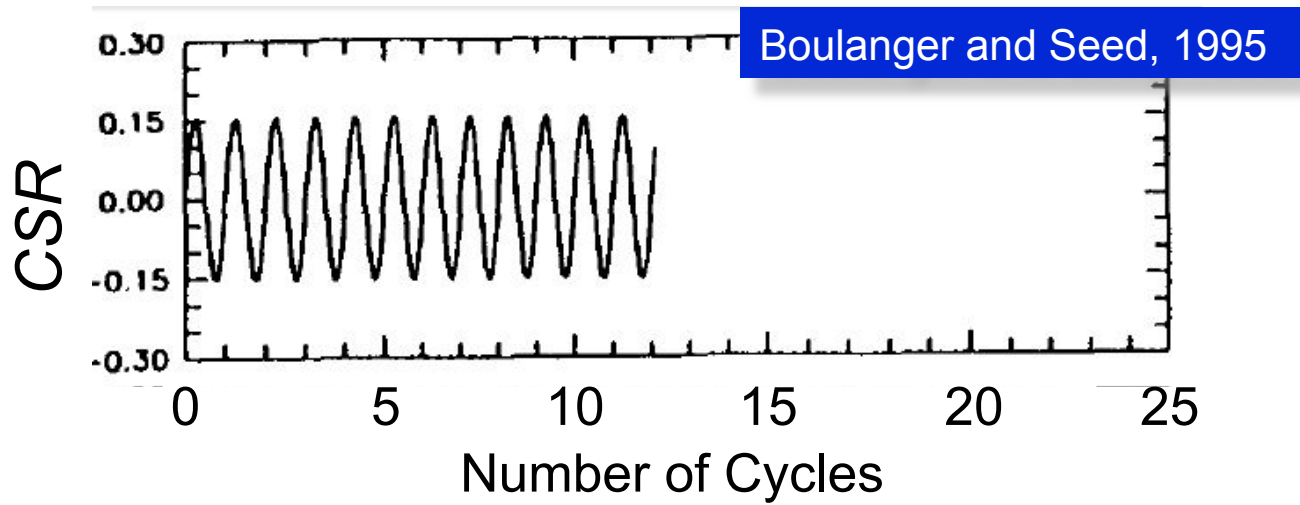
NTUA

*Cyclic simple shear*



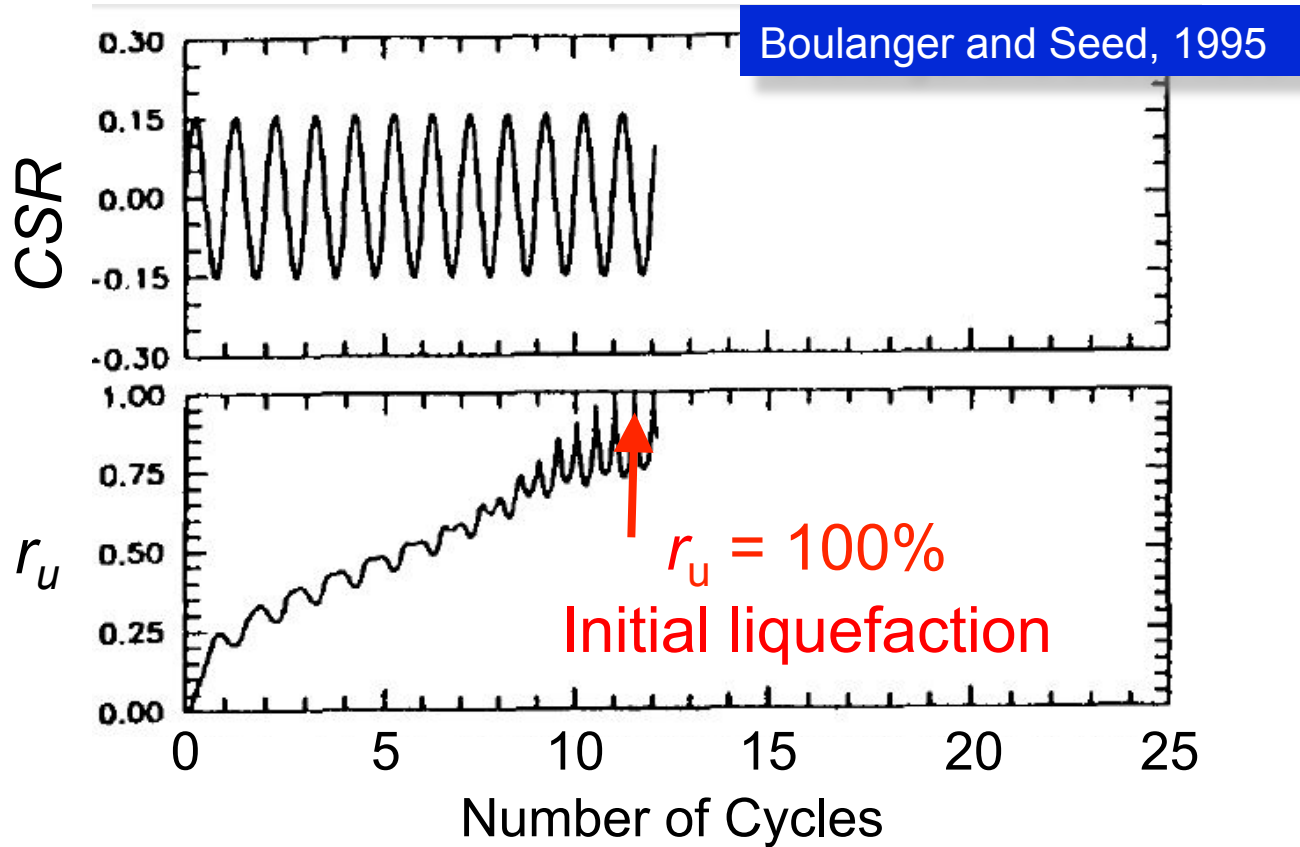
Geocomp

# Soil Liquefaction



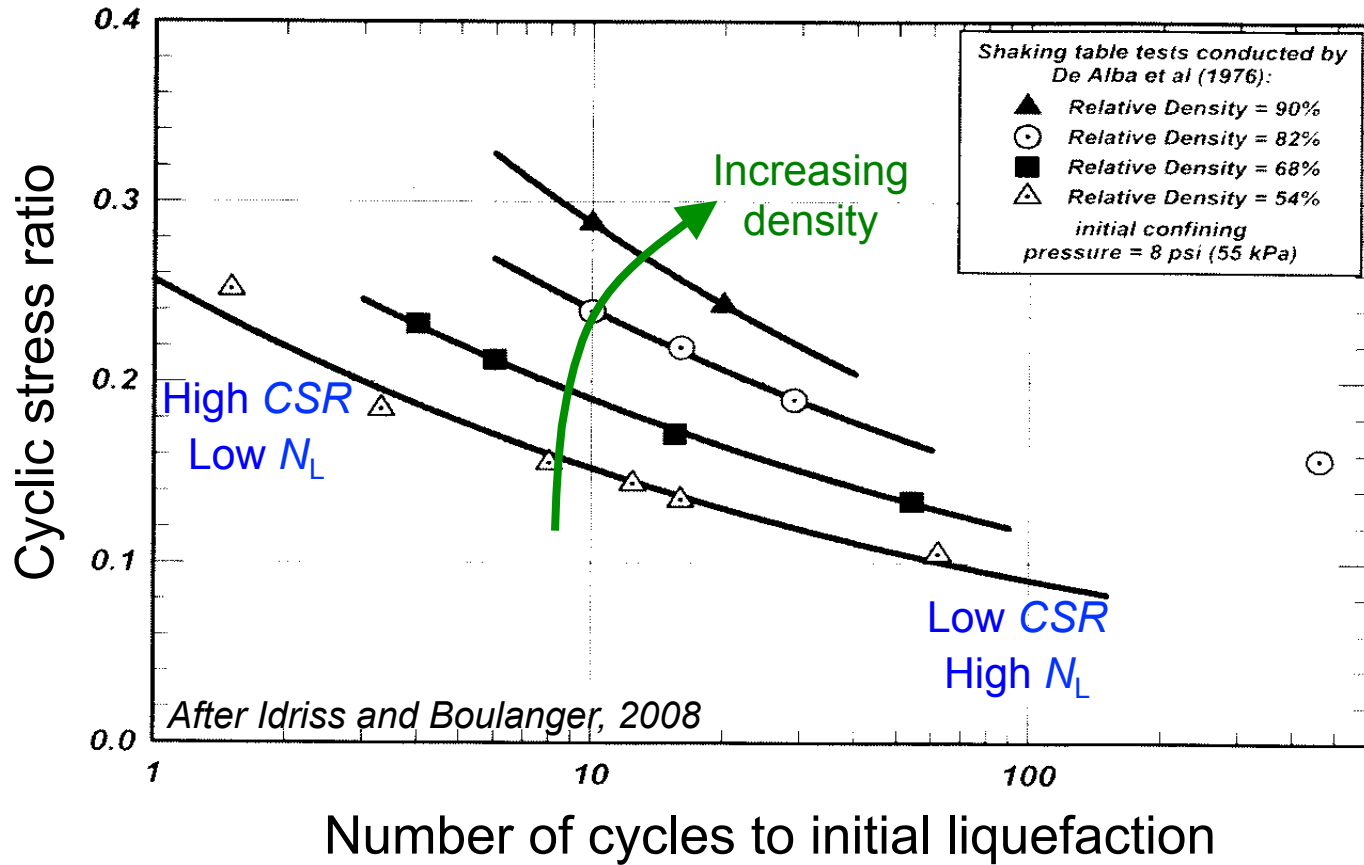


# Soil Liquefaction



# Soil Liquefaction

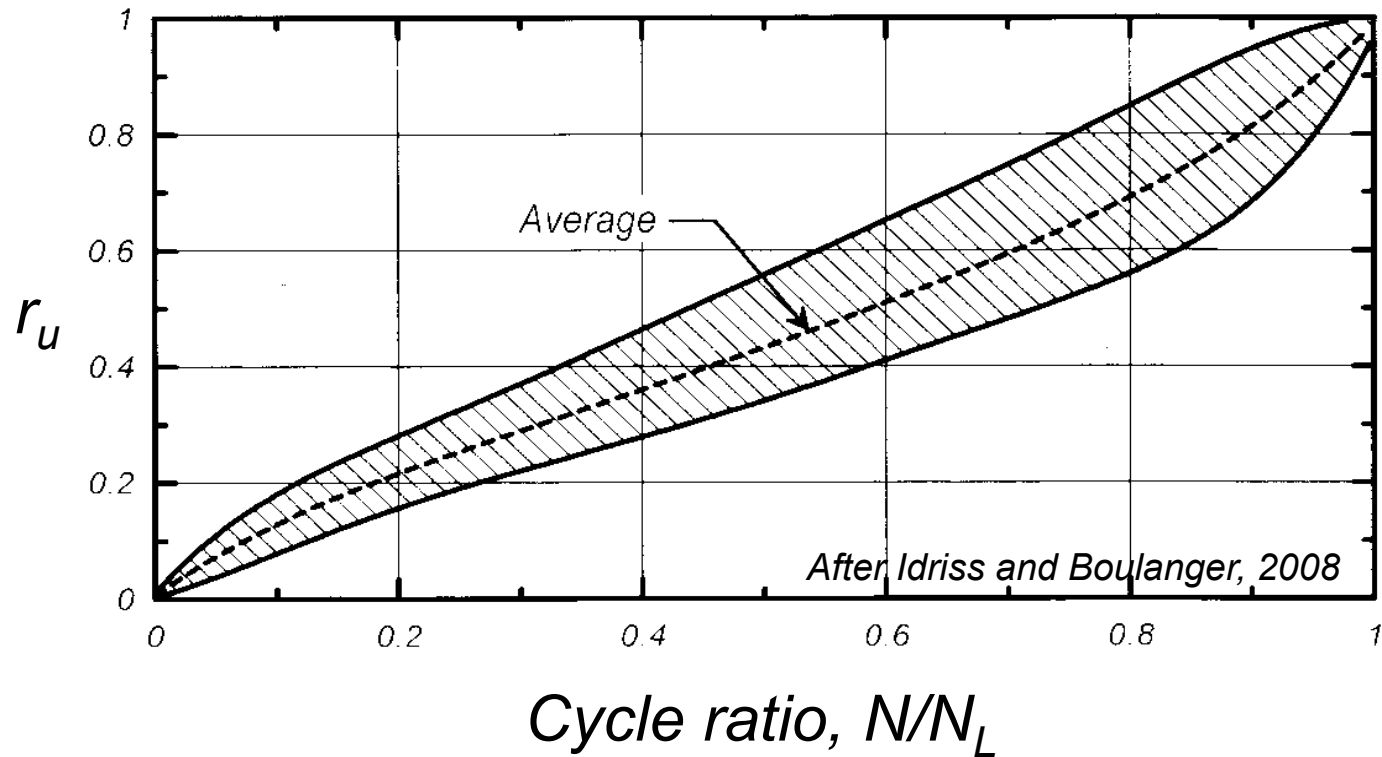
Typical behavior – harmonic loading



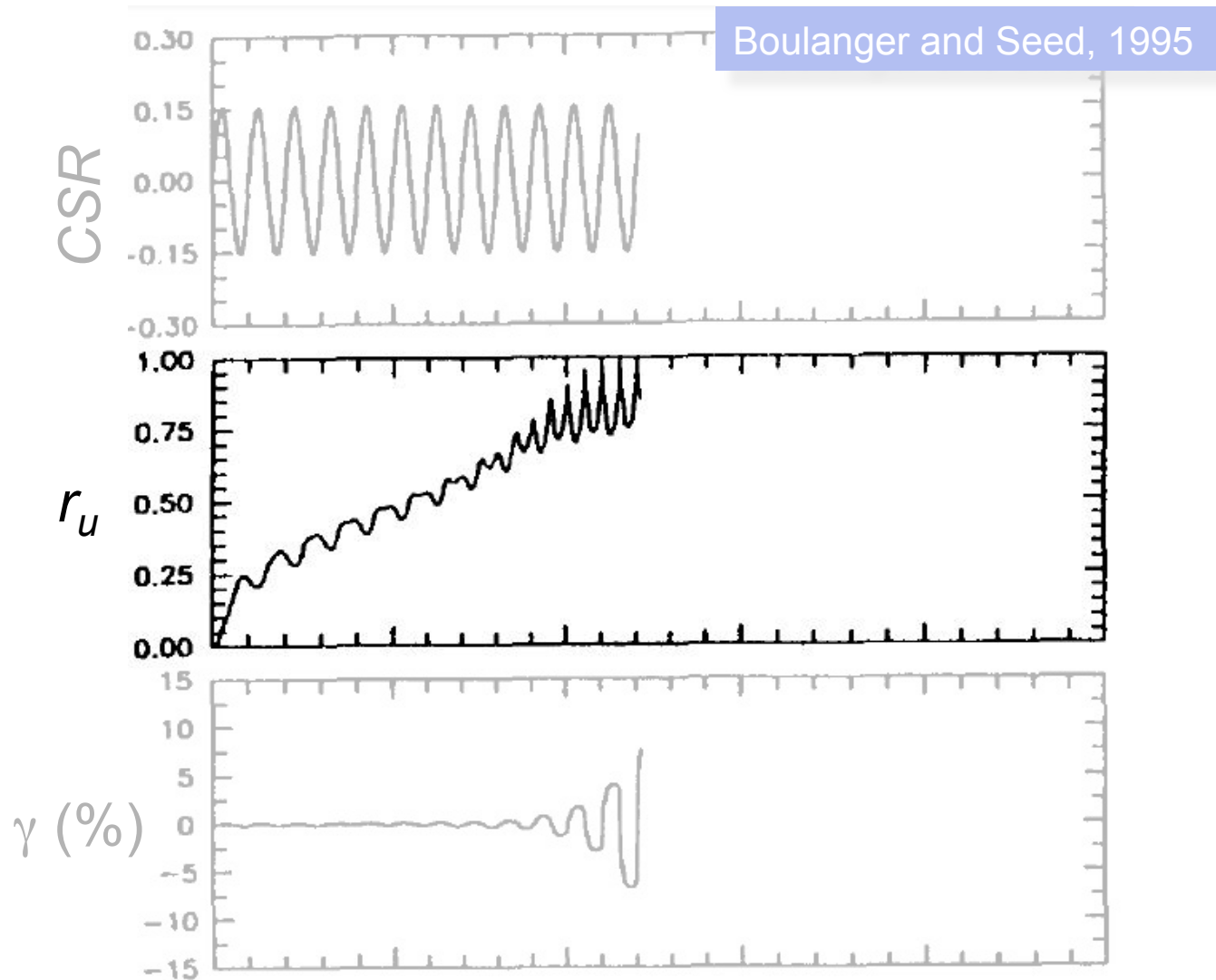


# Soil Liquefaction

Typical behavior – harmonic loading

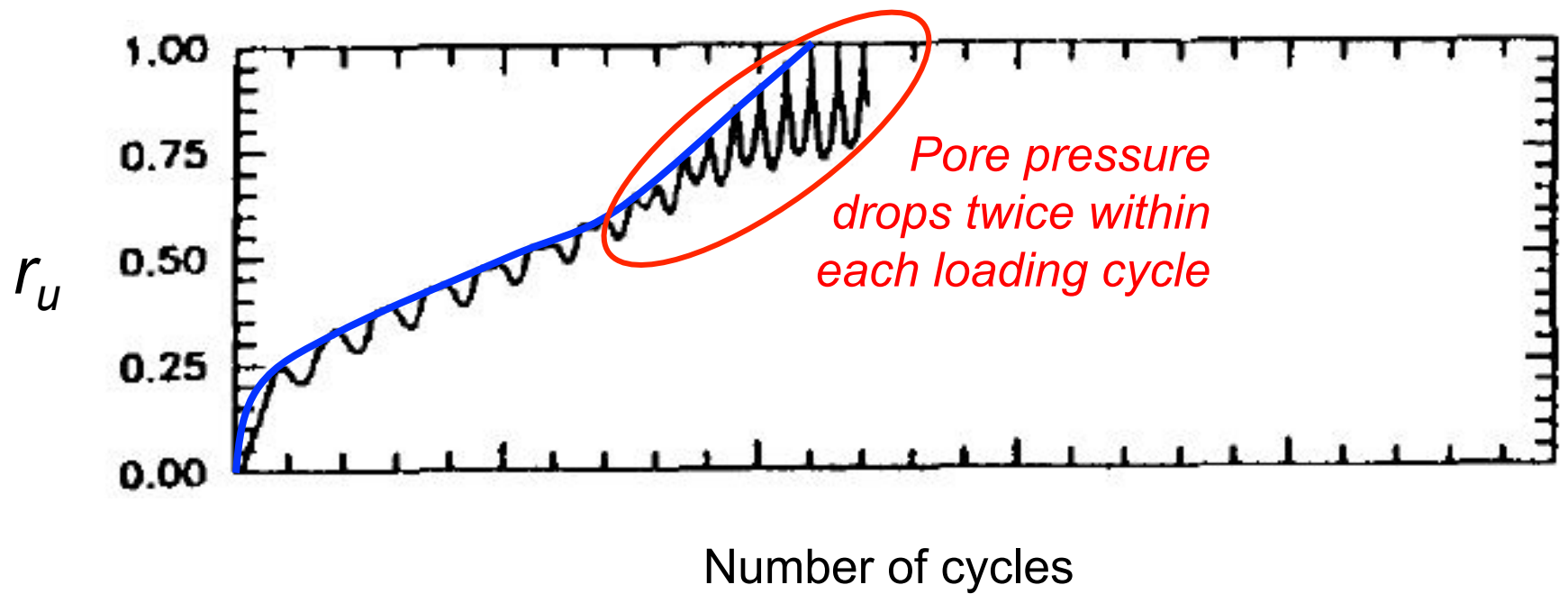


# Soil Liquefaction





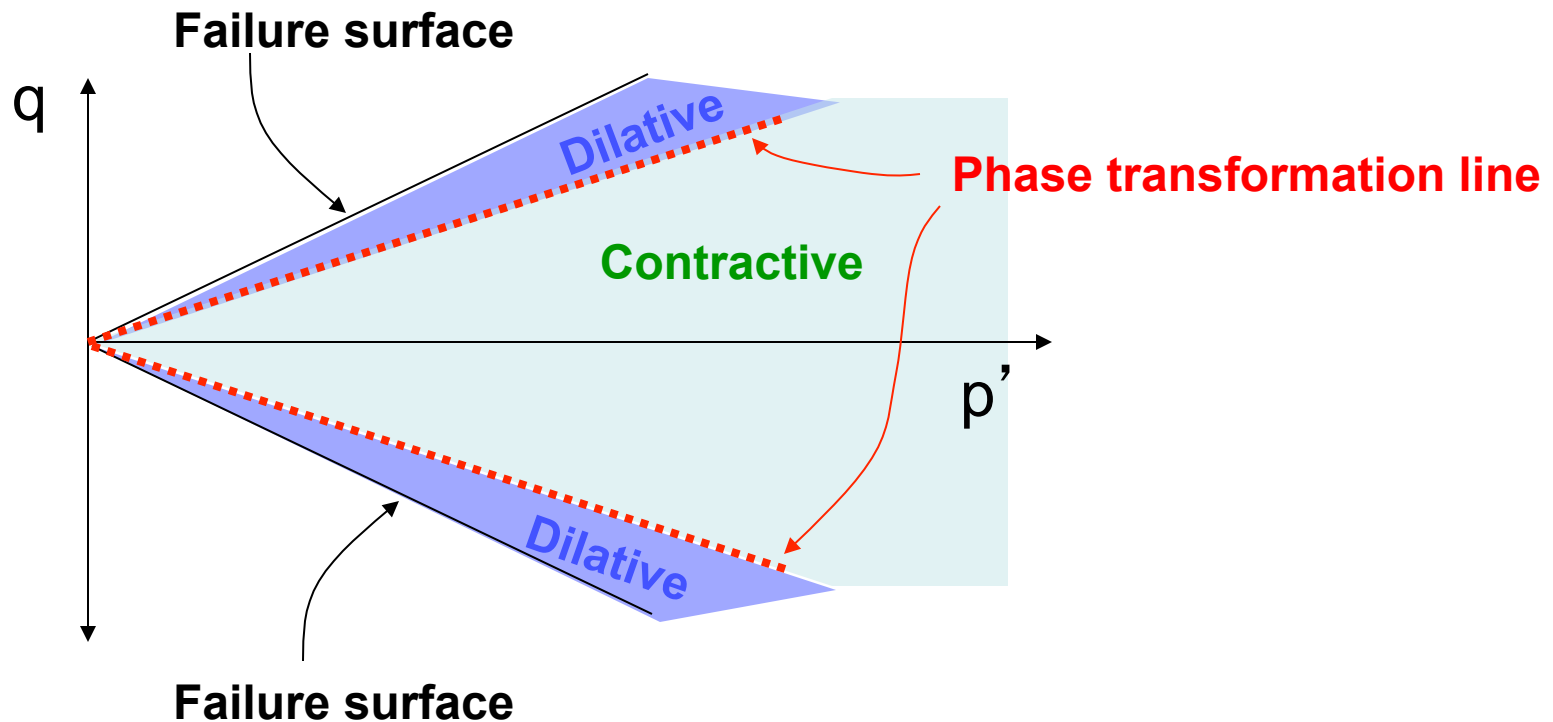
# Soil Liquefaction



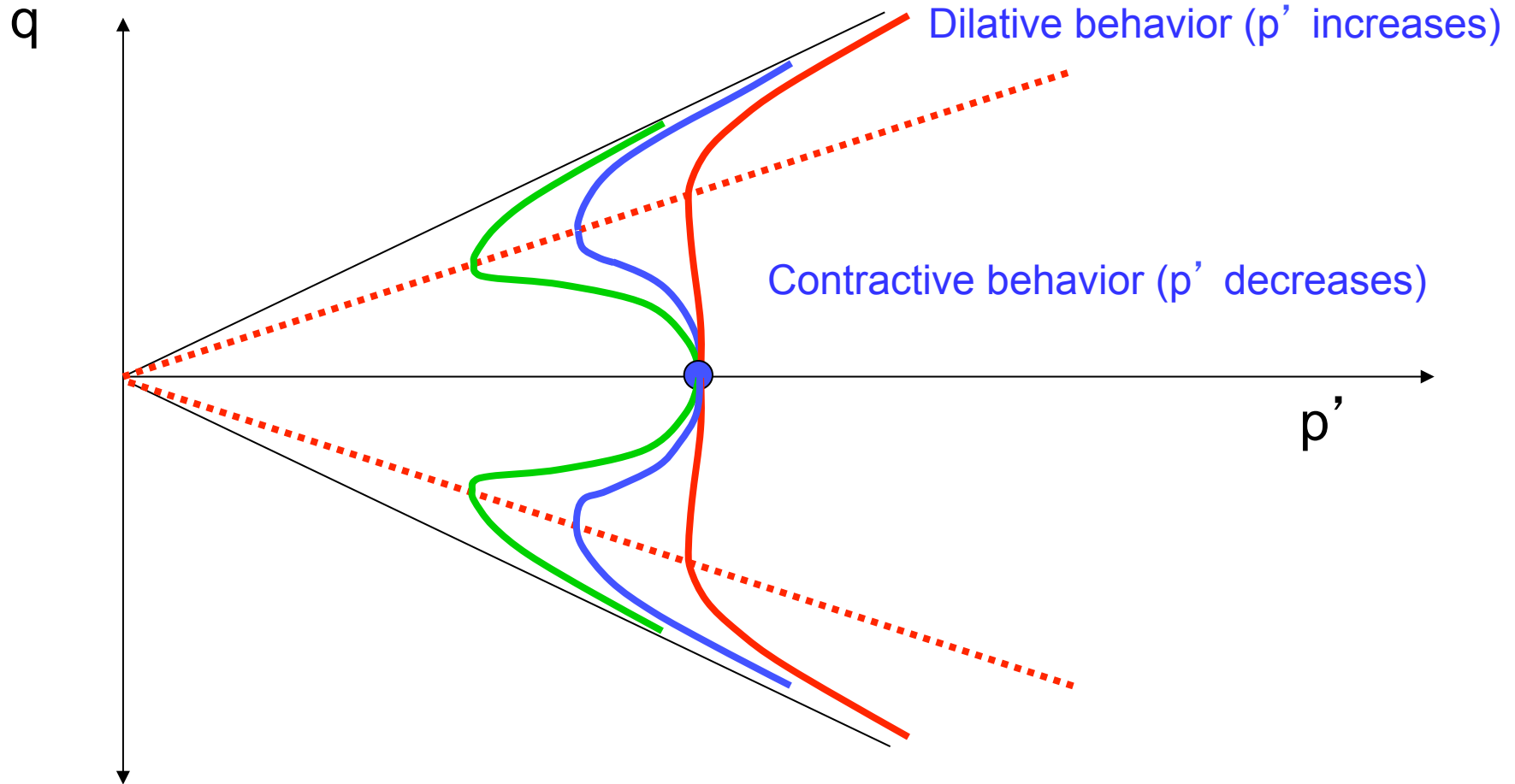
# Effects of Liquefaction

## Phase transformation

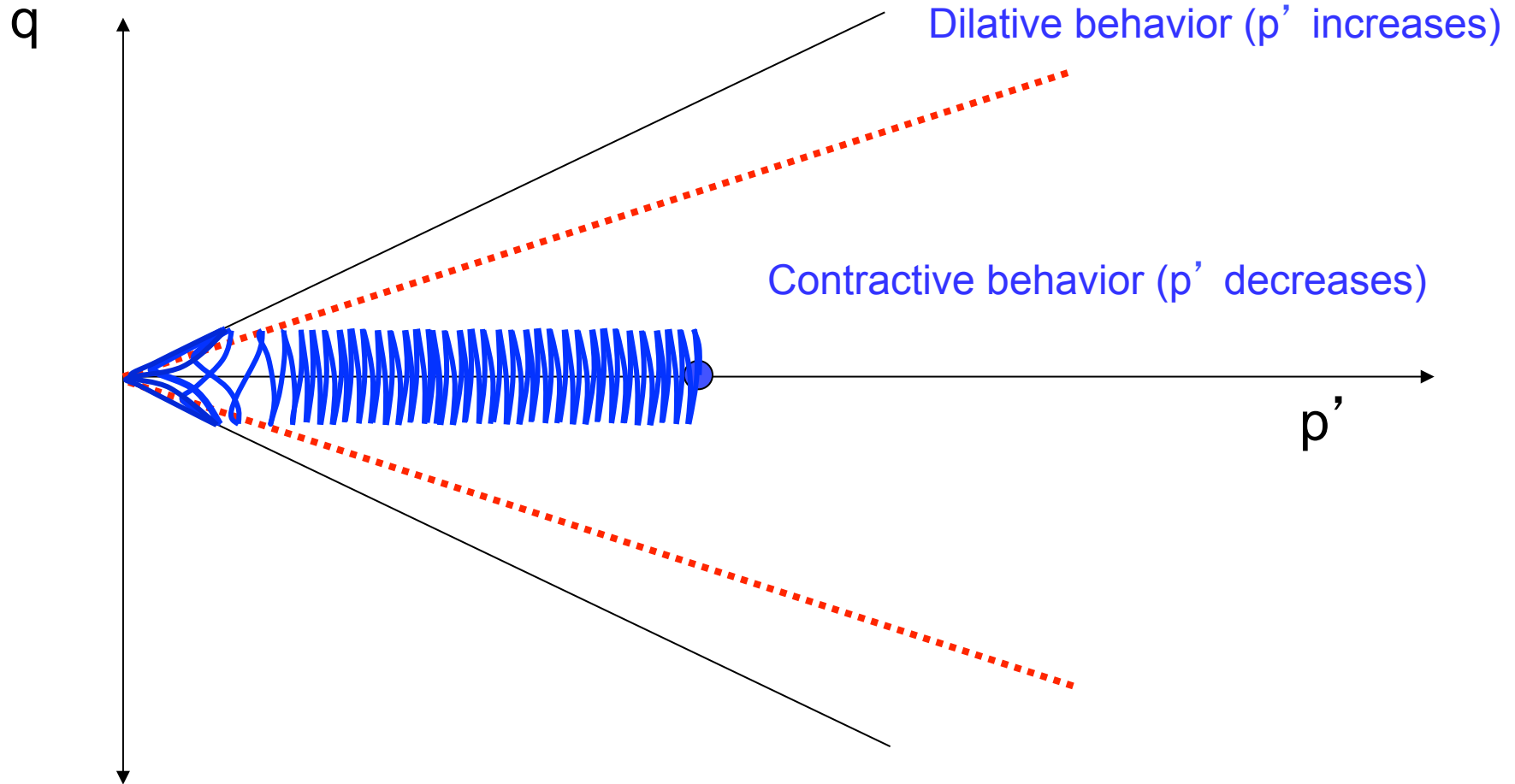
- Contractive behavior –  $u$  increases,  $p'$  decreases
- Dilative behavior –  $u$  decreases,  $p'$  increases



# Effects of Liquefaction

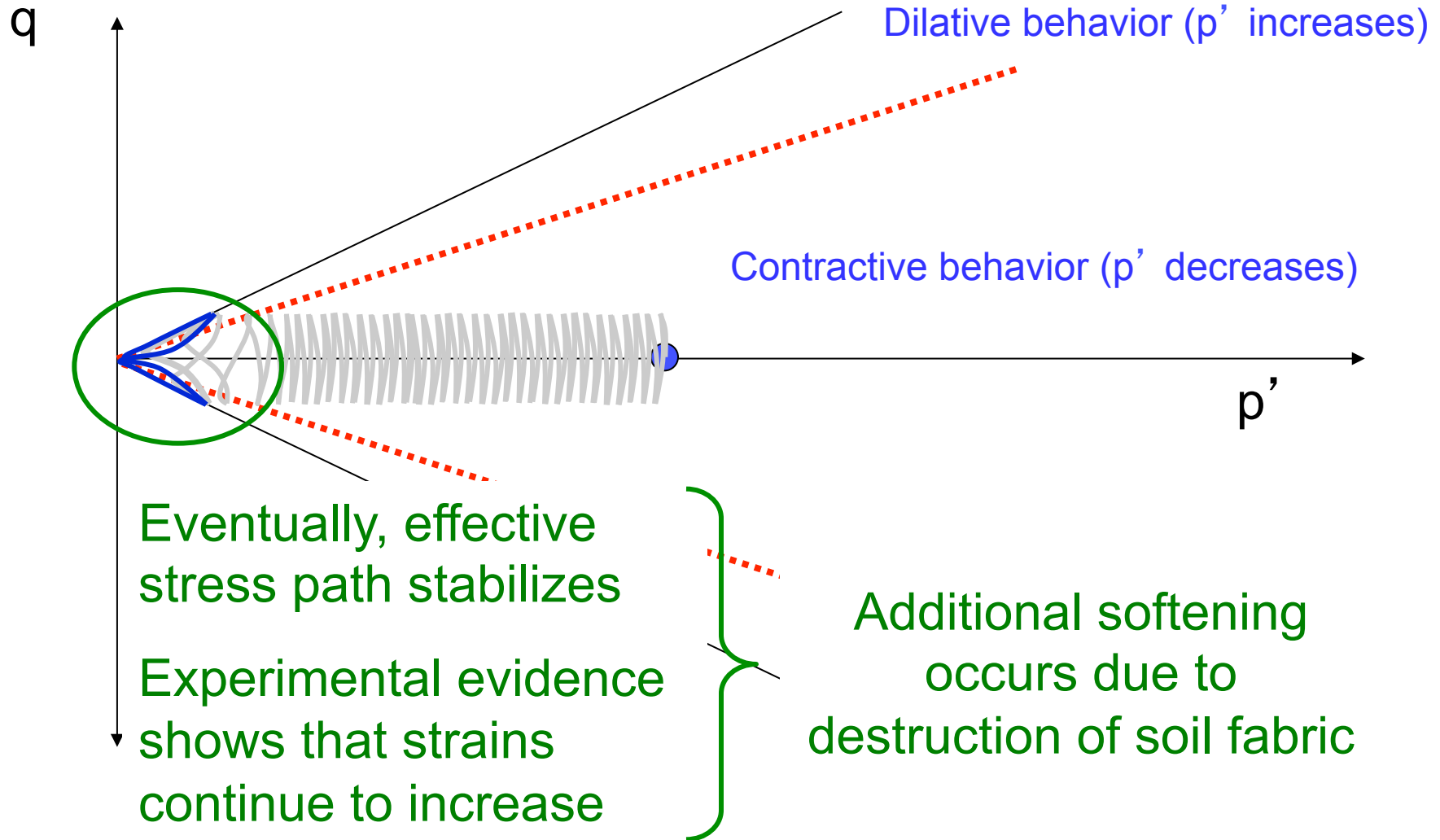


# Effects of Liquefaction

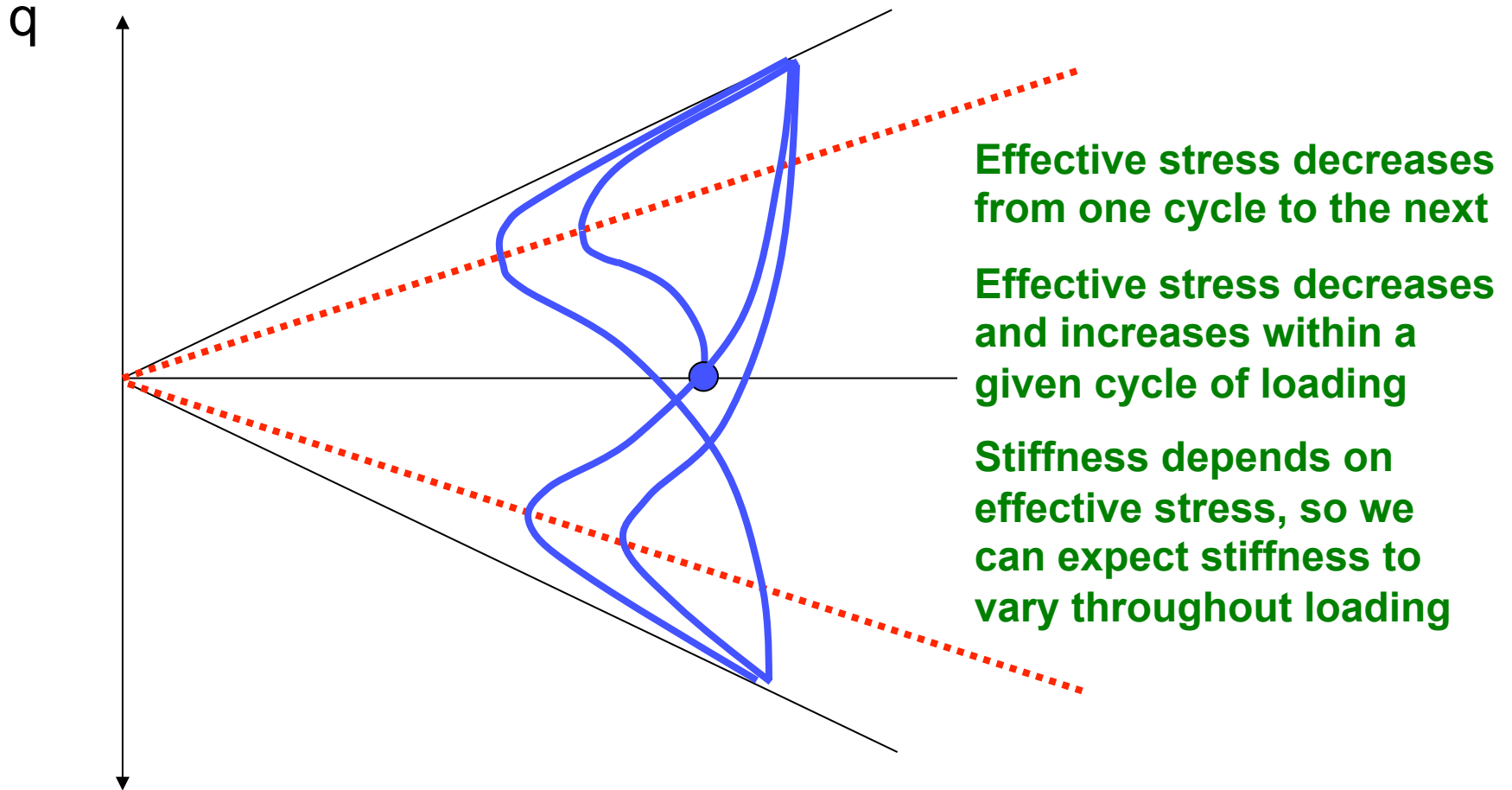




# Effects of Liquefaction

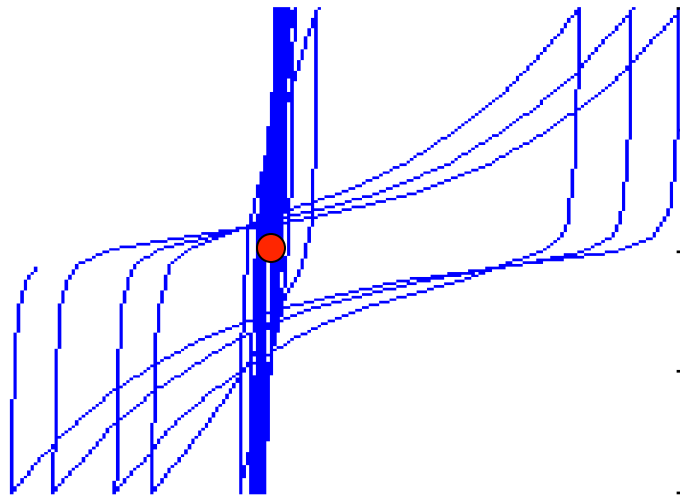


# Effects of Liquefaction

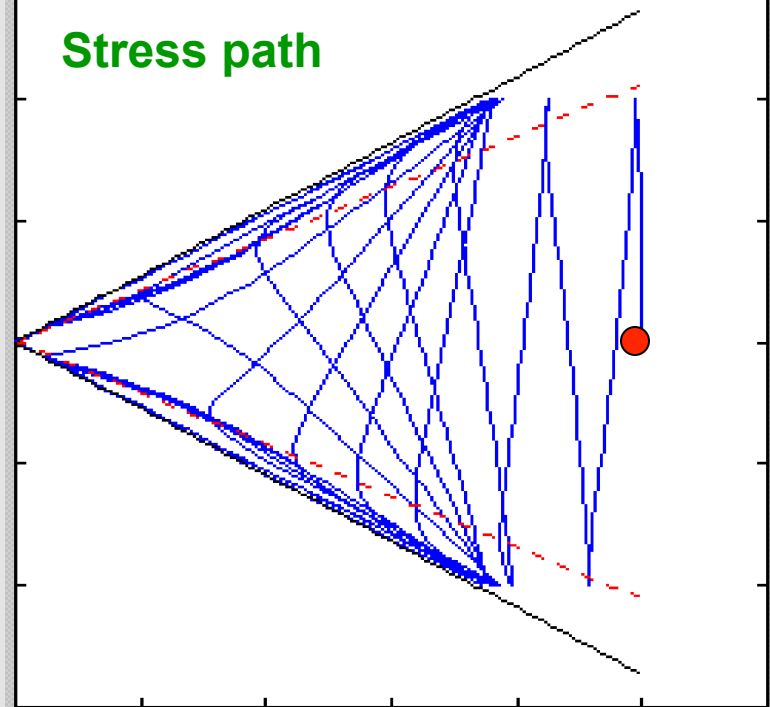


# Effects of Liquefaction

Stress-strain

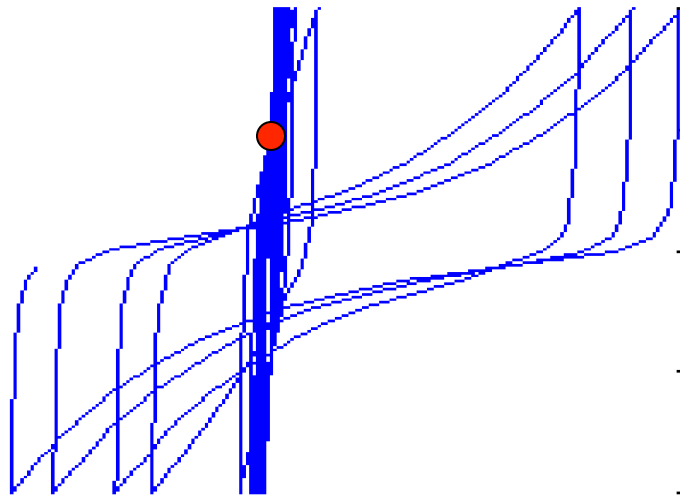


Stress path

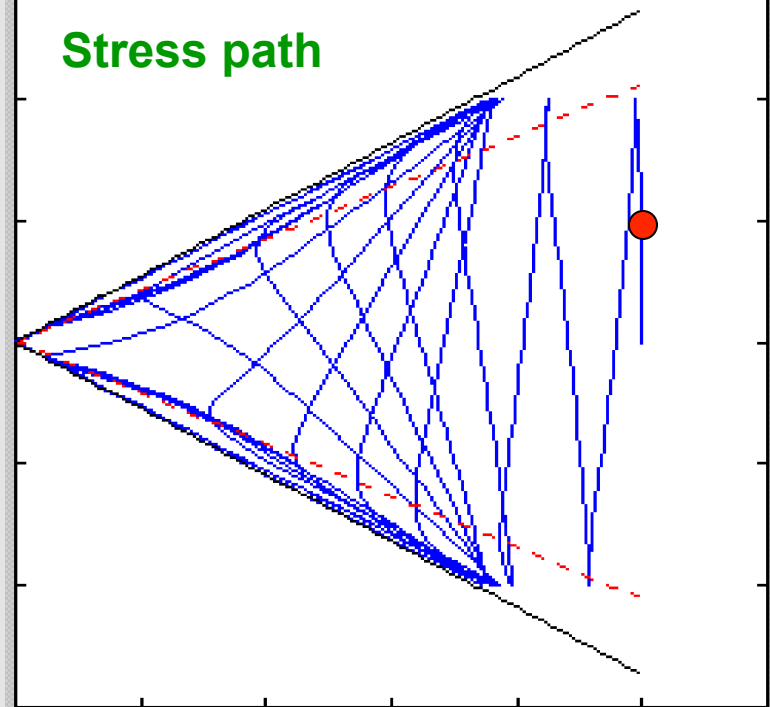


# Effects of Liquefaction

Stress-strain



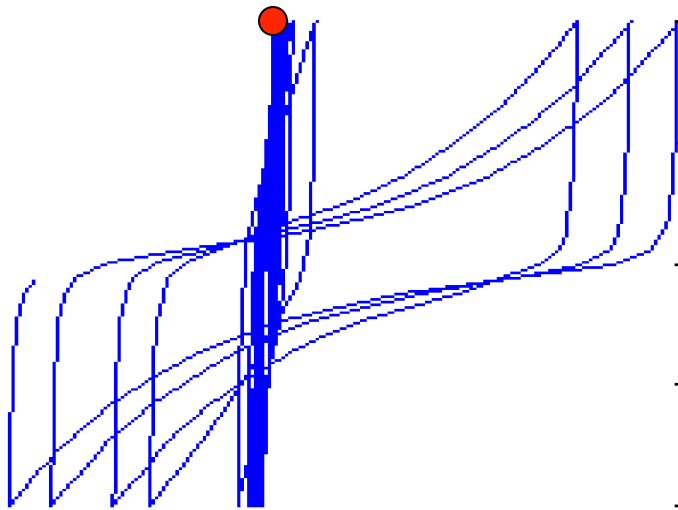
Stress path



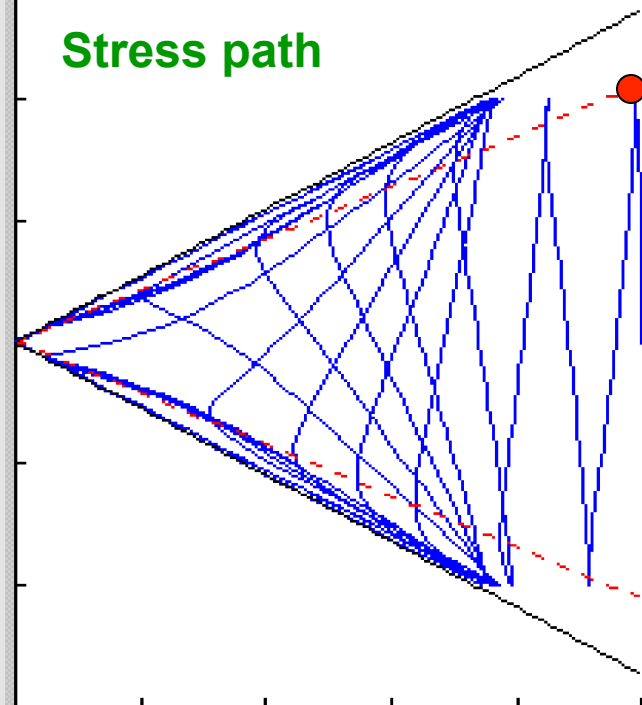


# Effects of Liquefaction

Stress-strain

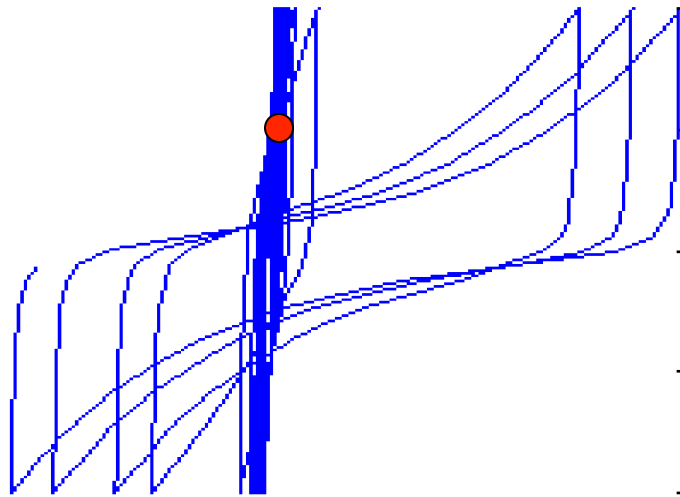


Stress path

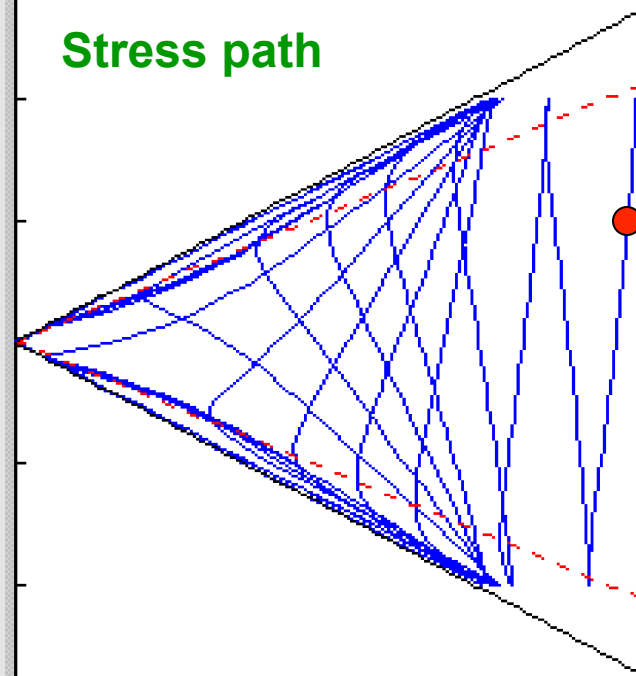


# Effects of Liquefaction

Stress-strain

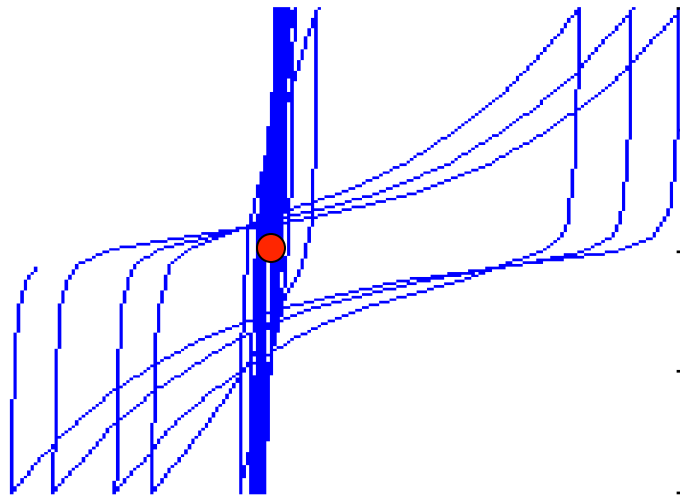


Stress path

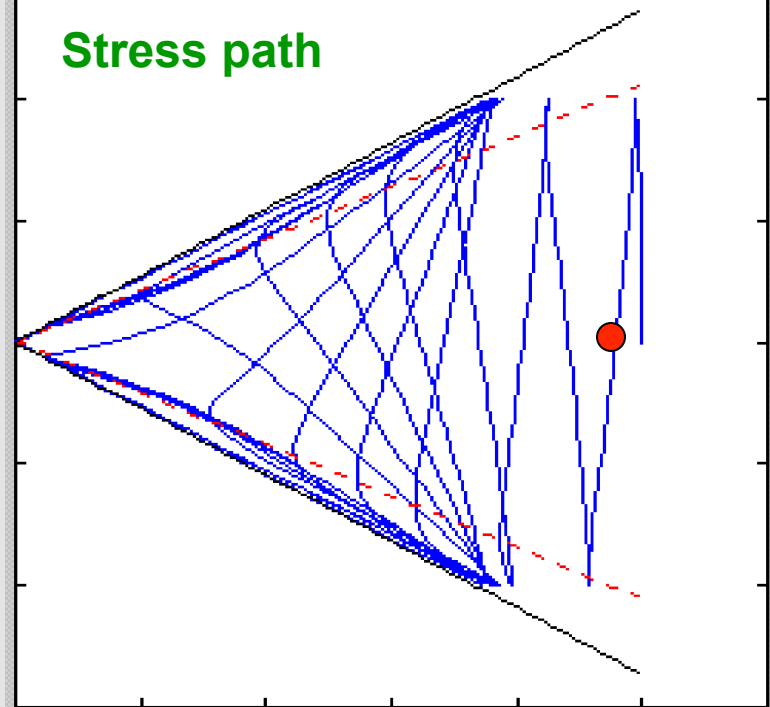


# Effects of Liquefaction

Stress-strain

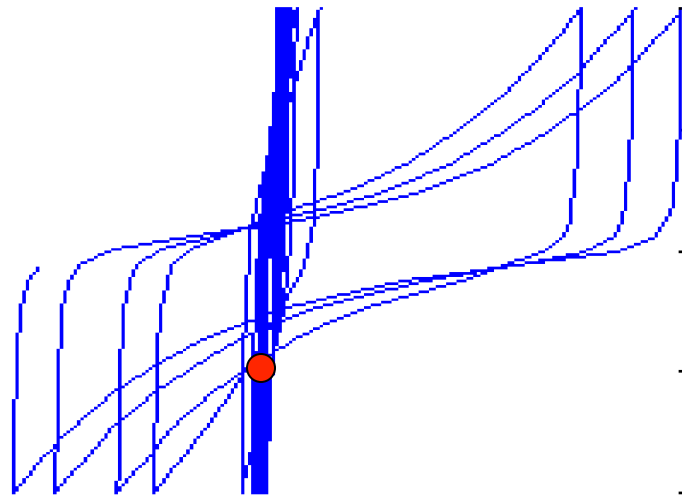


Stress path

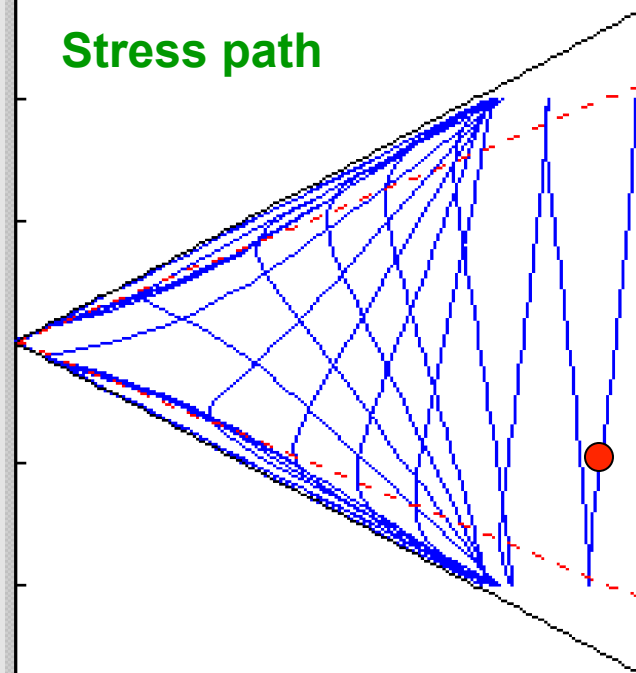


# Effects of Liquefaction

Stress-strain



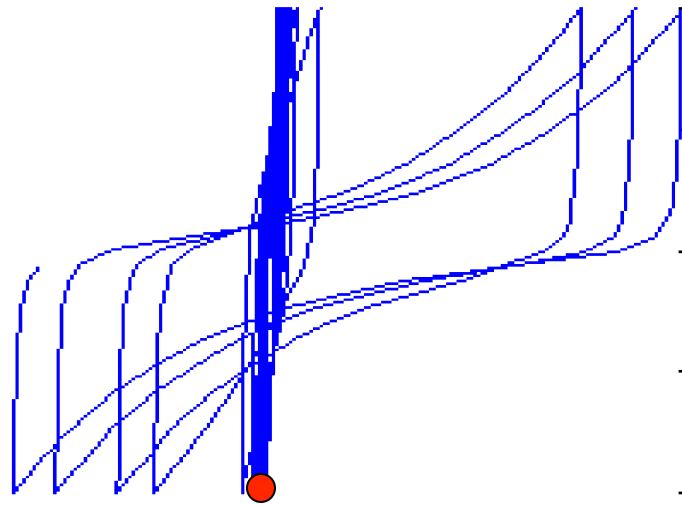
Stress path



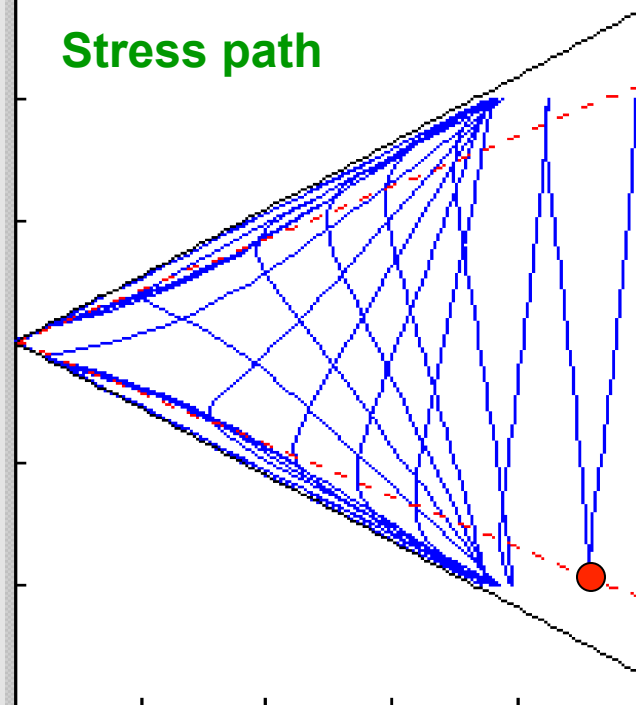


# Effects of Liquefaction

Stress-strain

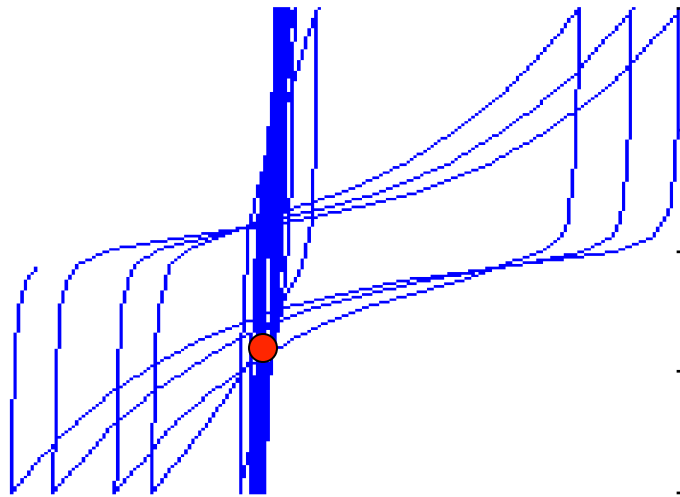


Stress path

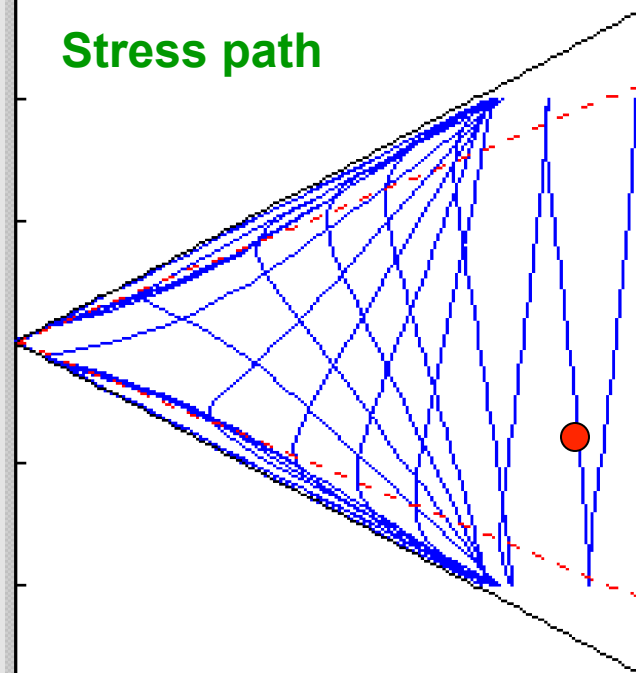


# Effects of Liquefaction

Stress-strain

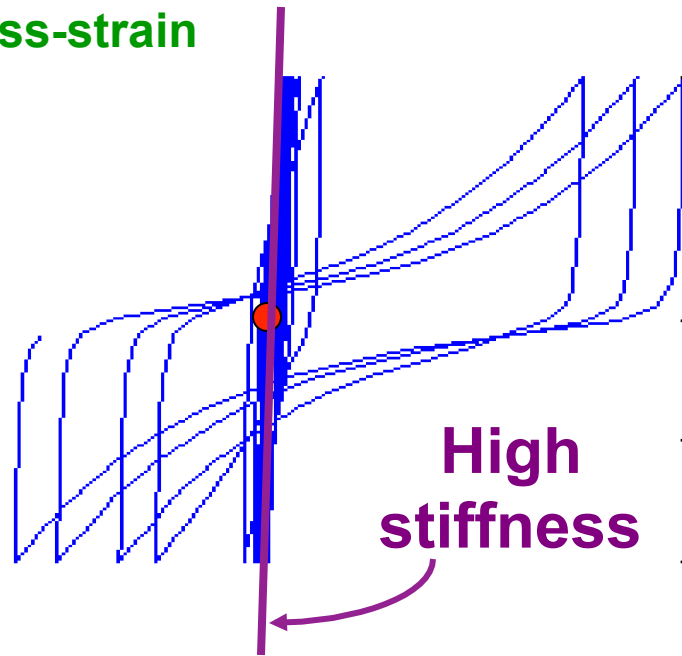


Stress path

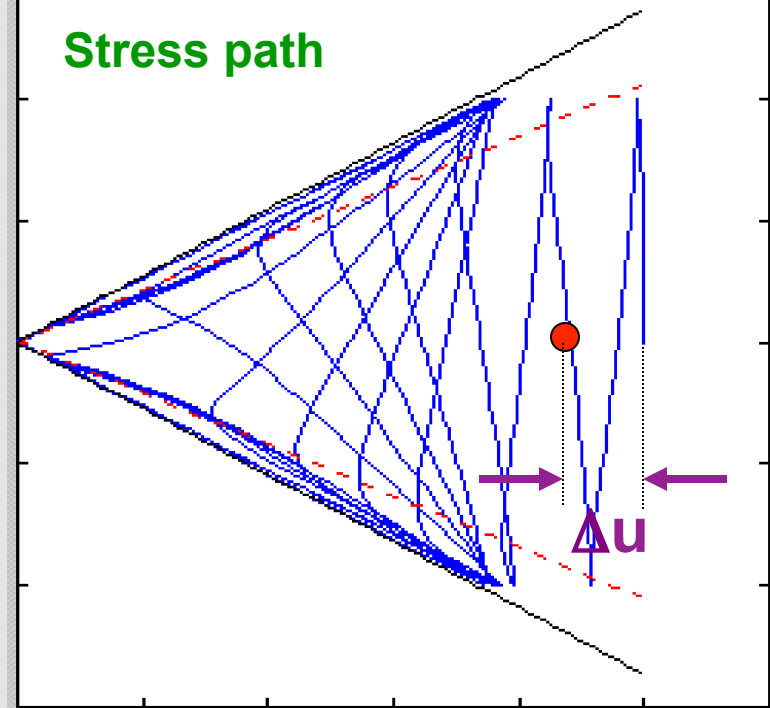


# Effects of Liquefaction

Stress-strain

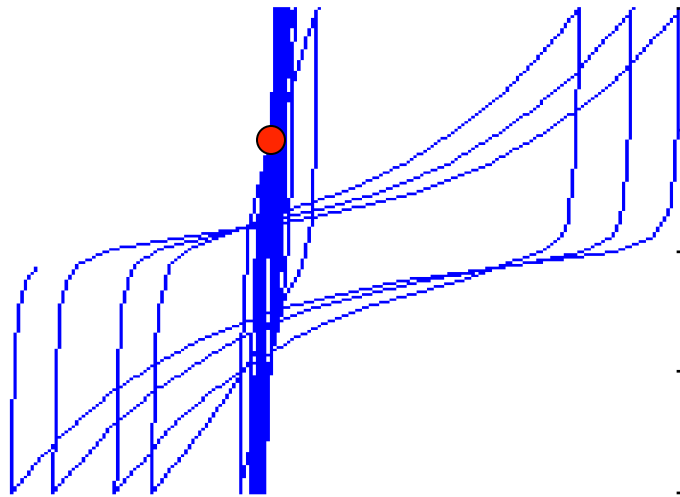


Stress path

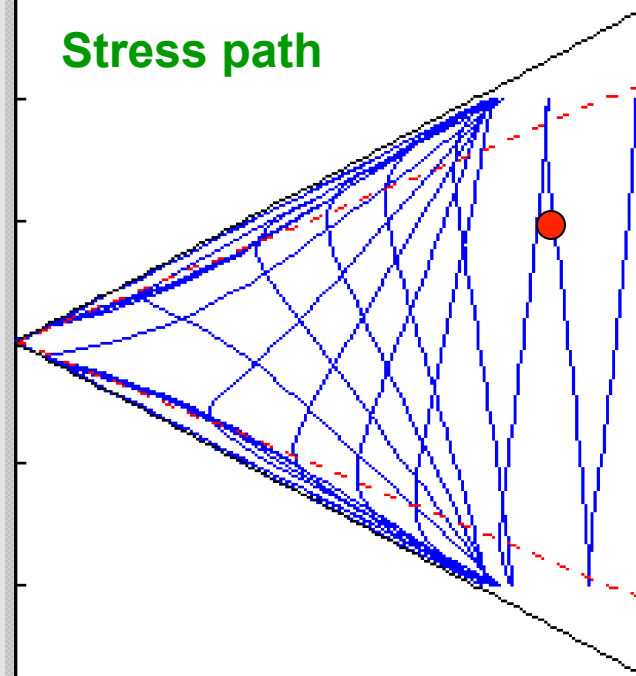


# Effects of Liquefaction

Stress-strain



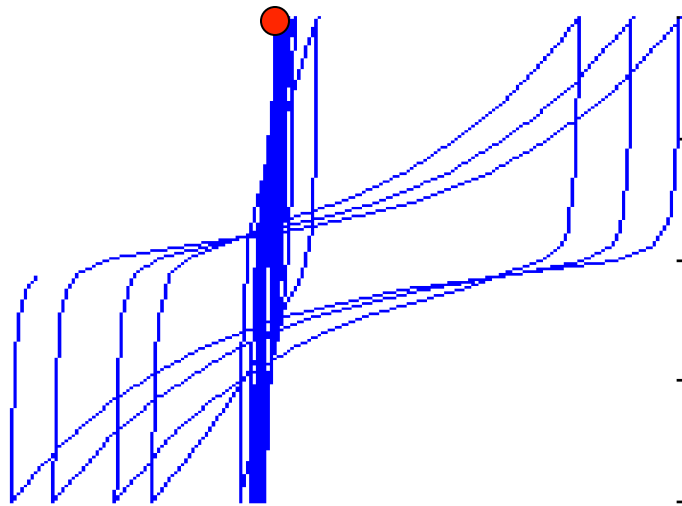
Stress path



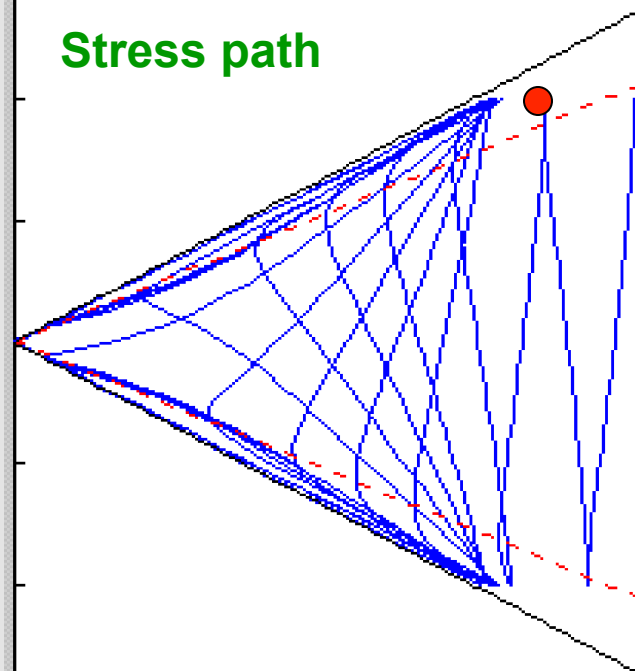


# Effects of Liquefaction

Stress-strain

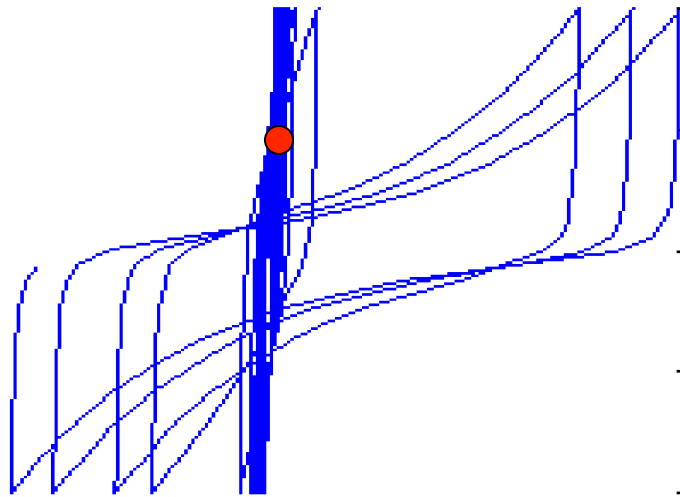


Stress path

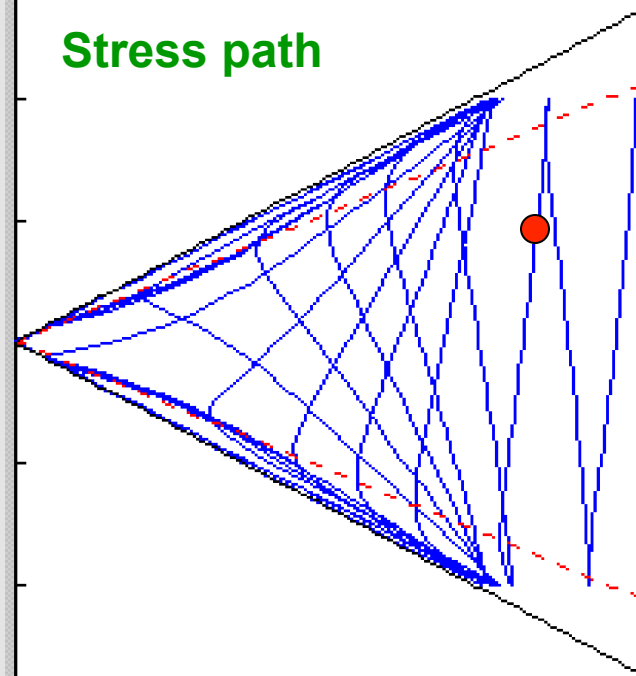


# Effects of Liquefaction

Stress-strain

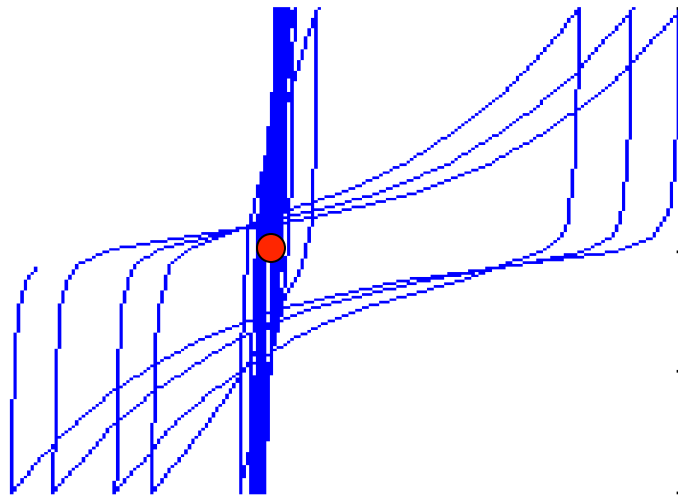


Stress path

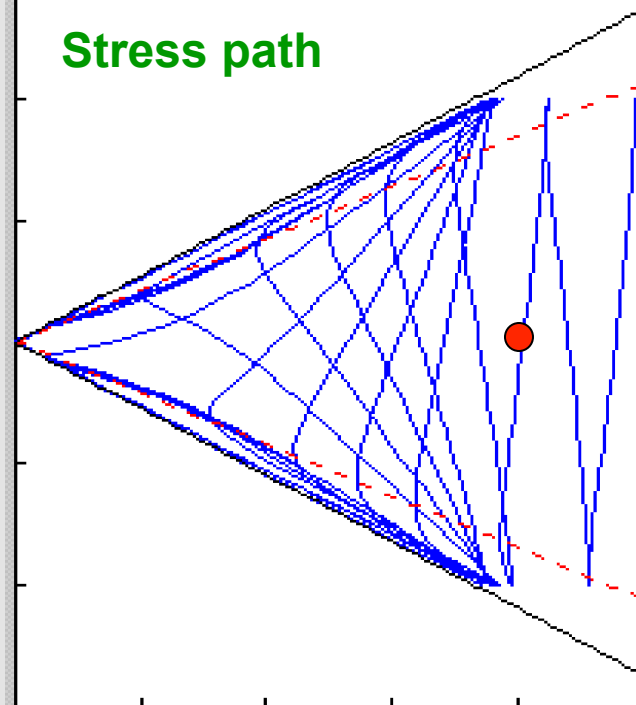


# Effects of Liquefaction

Stress-strain

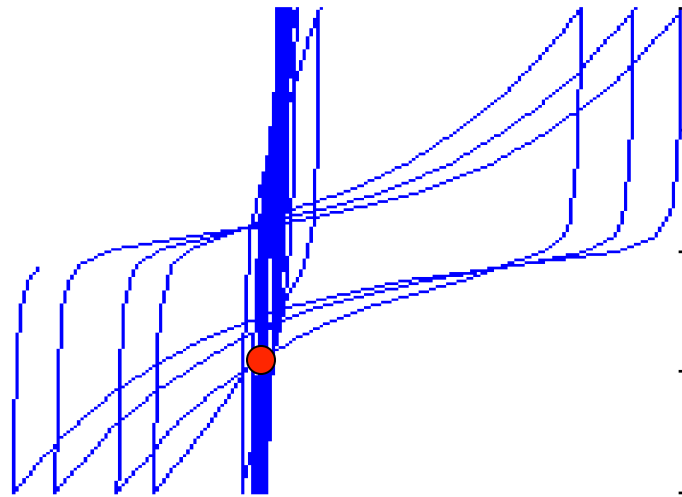


Stress path

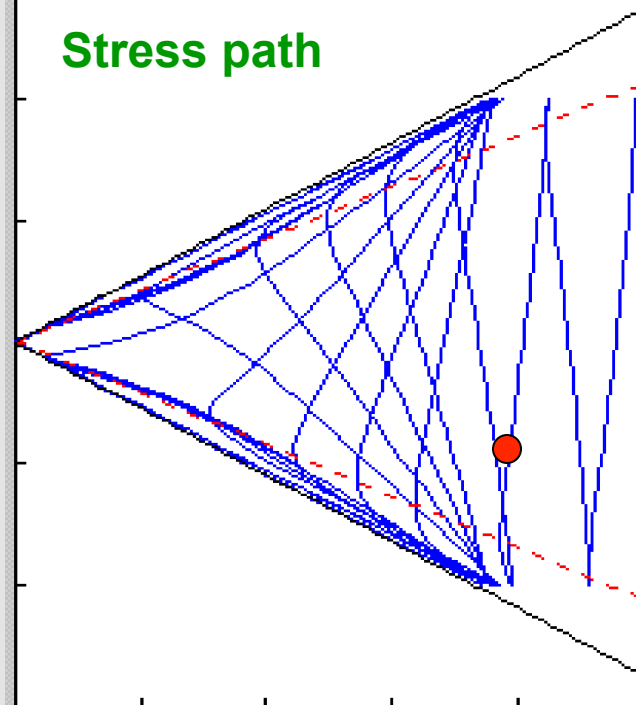


# Effects of Liquefaction

Stress-strain

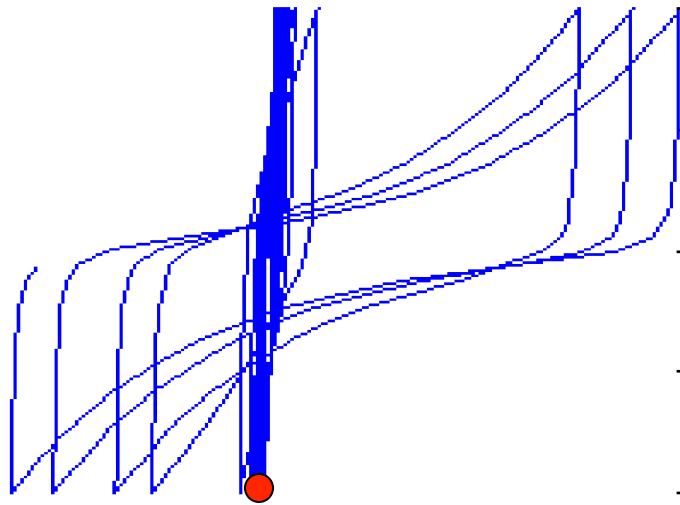


Stress path

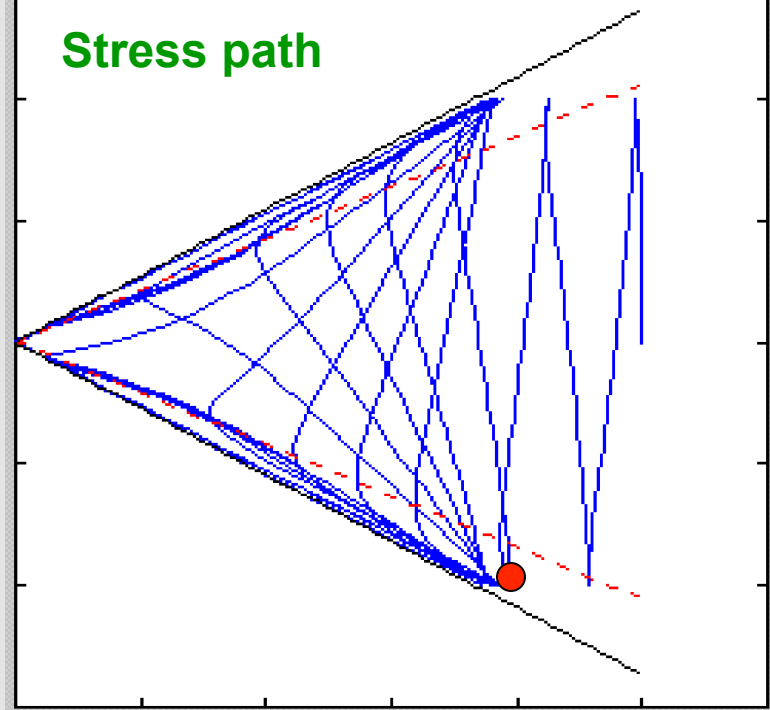


# Effects of Liquefaction

Stress-strain

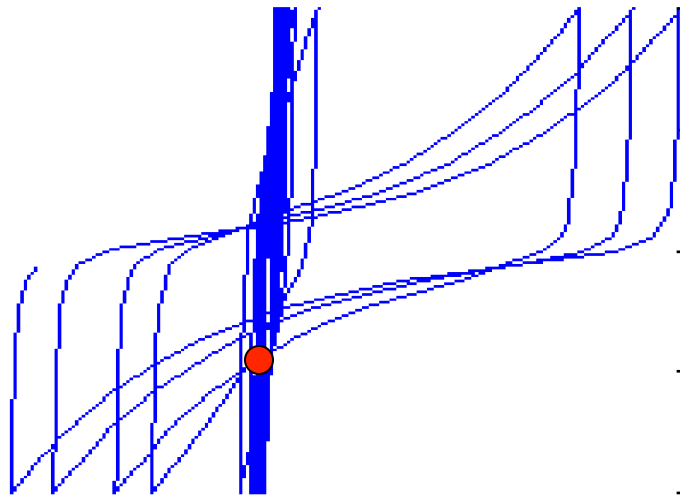


Stress path

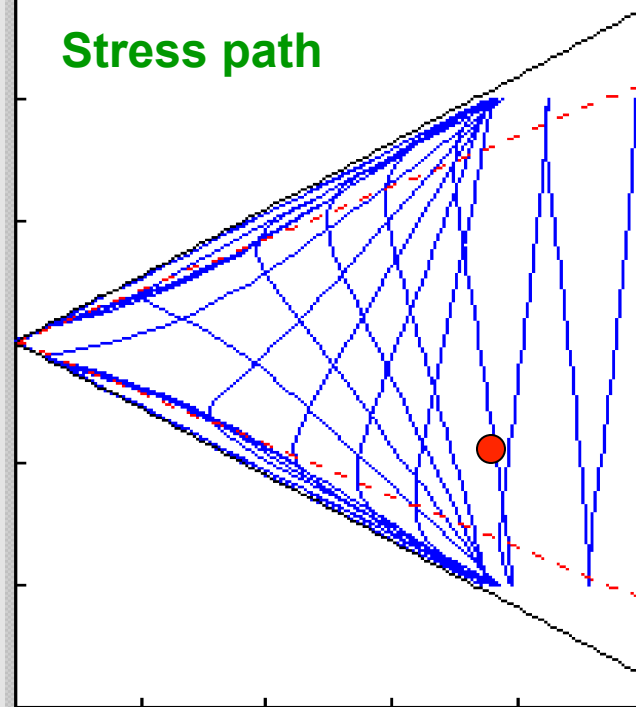


# Effects of Liquefaction

Stress-strain

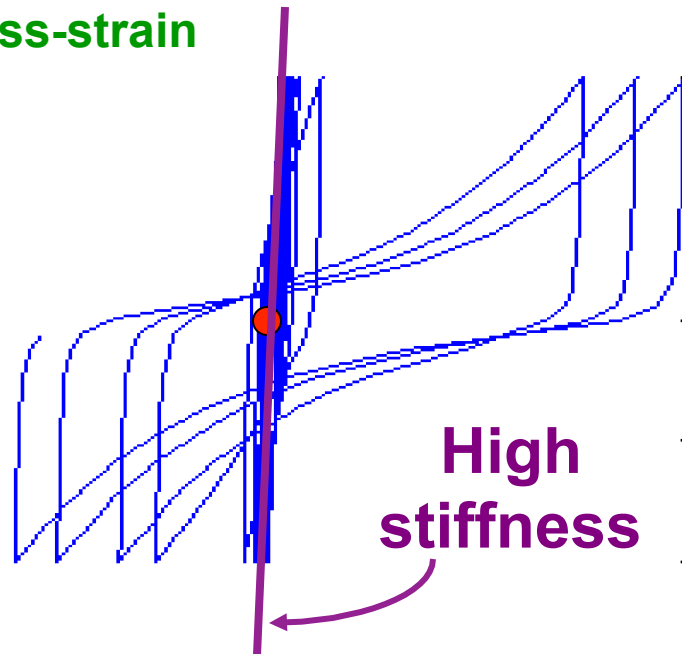


Stress path

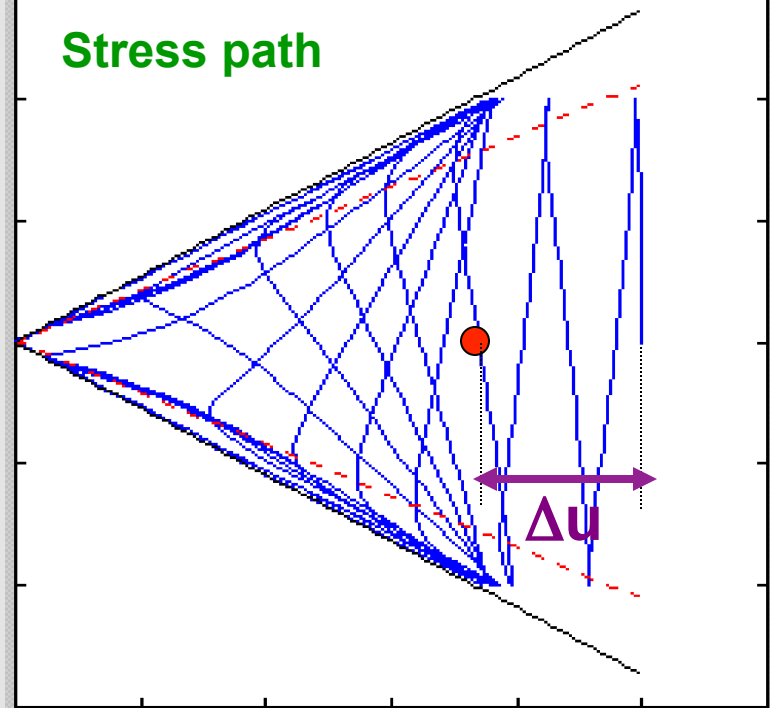


# Effects of Liquefaction

Stress-strain

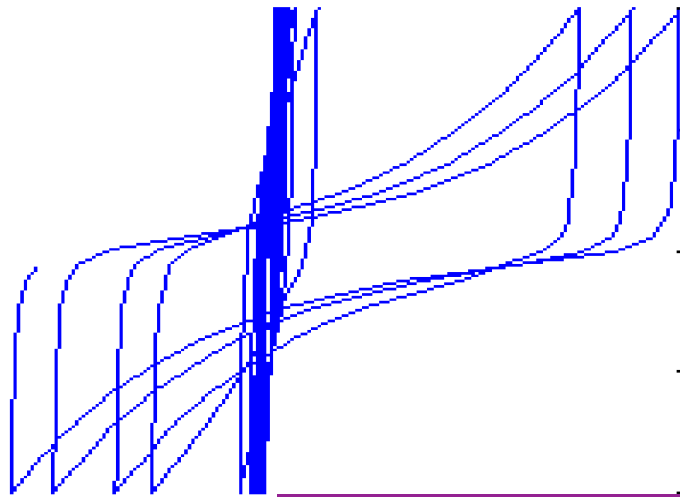


Stress path

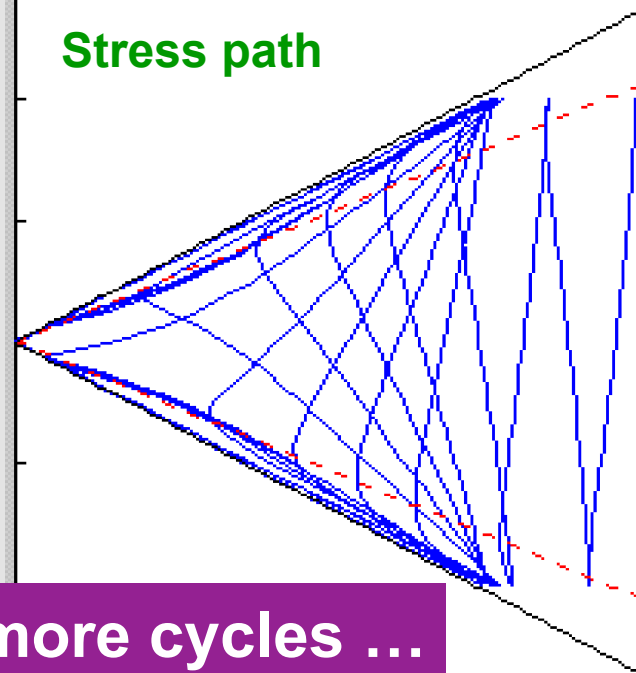


# Effects of Liquefaction

Stress-strain



Stress path

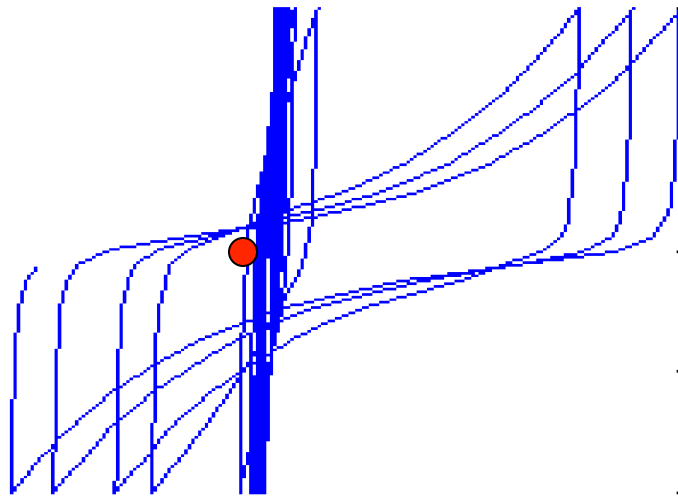


After several more cycles ...

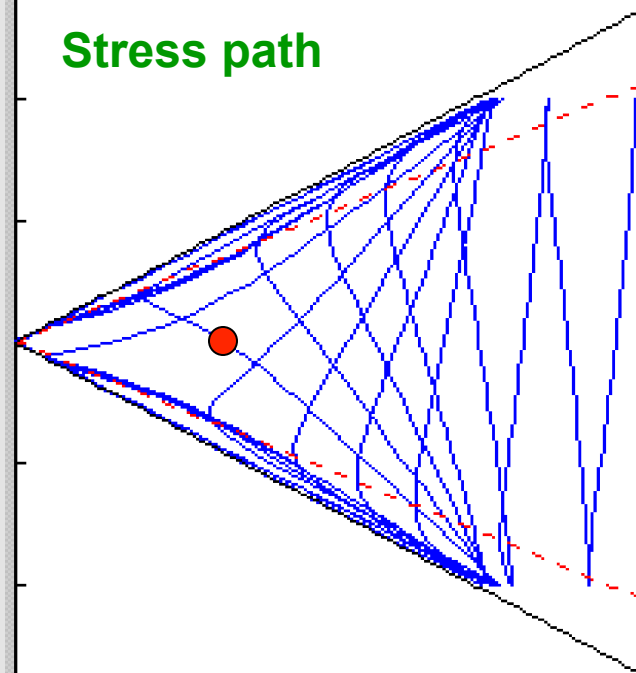


# Effects of Liquefaction

Stress-strain

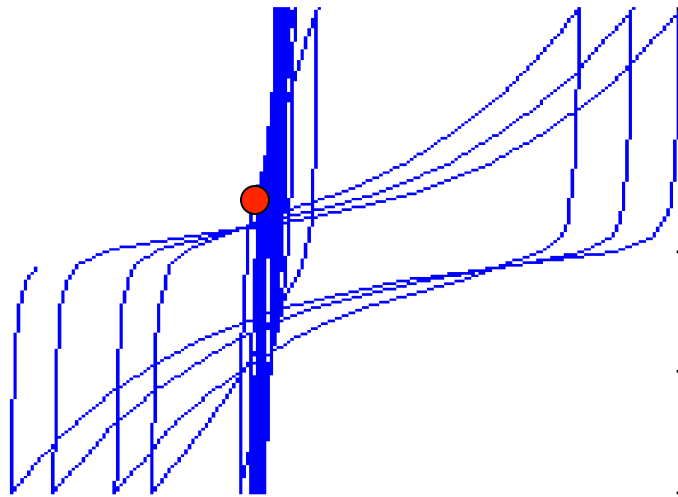


Stress path

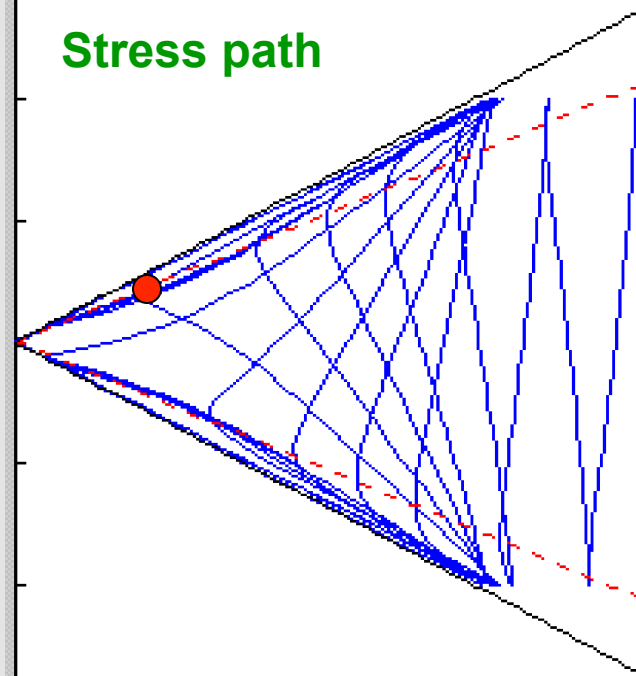


# Effects of Liquefaction

Stress-strain

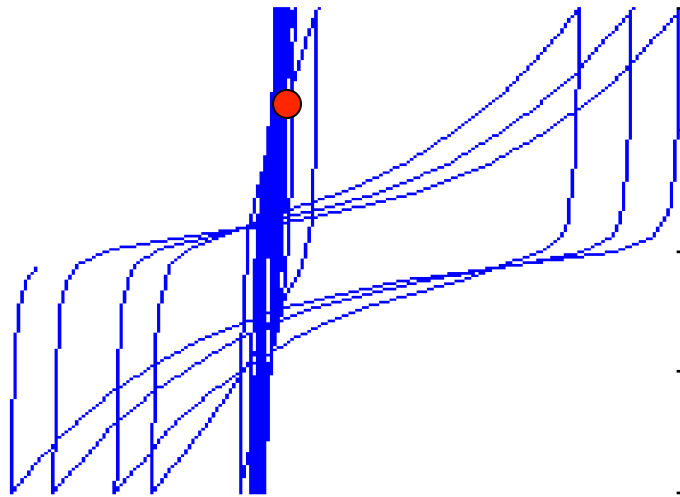


Stress path

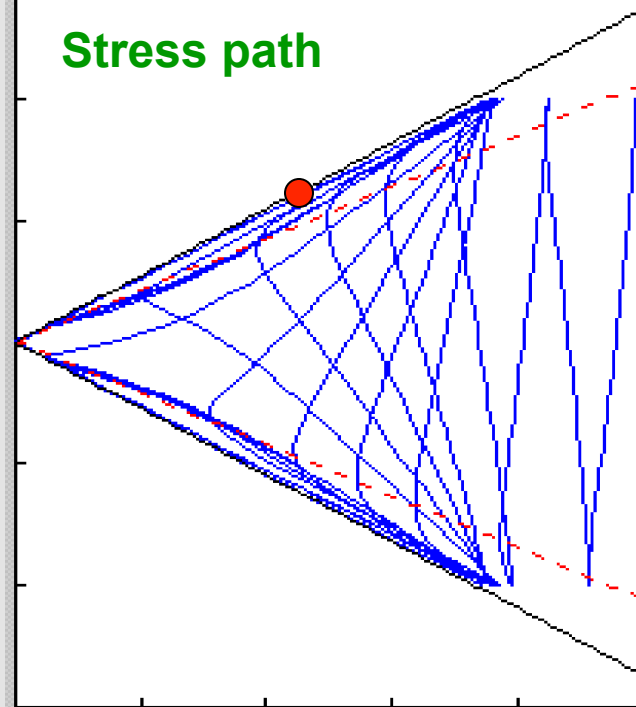


# Effects of Liquefaction

Stress-strain

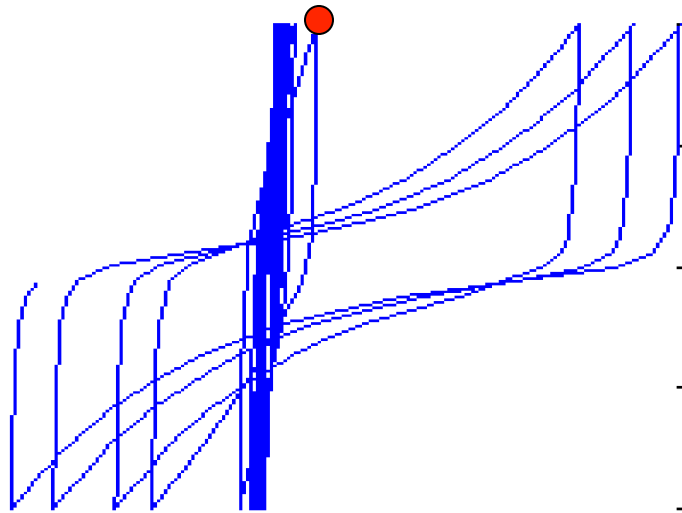


Stress path

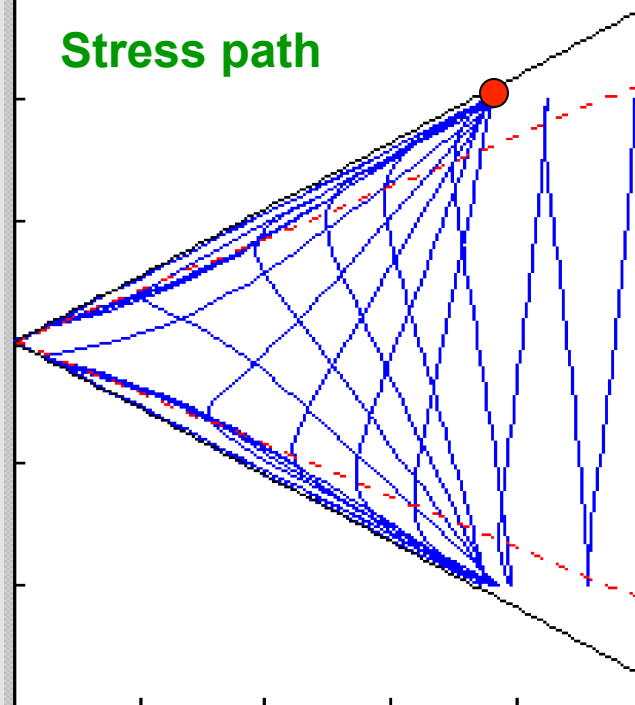


# Effects of Liquefaction

Stress-strain

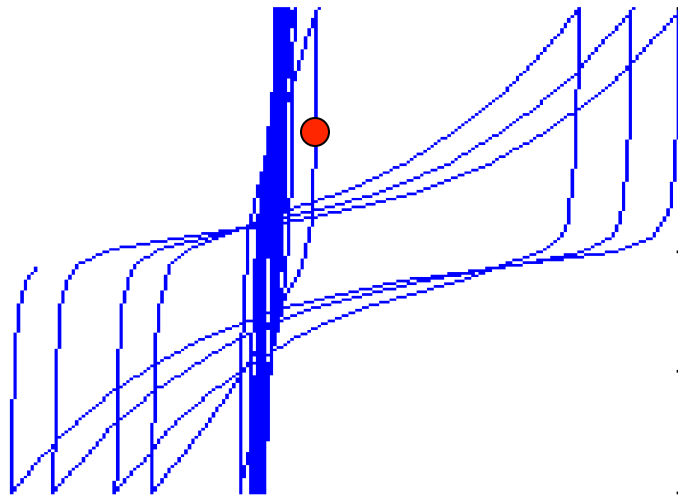


Stress path

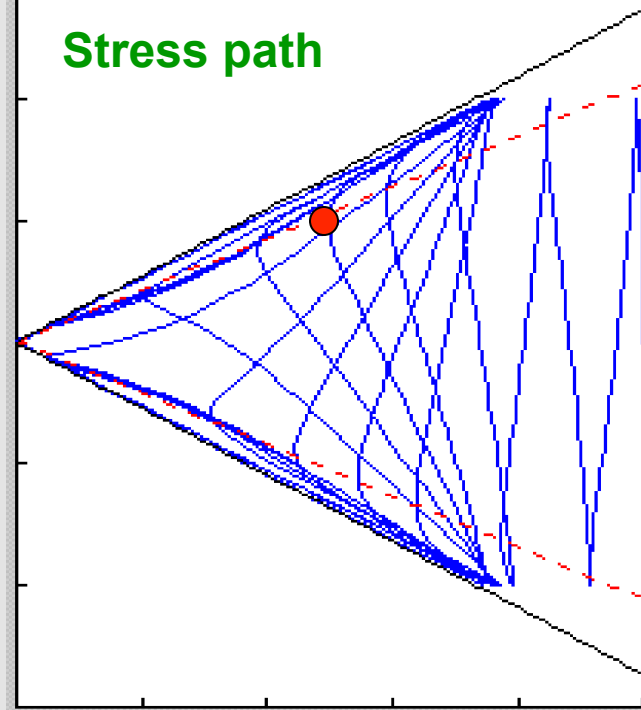


# Effects of Liquefaction

Stress-strain

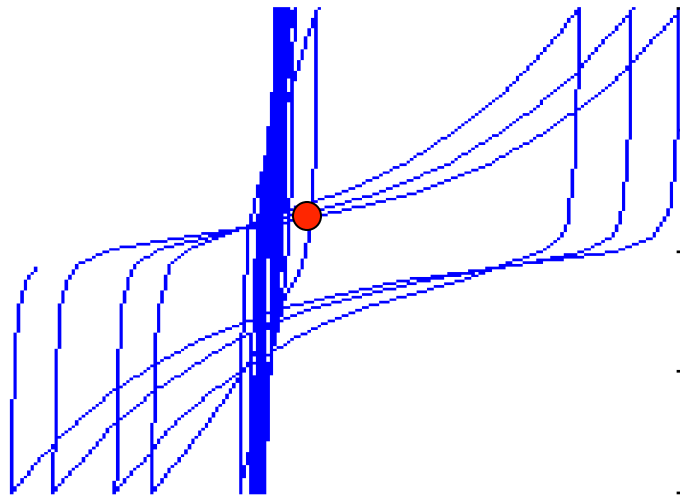


Stress path

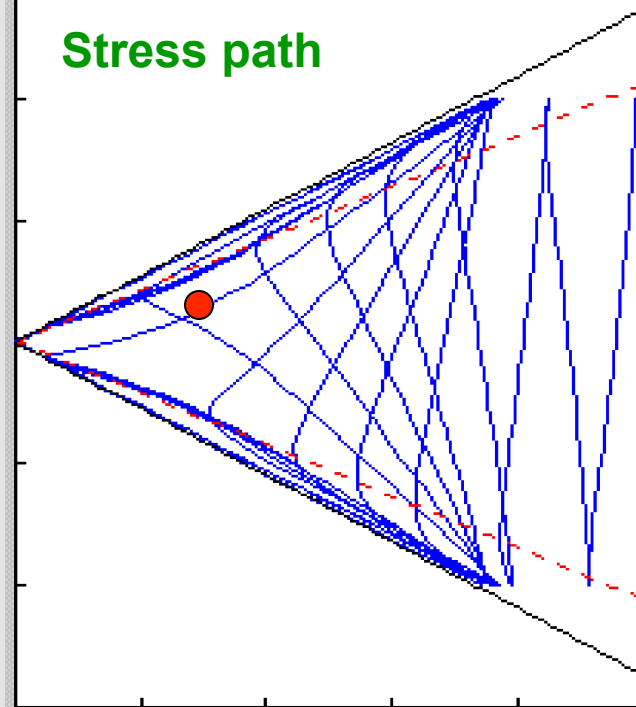


# Effects of Liquefaction

Stress-strain

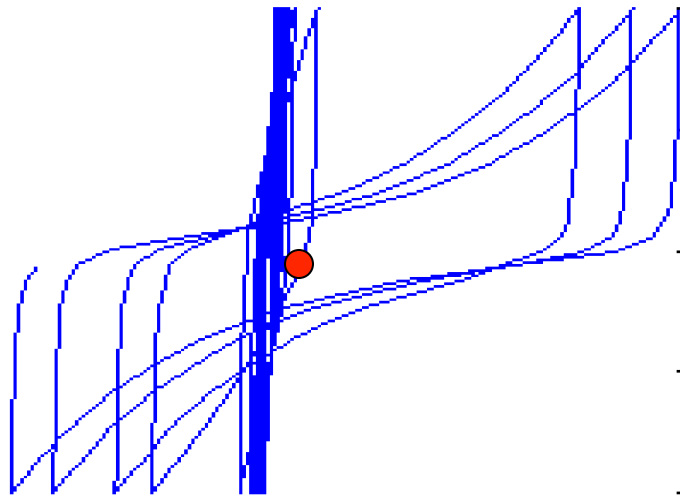


Stress path

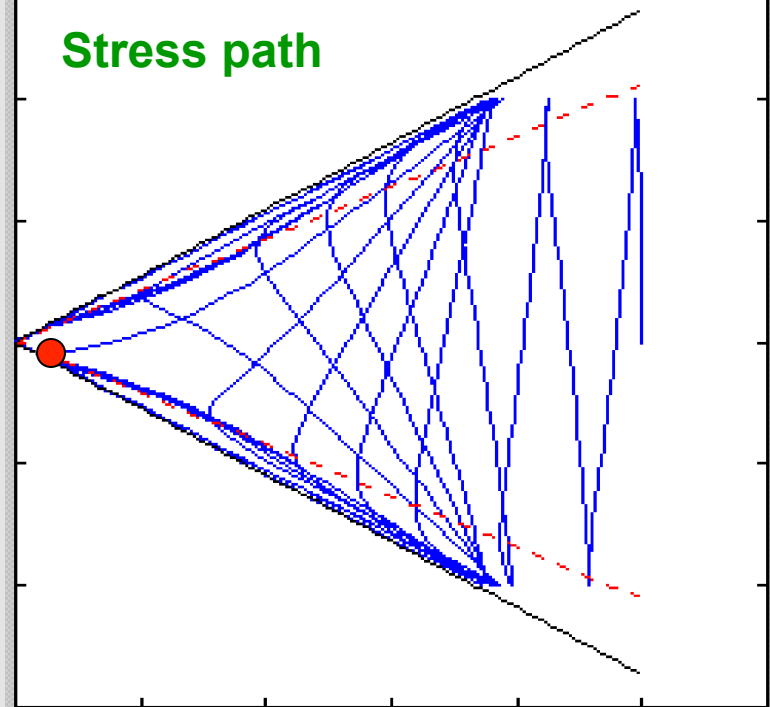


# Effects of Liquefaction

Stress-strain

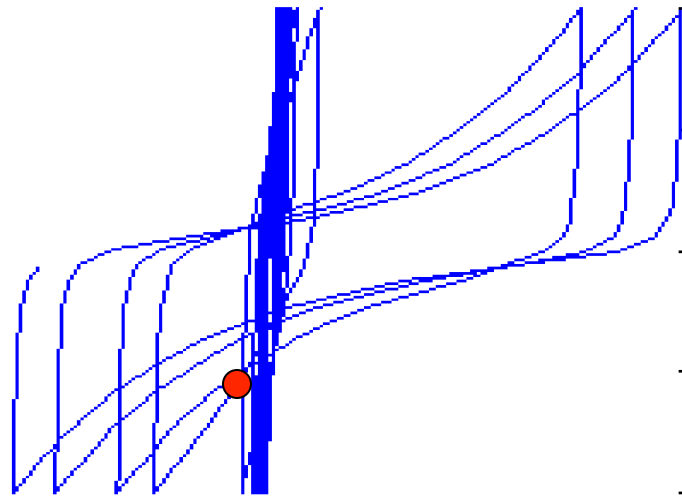


Stress path

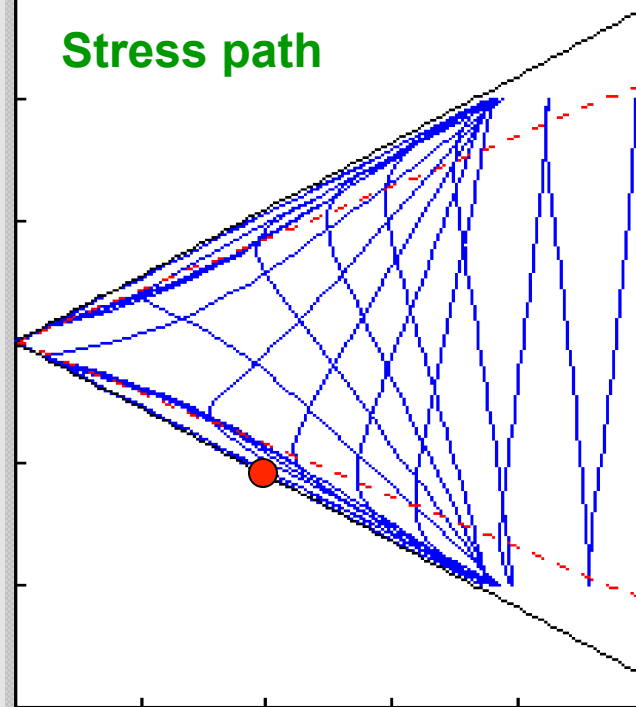


# Effects of Liquefaction

Stress-strain



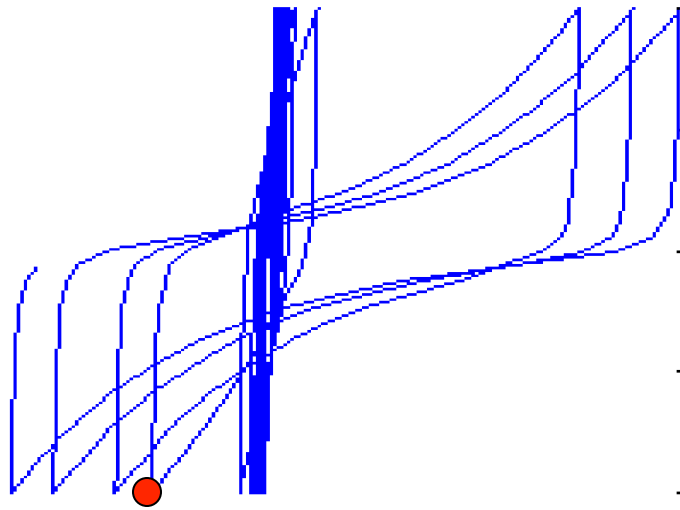
Stress path



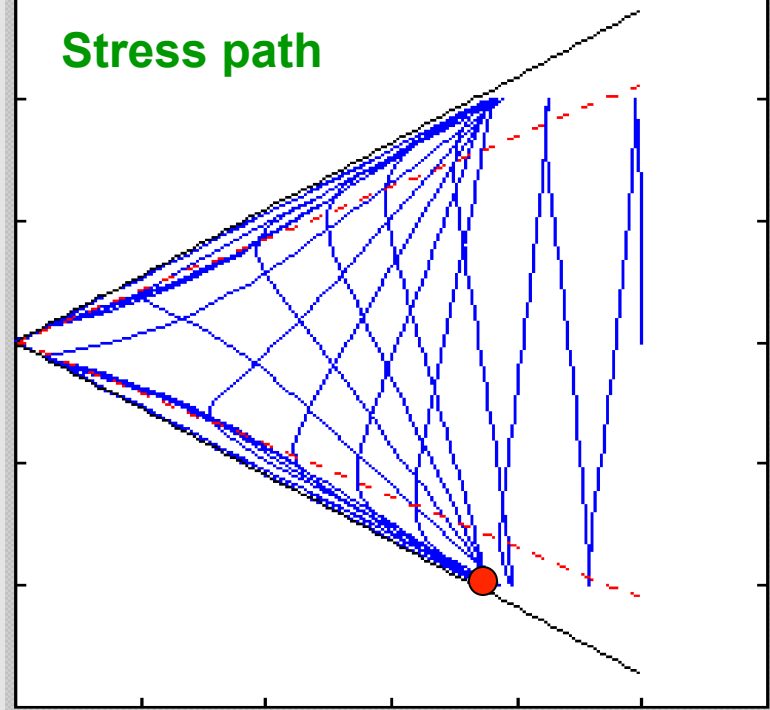


# Effects of Liquefaction

Stress-strain

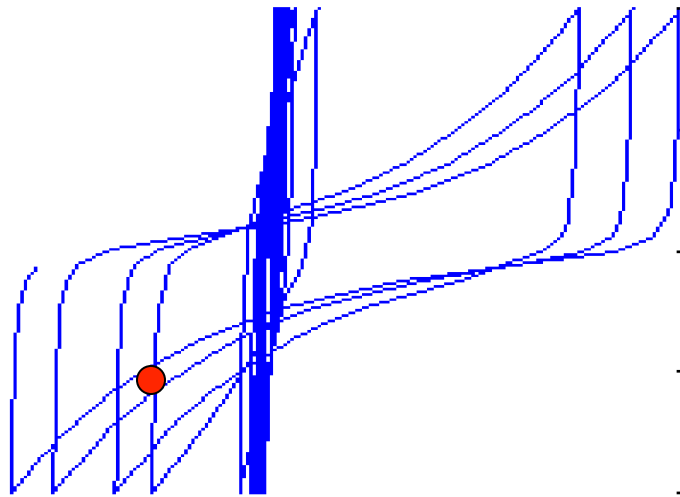


Stress path

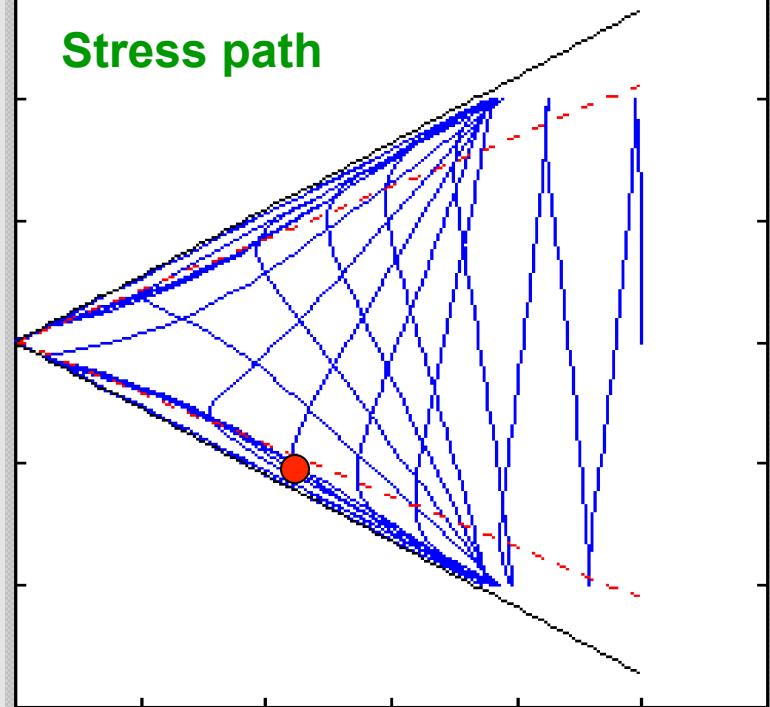


# Effects of Liquefaction

Stress-strain

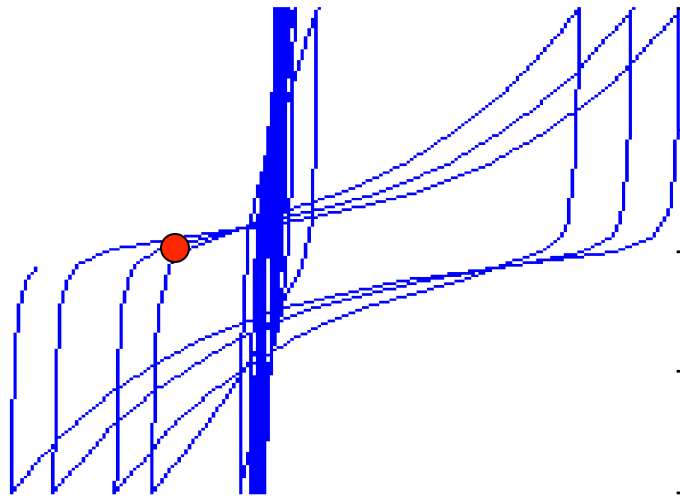


Stress path

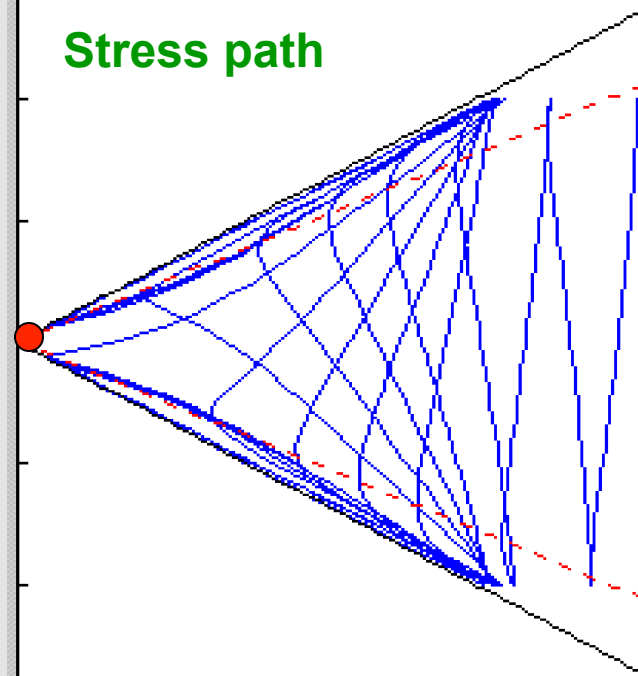


# Effects of Liquefaction

Stress-strain



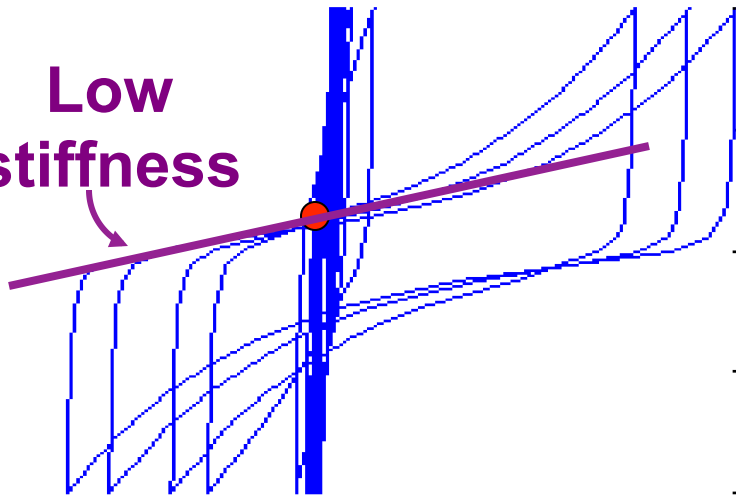
Stress path



# Effects of Liquefaction

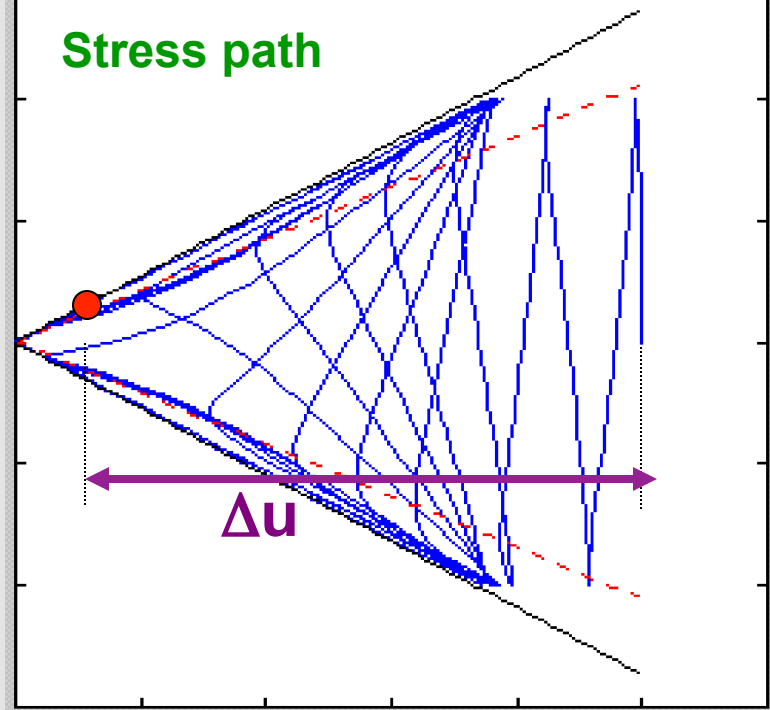
Stress-strain

Low  
stiffness



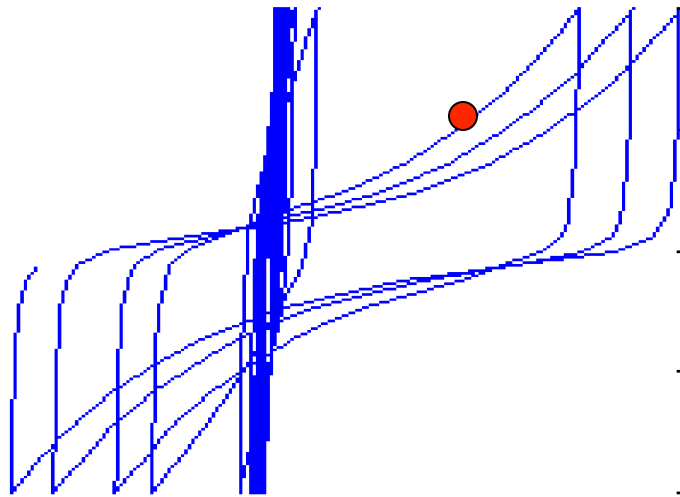
Stress path

$\Delta u$

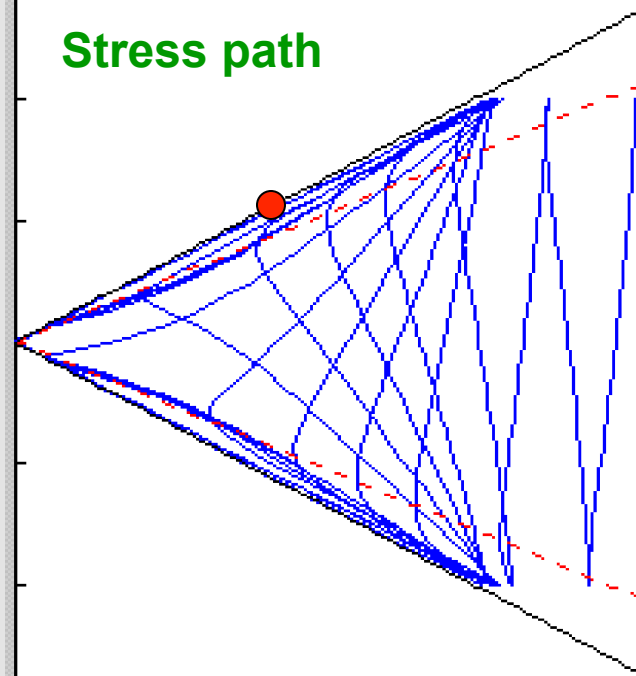


# Effects of Liquefaction

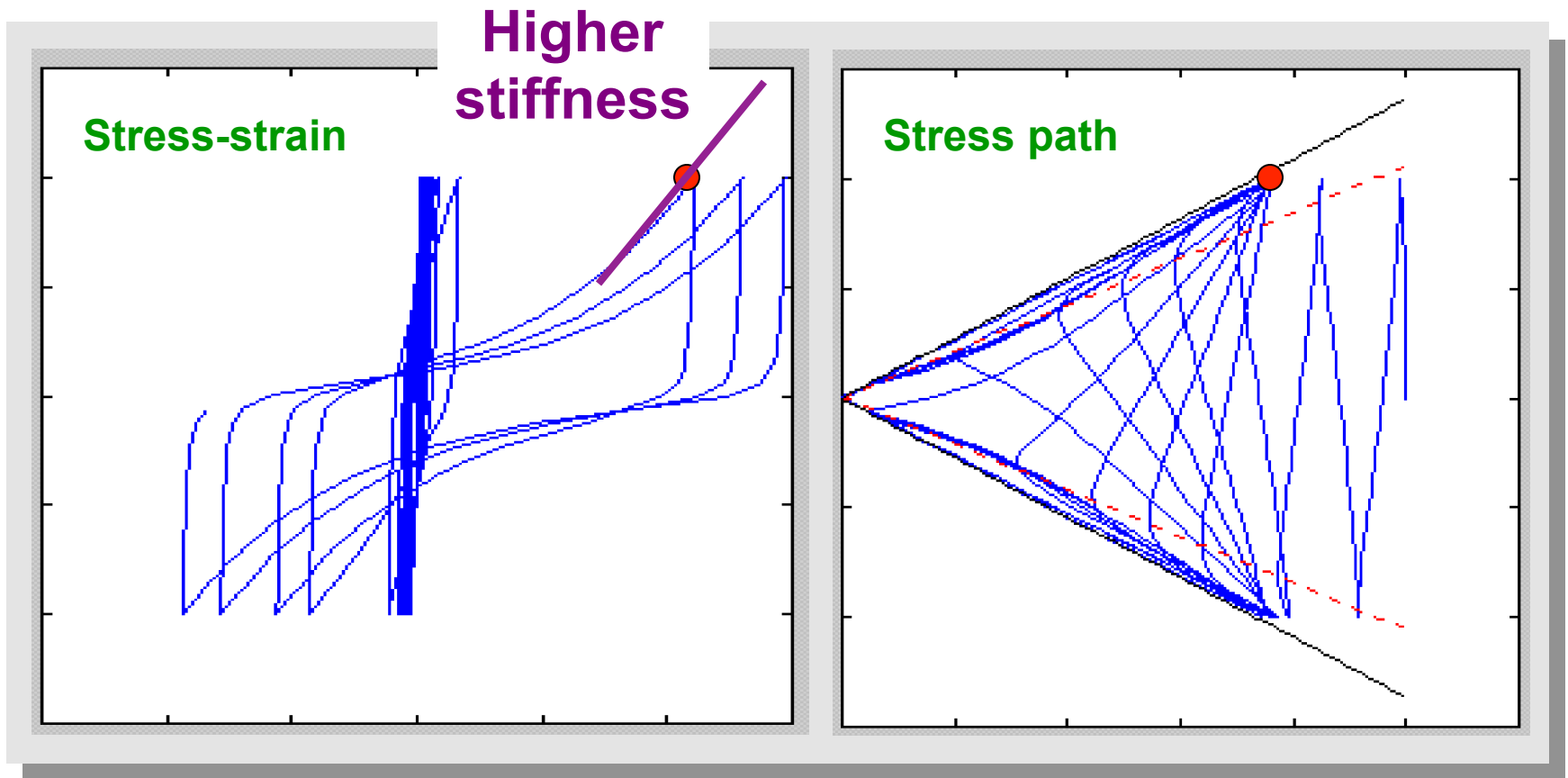
Stress-strain



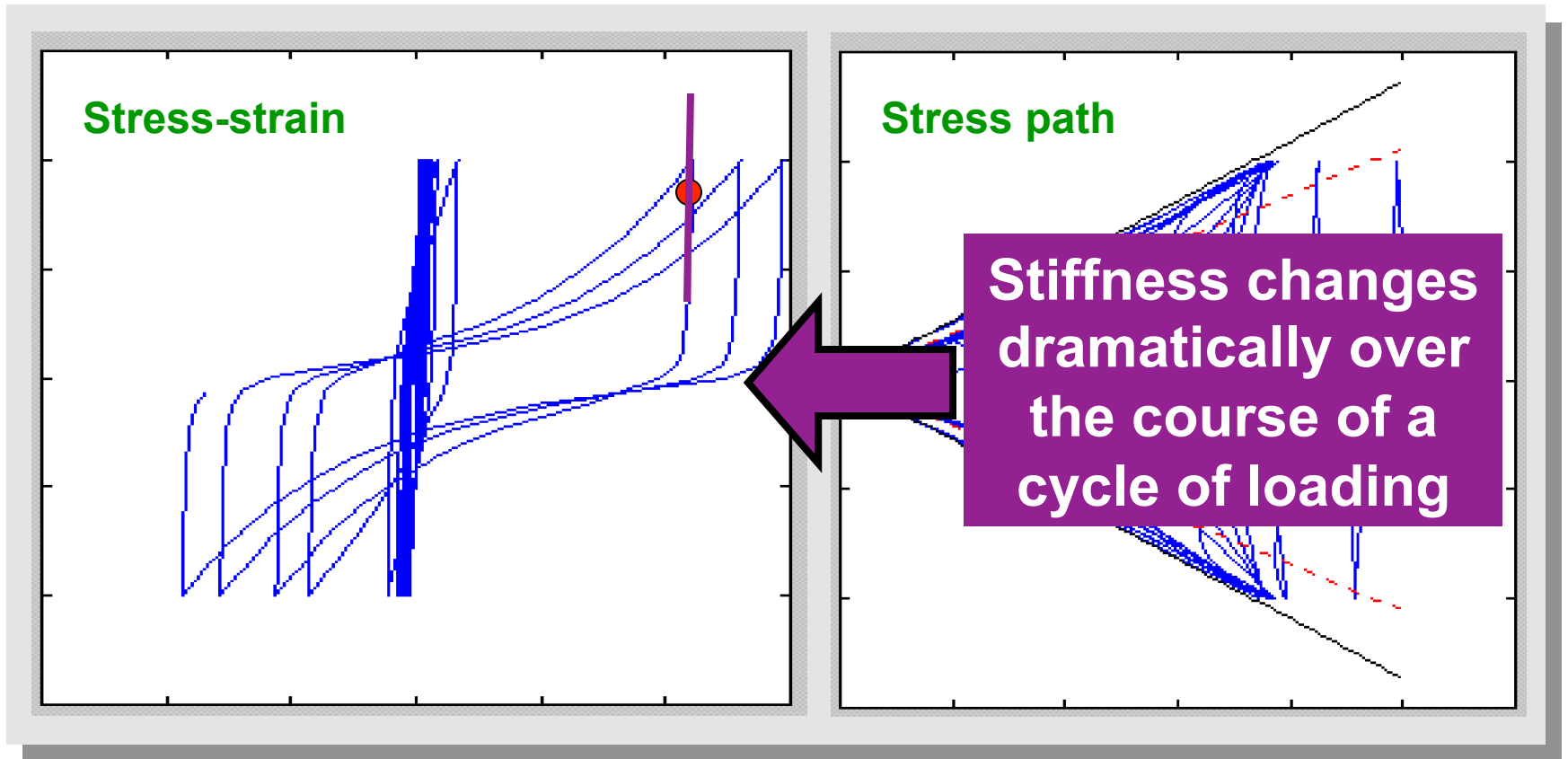
Stress path



# Effects of Liquefaction

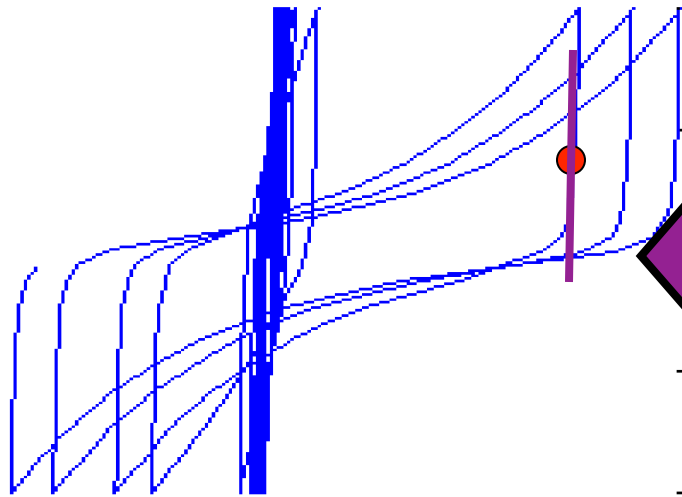


# Effects of Liquefaction

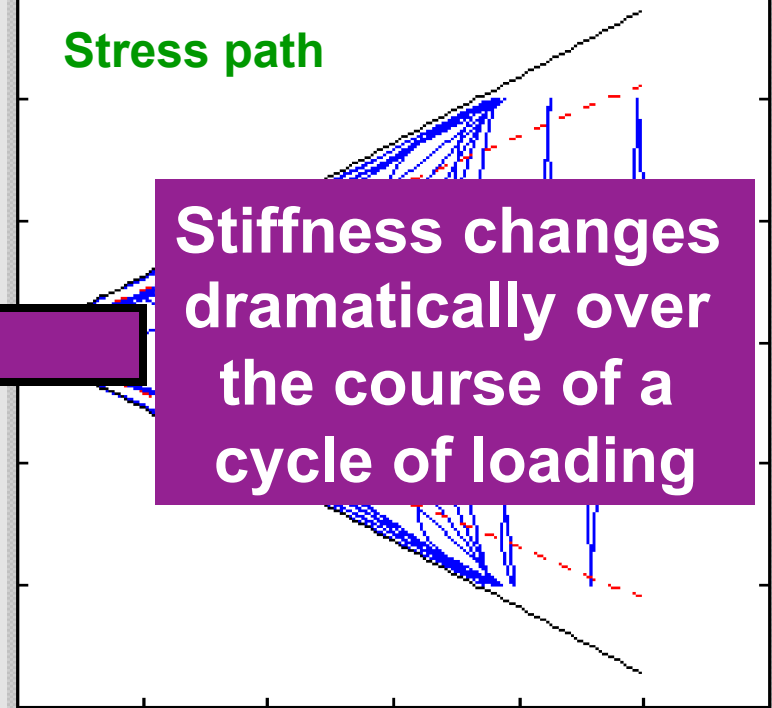


# Effects of Liquefaction

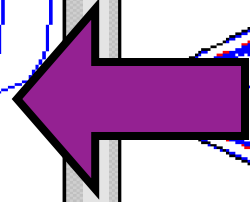
Stress-strain



Stress path



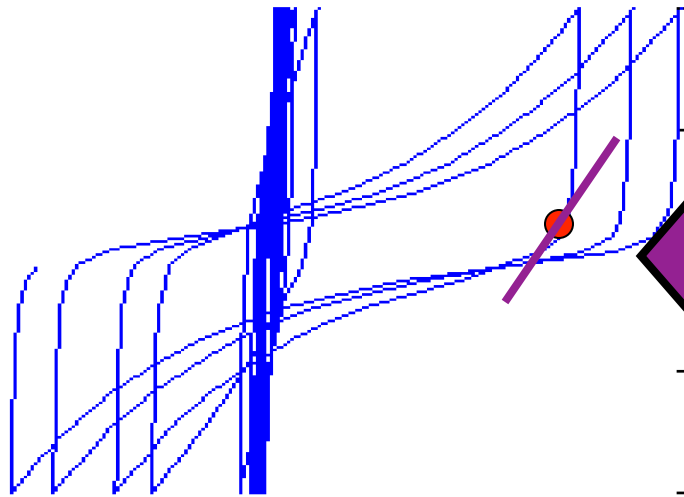
Stiffness changes dramatically over the course of a cycle of loading



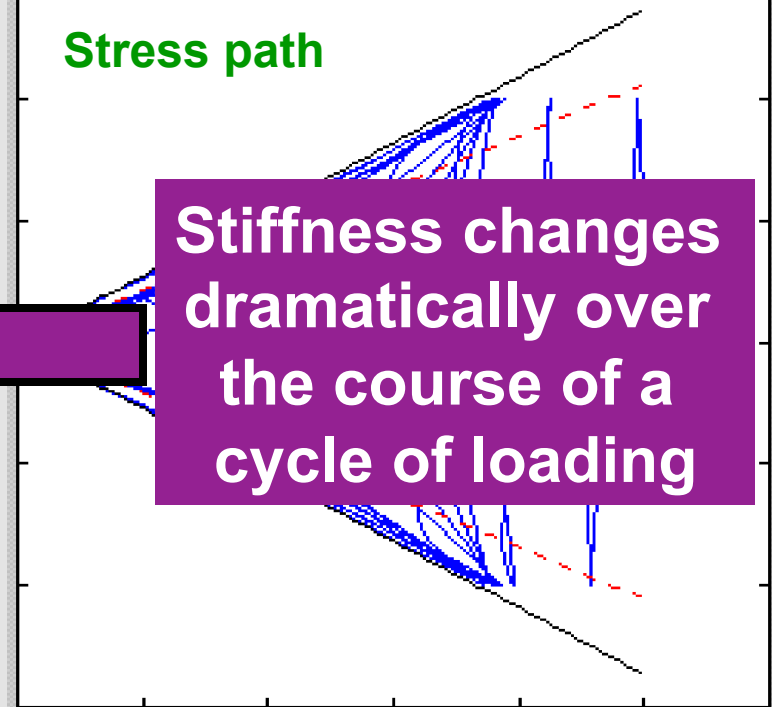


# Effects of Liquefaction

Stress-strain



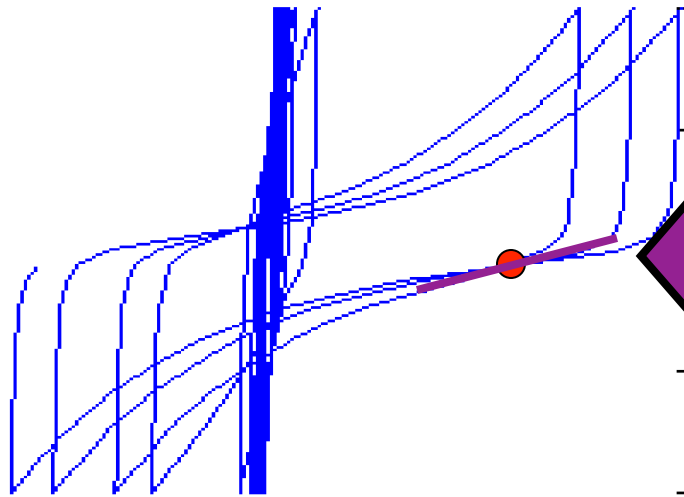
Stress path



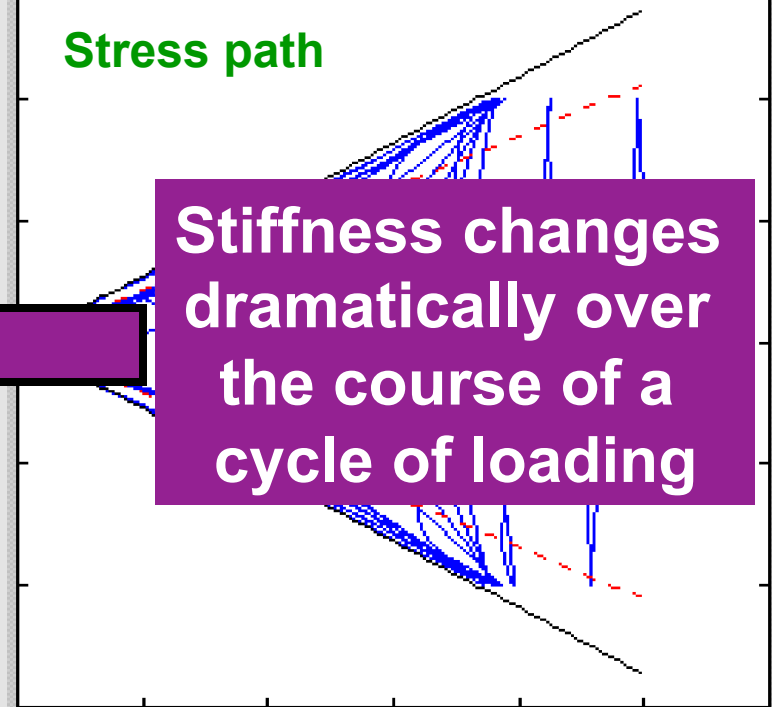
Stiffness changes dramatically over the course of a cycle of loading

# Effects of Liquefaction

Stress-strain



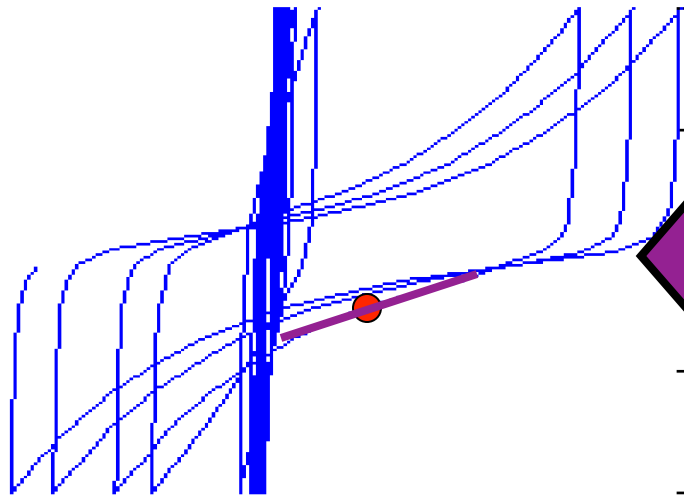
Stress path



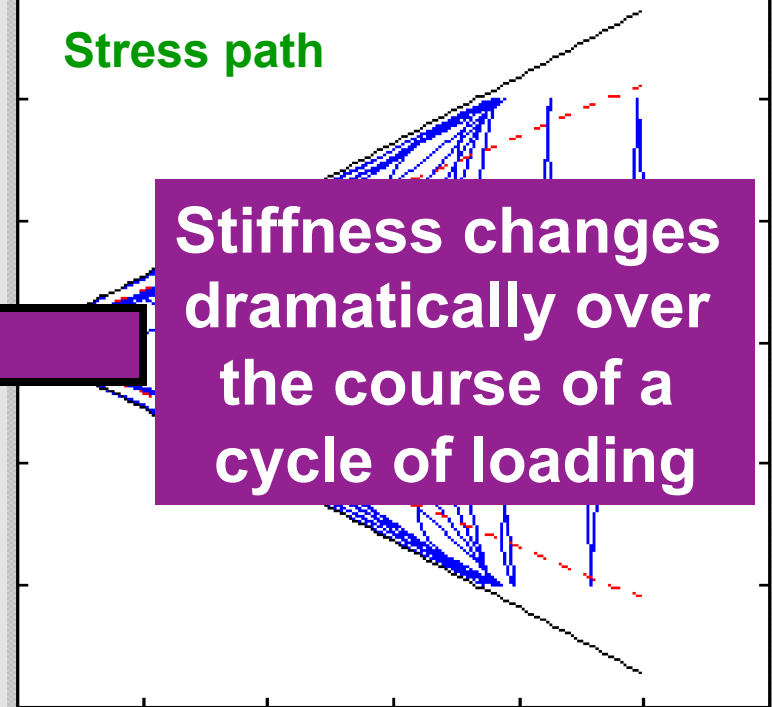
Stiffness changes dramatically over the course of a cycle of loading

# Effects of Liquefaction

Stress-strain



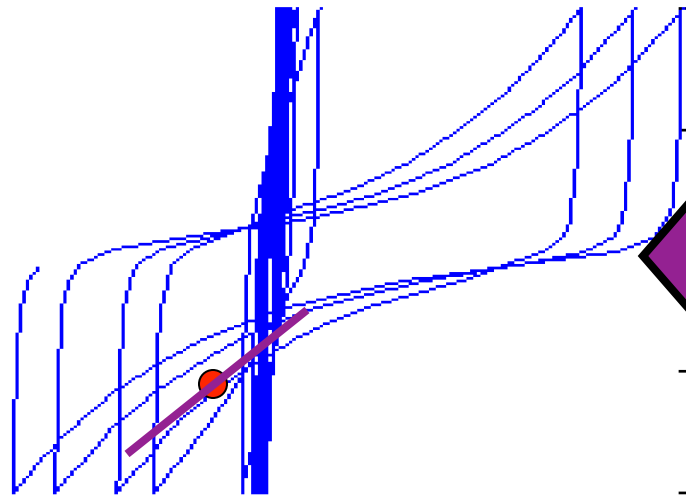
Stress path



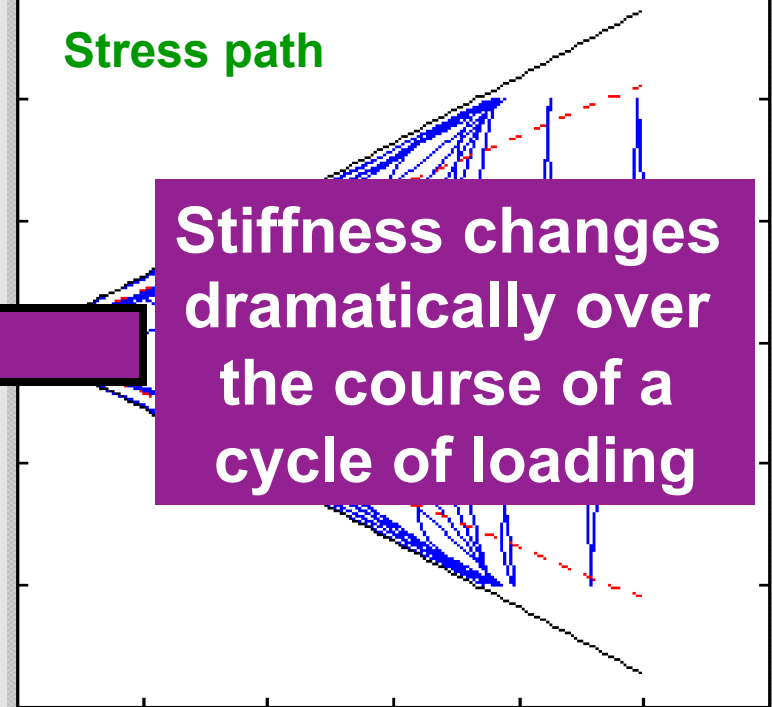
Stiffness changes dramatically over the course of a cycle of loading

# Effects of Liquefaction

Stress-strain



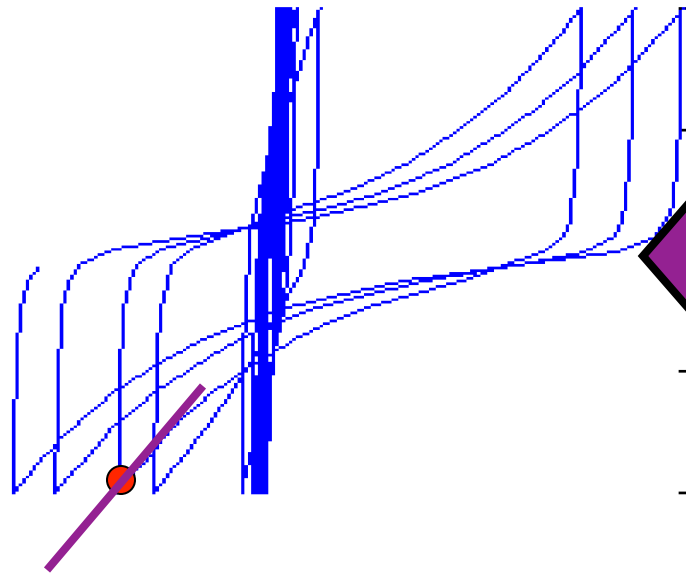
Stress path



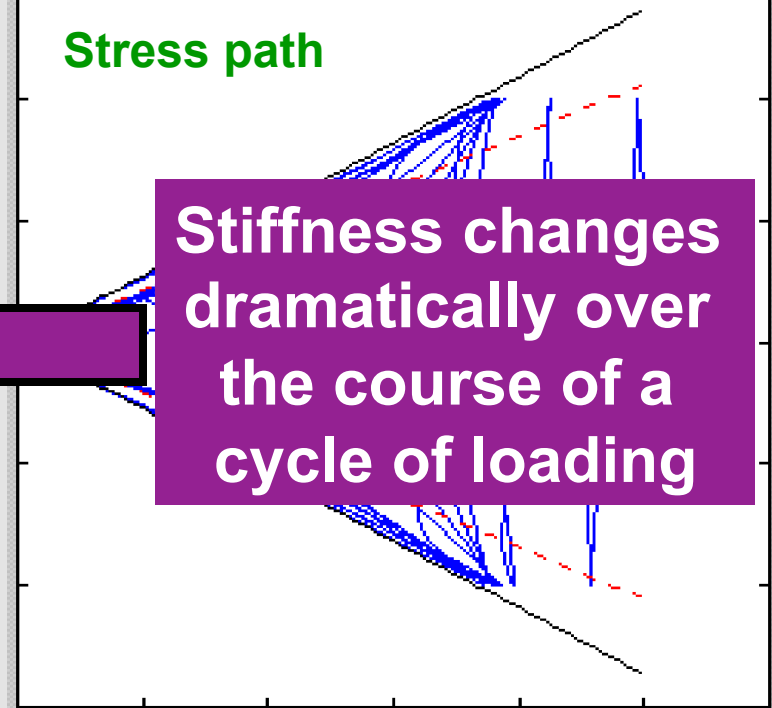
Stiffness changes dramatically over the course of a cycle of loading

# Effects of Liquefaction

Stress-strain

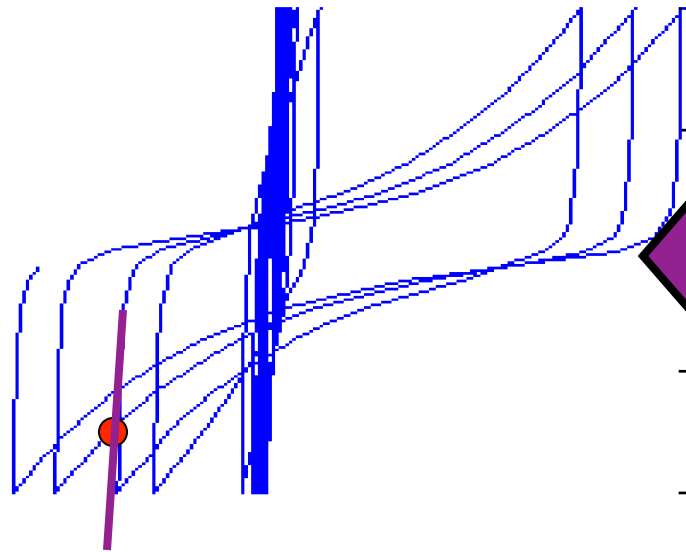


Stress path



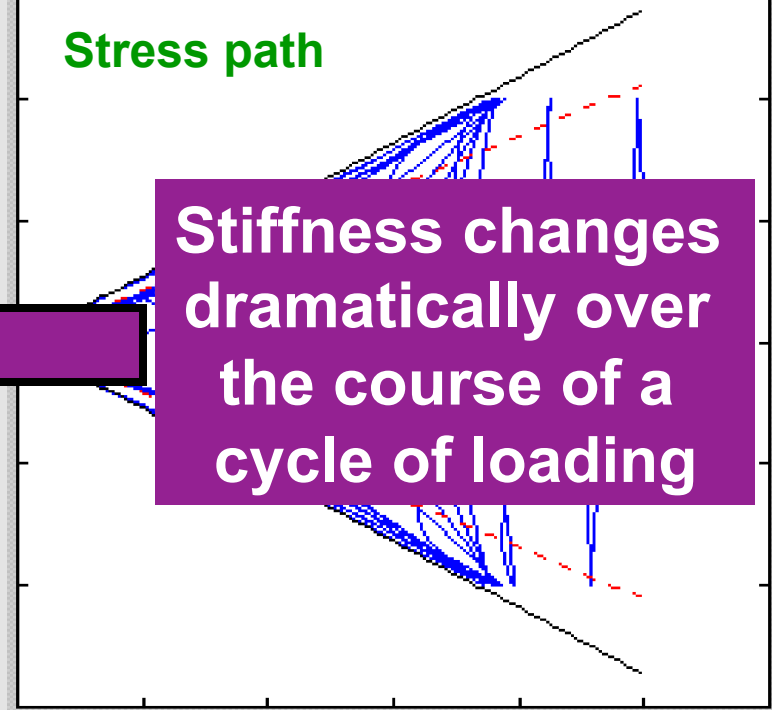
# Effects of Liquefaction

Stress-strain



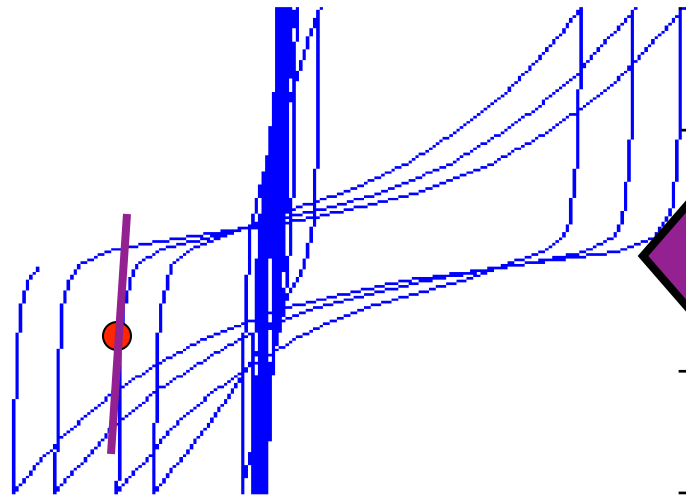
Stress path

Stiffness changes dramatically over the course of a cycle of loading

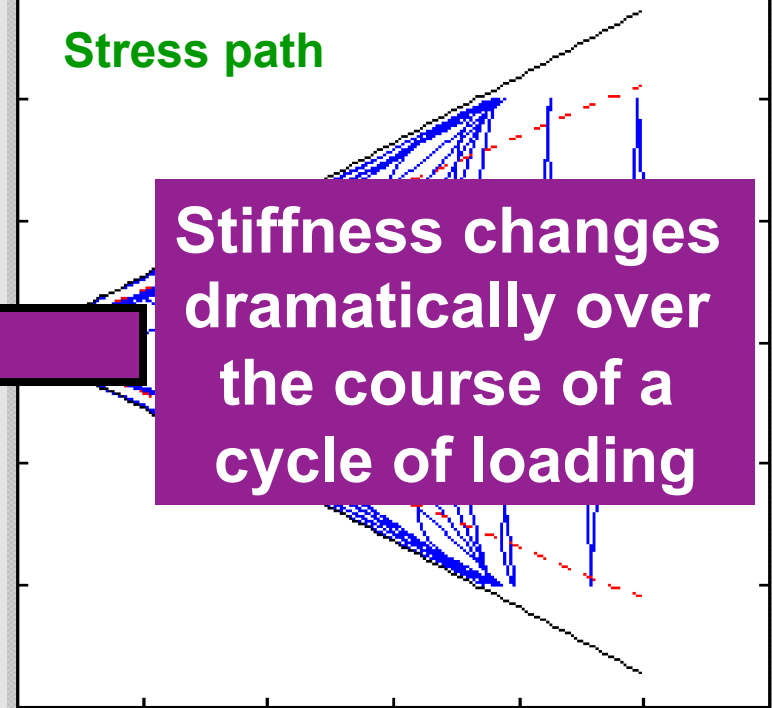


# Effects of Liquefaction

Stress-strain



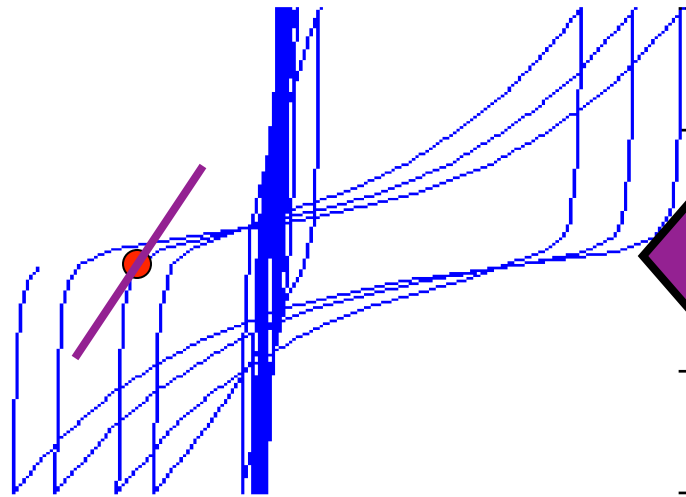
Stress path



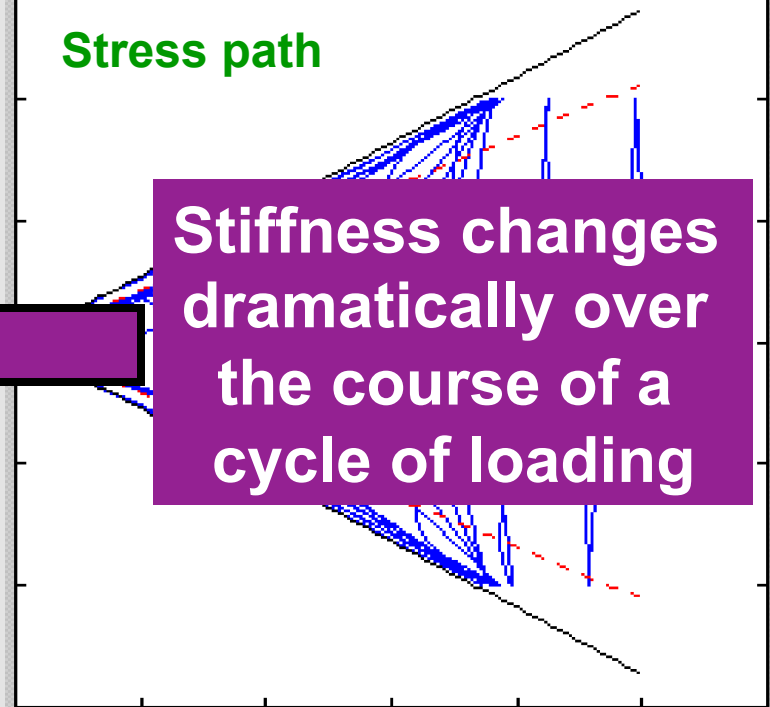
Stiffness changes dramatically over the course of a cycle of loading

# Effects of Liquefaction

Stress-strain



Stress path

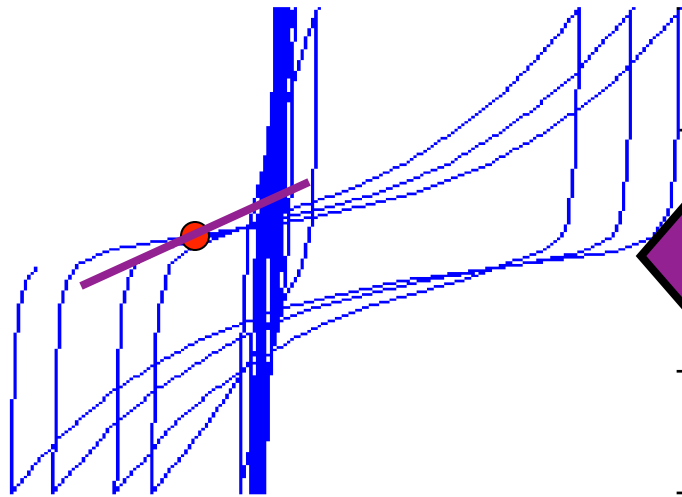


Stiffness changes dramatically over the course of a cycle of loading

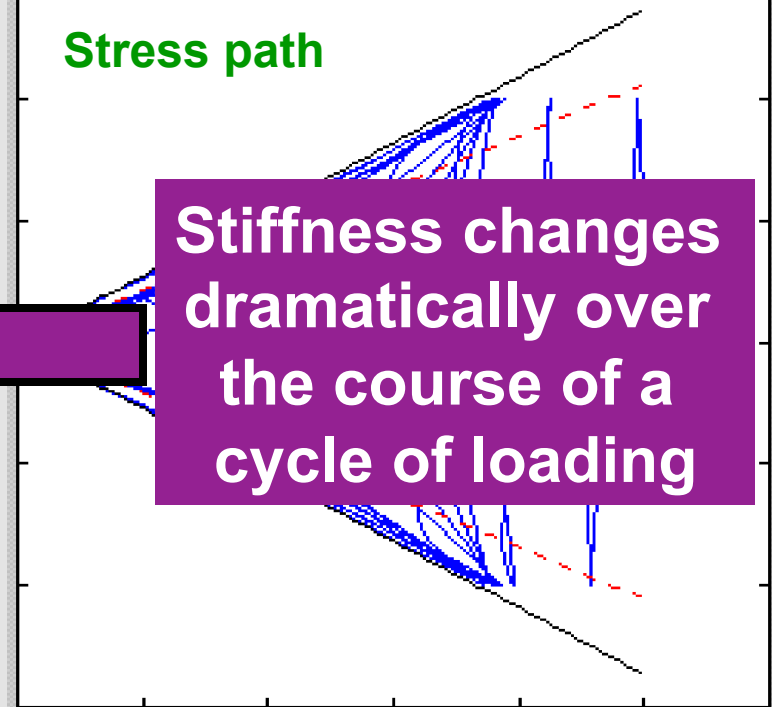


# Effects of Liquefaction

Stress-strain

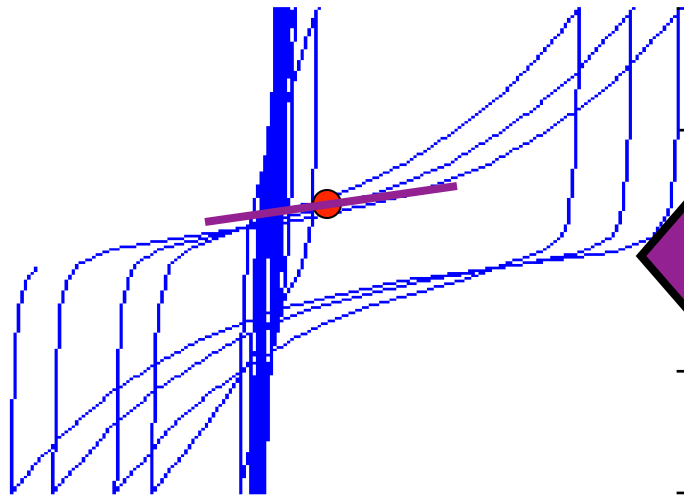


Stress path

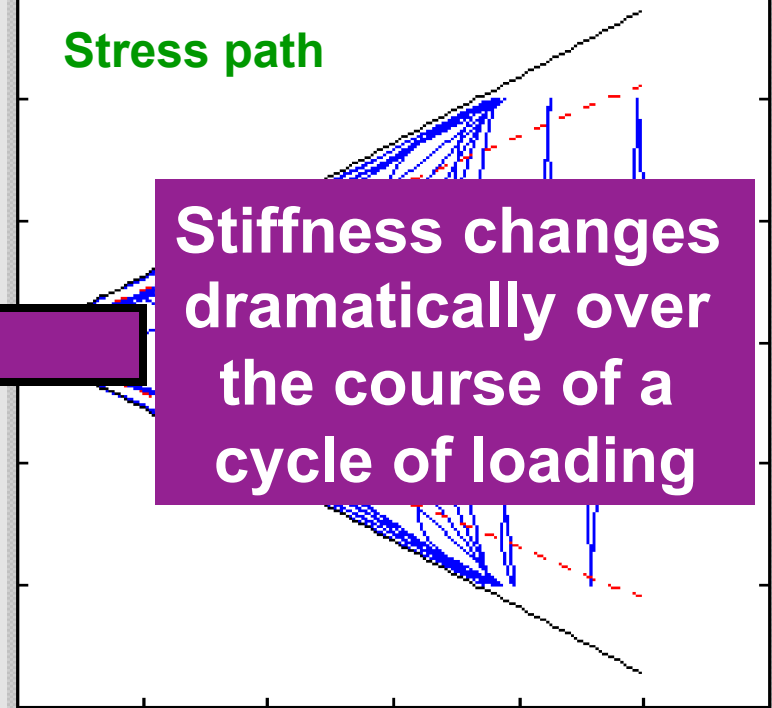


# Effects of Liquefaction

Stress-strain



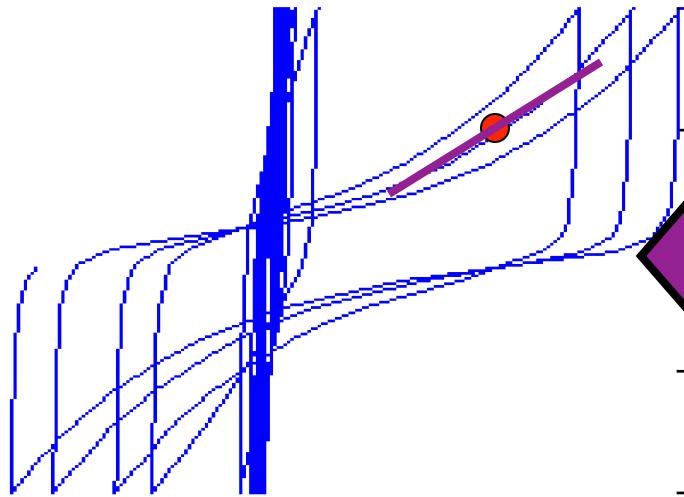
Stress path



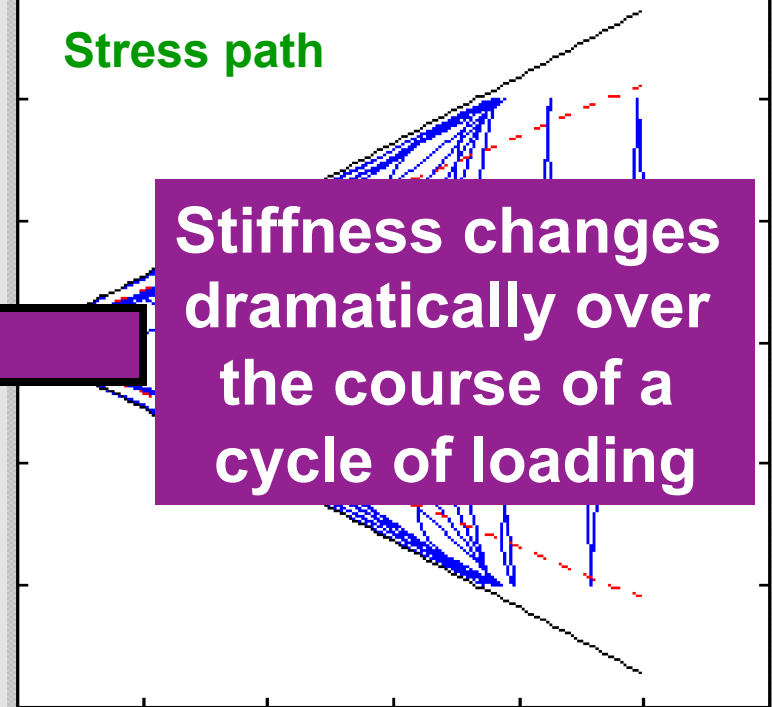
Stiffness changes dramatically over the course of a cycle of loading

# Effects of Liquefaction

Stress-strain

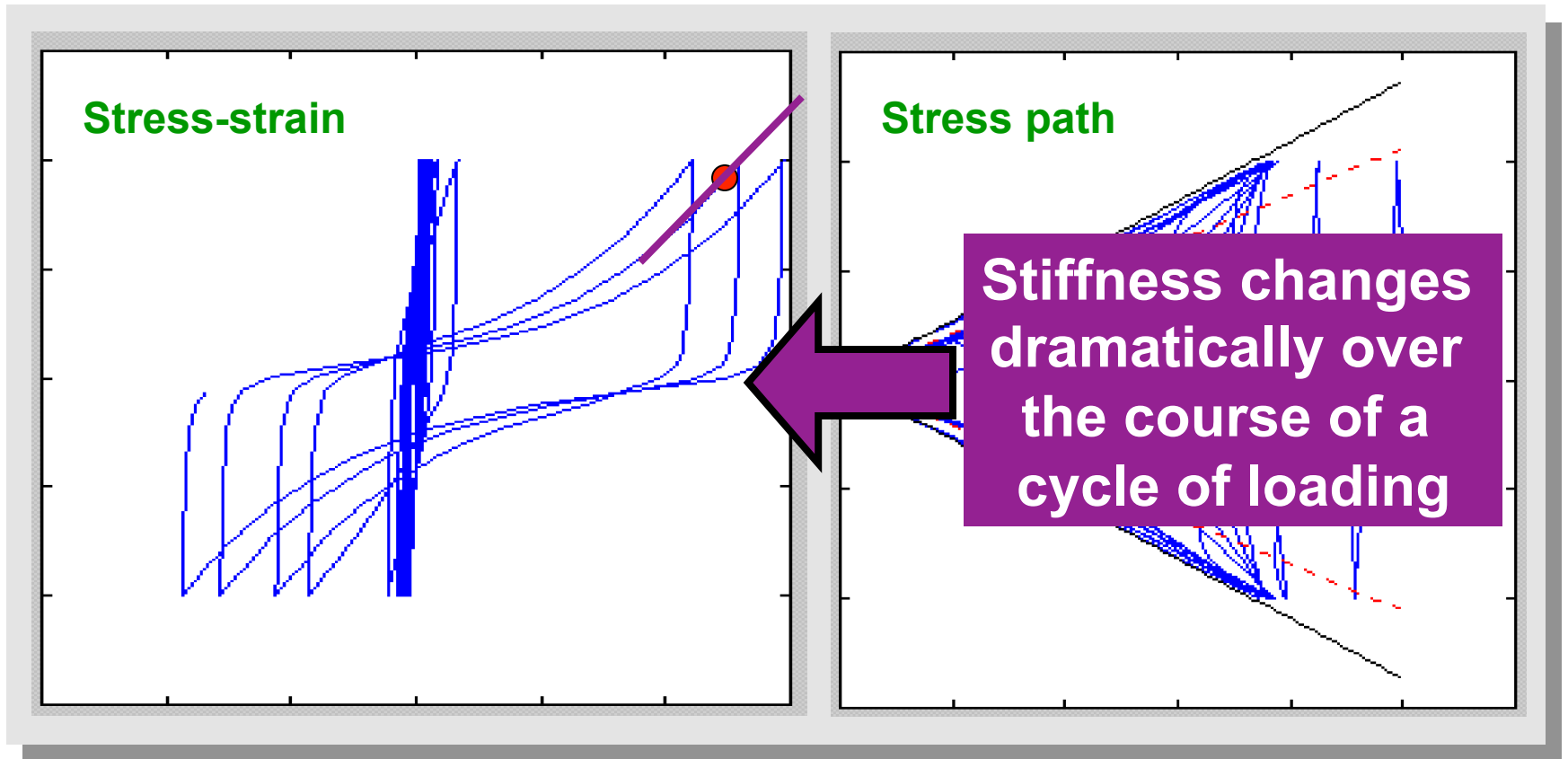


Stress path



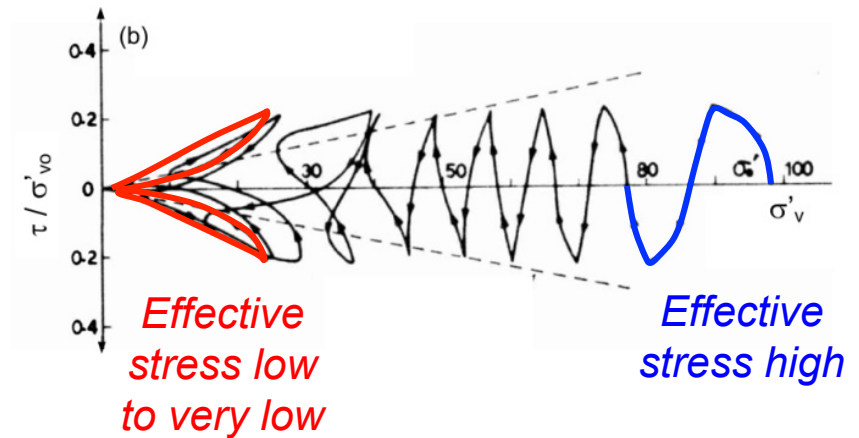
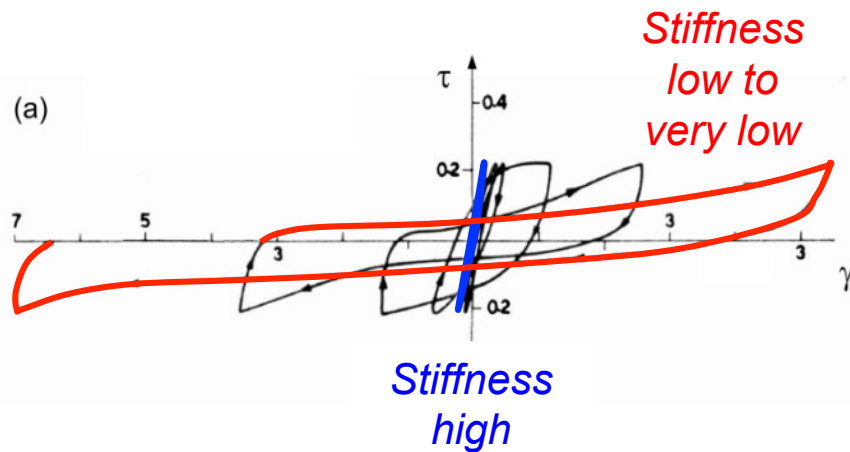
Stiffness changes dramatically over the course of a cycle of loading

# Effects of Liquefaction



# Effects of Liquefaction

Ishihara (1985) – Cyclic simple shear test



*Phase transformation behavior well established by laboratory tests*

# Effects of Liquefaction

## Site Response

- Stiffness generally decreases
- Longer period motion
- Lower acceleration amplitudes
- Higher displacement amplitudes

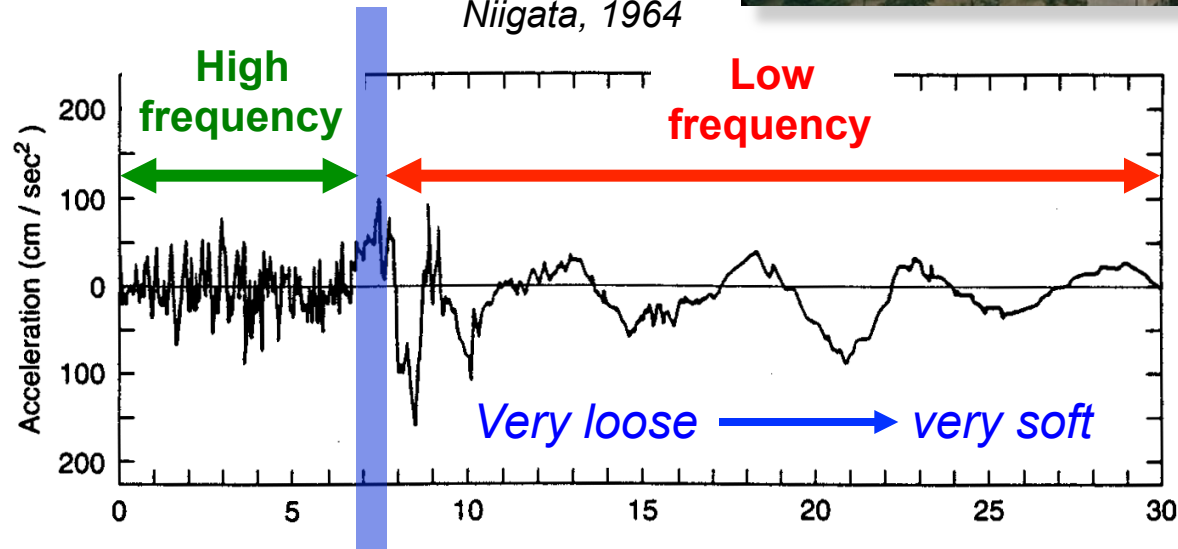
# Effects of Liquefaction

## Site Response

- Stiffness generally decreases
- Longer period motion
- Lower acceleration amplitudes
- Higher displacement amplitudes



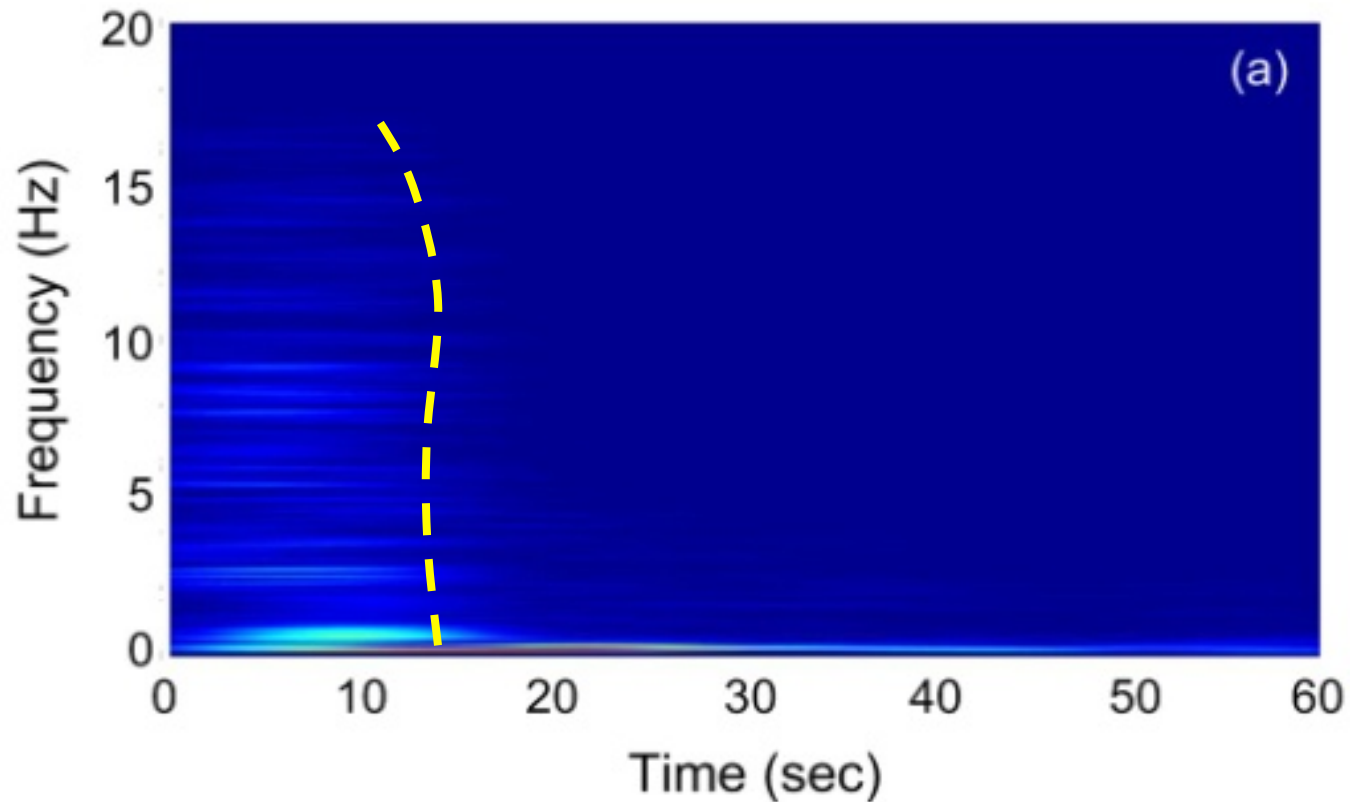
*Kawagishi-cho apartment buildings  
Niigata, 1964*



# Effects of Liquefaction

Time-frequency response

*Short-time Fourier Transform*

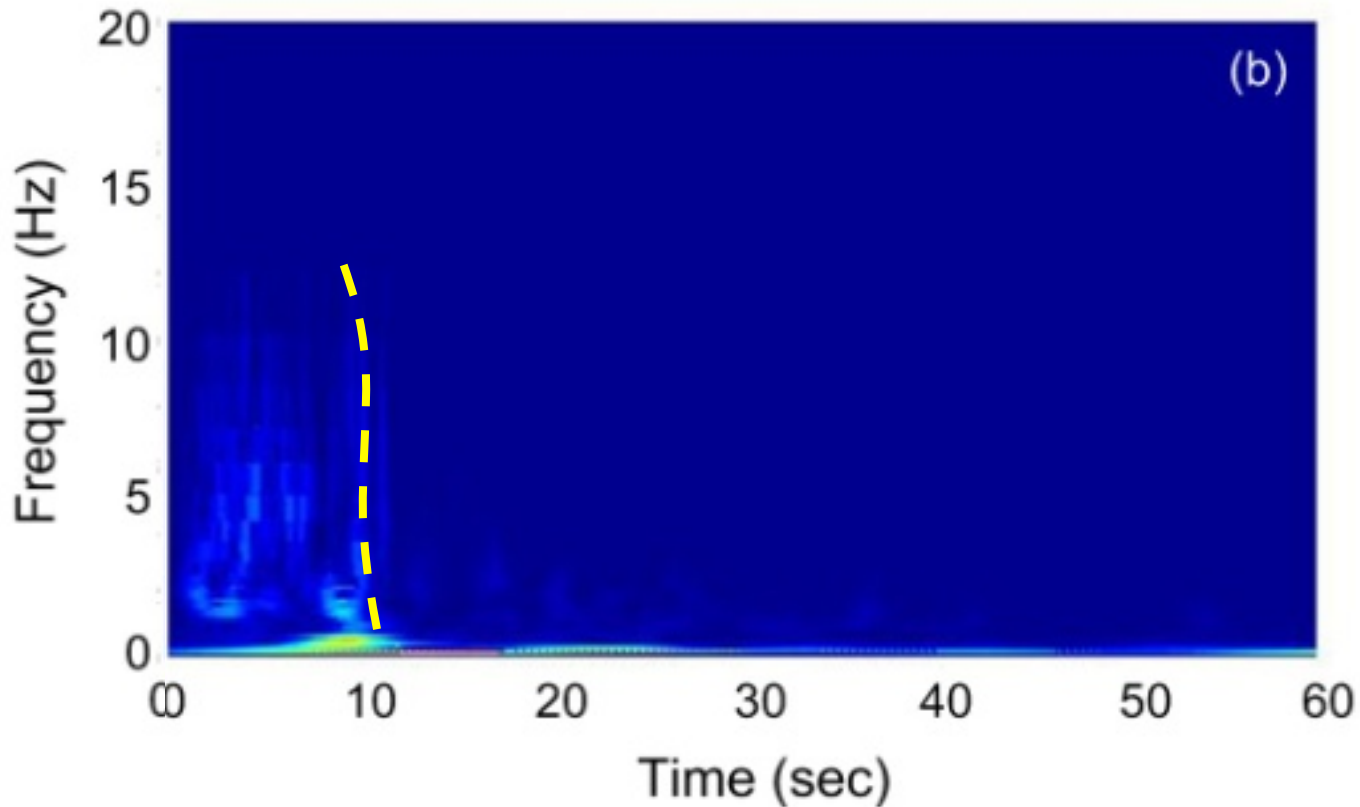




# Effects of Liquefaction

Time-frequency response

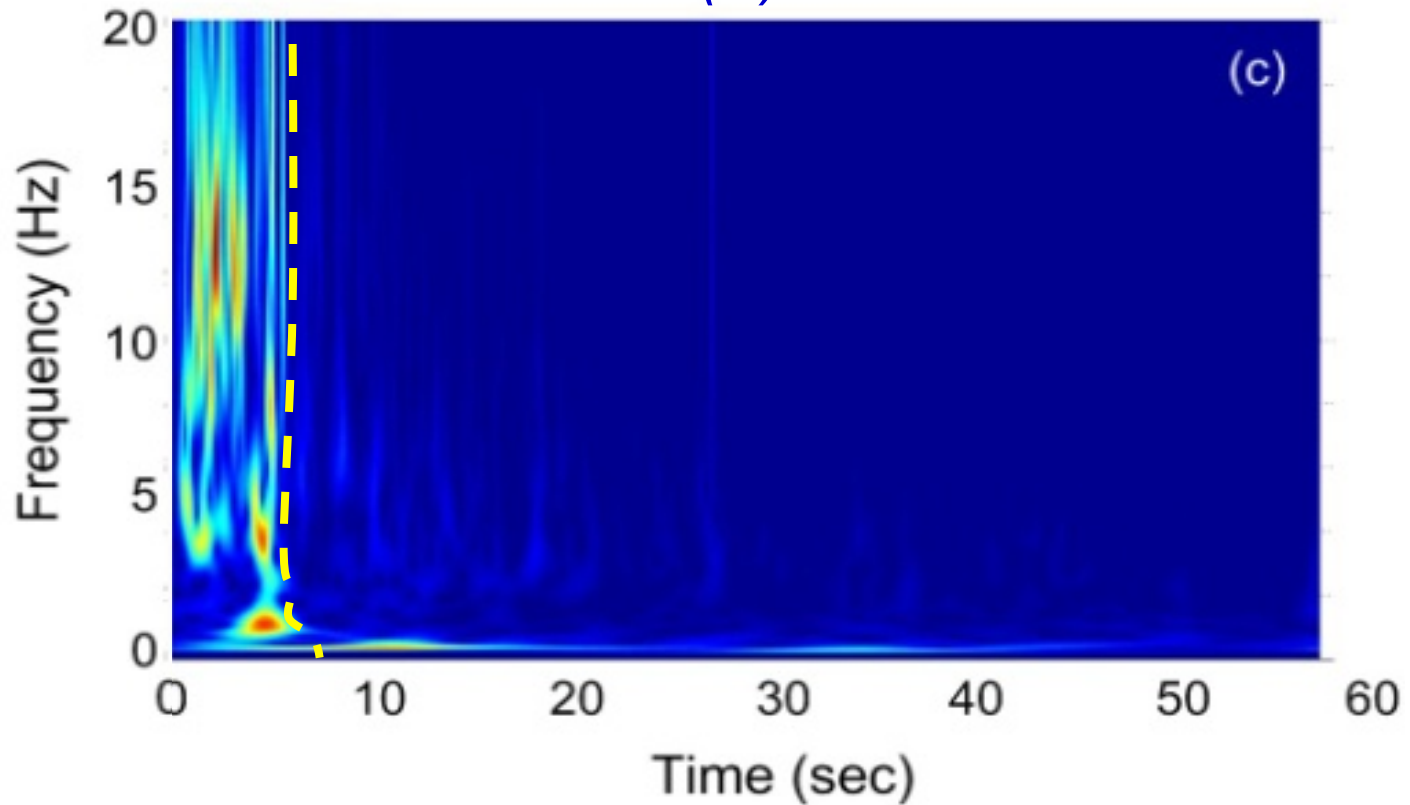
*Wavelet Transform*



# Effects of Liquefaction

Time-frequency response

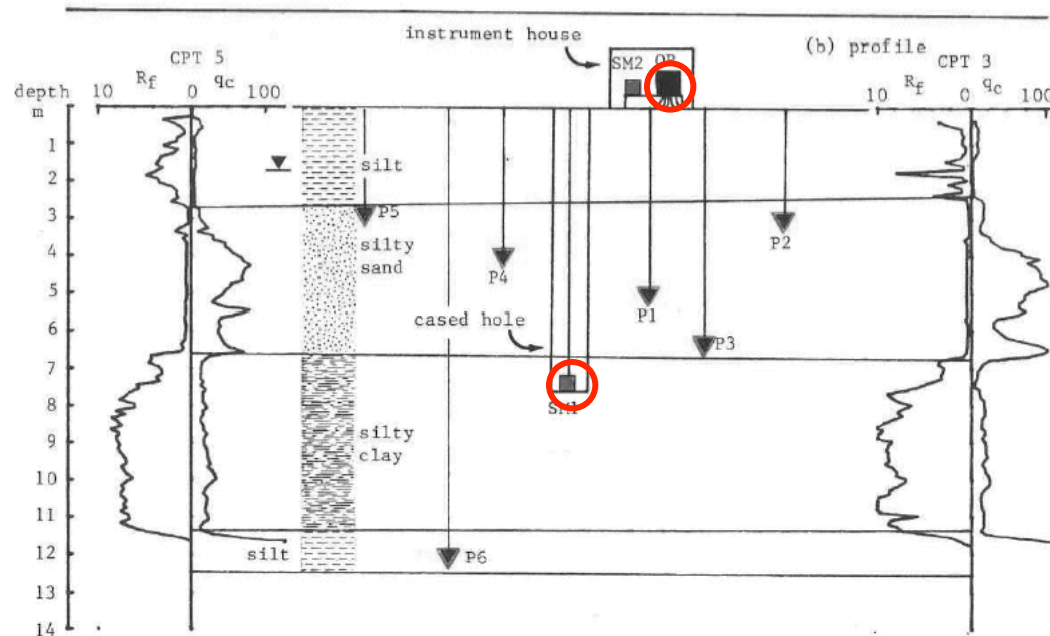
*Stockwell (S) Transform*



# Site Response

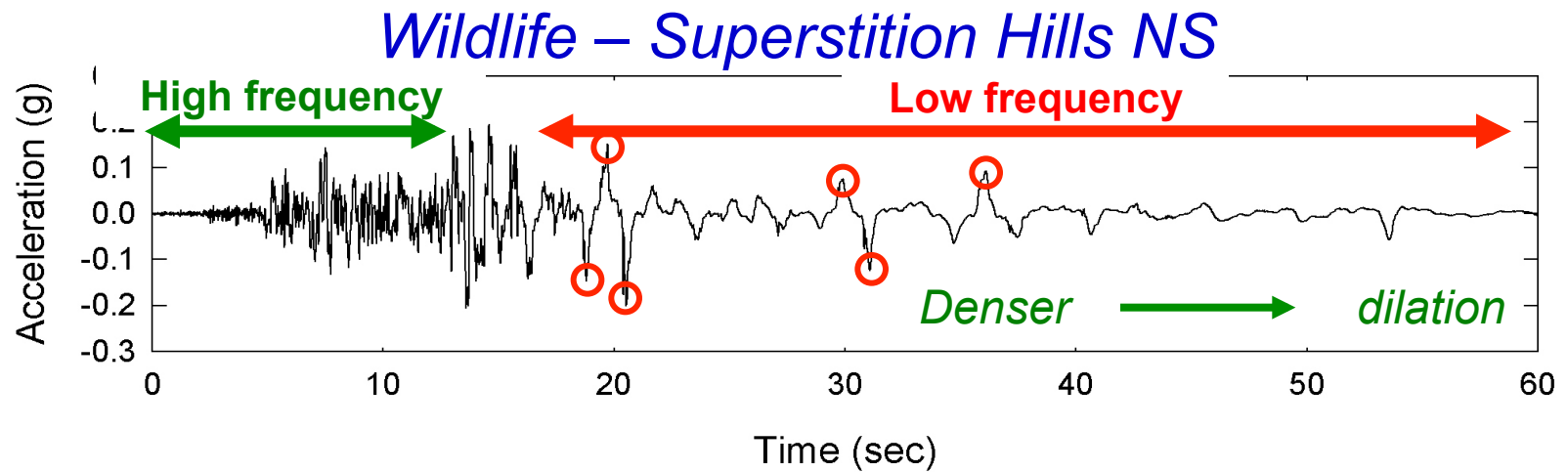
## Wildlife Array

- Located west side of Alamo River, Imperial county, CA
- Instrumented in 1982 by the USGS
- Non-liquefaction event – 1987 Elmore Ranch (M = 6.2)
- Liquefaction event – 1987 Superstition Hills (M = 6.6)



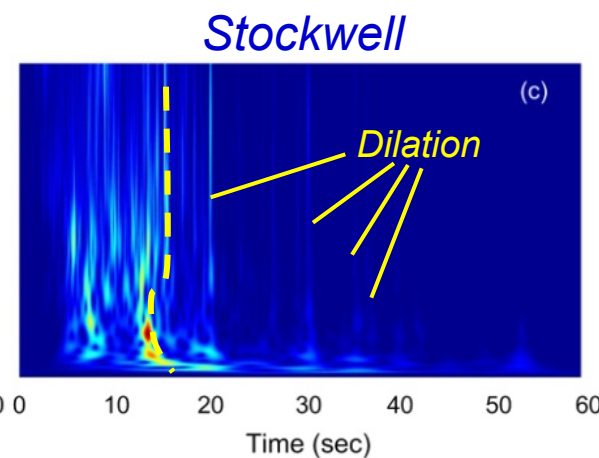
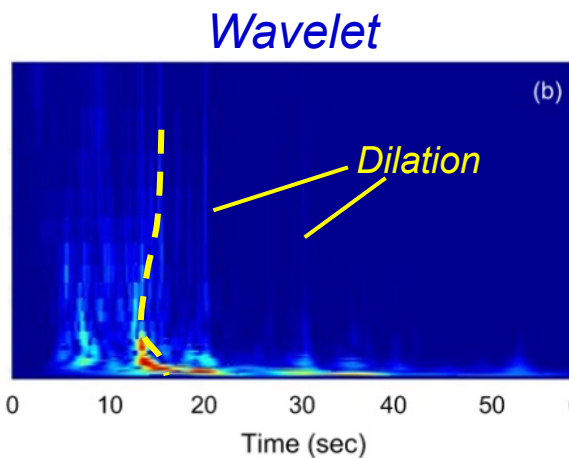
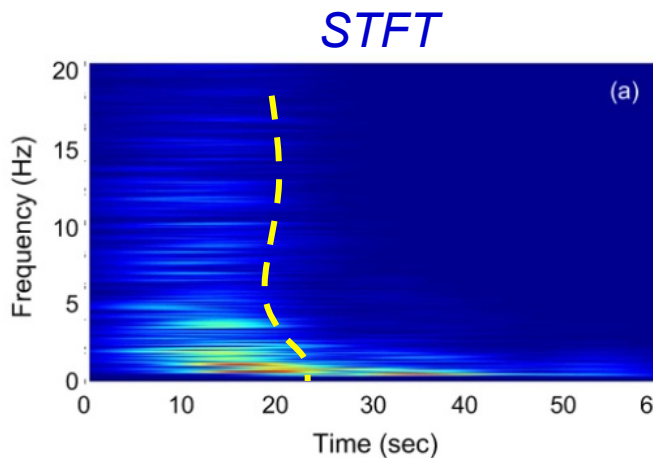
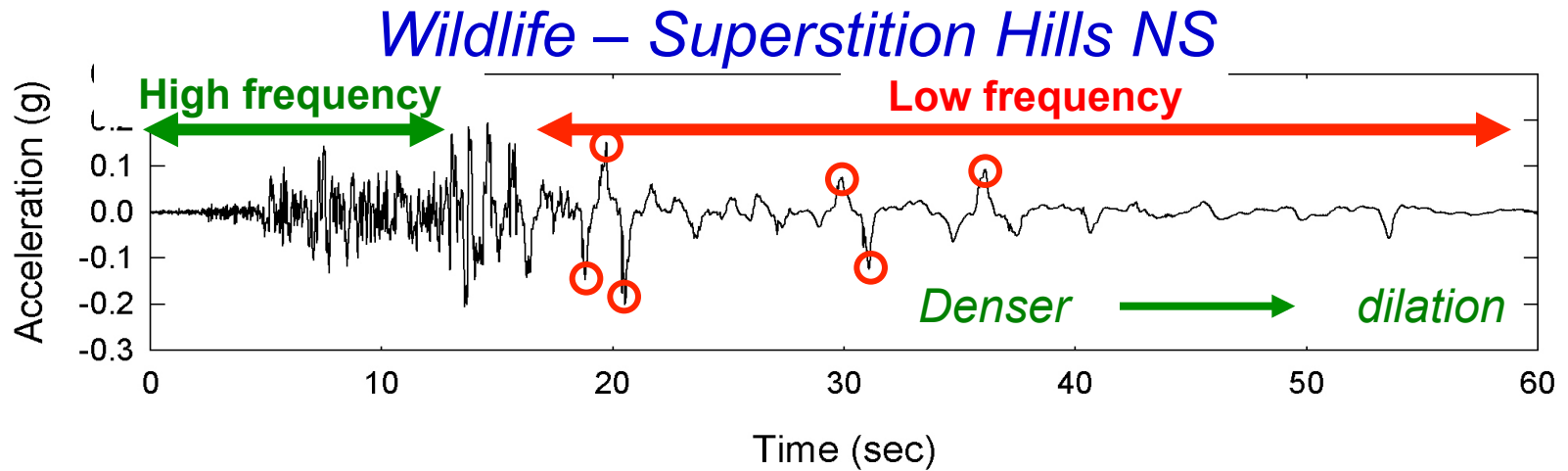
# Effects of Liquefaction

Time-frequency response



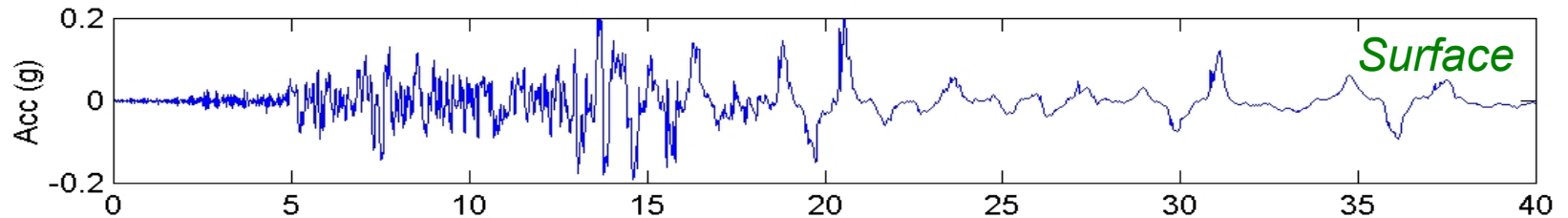
# Effects of Liquefaction

Time-frequency response

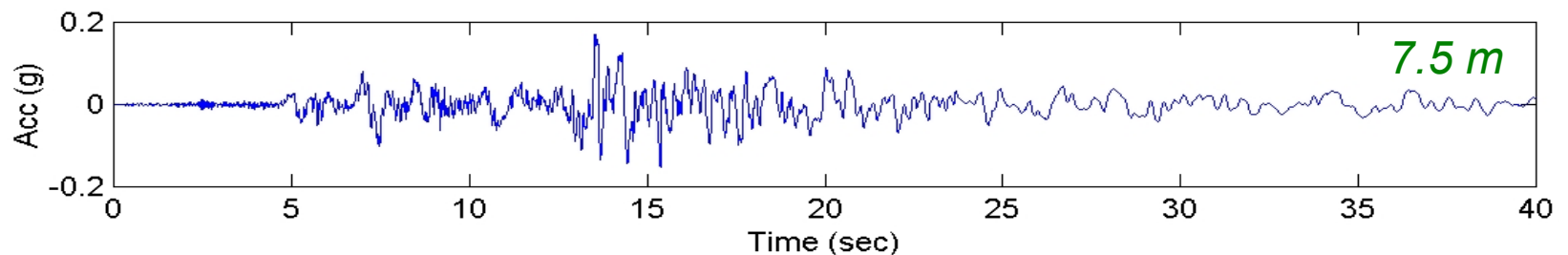


# Effects of Liquefaction

## Time-frequency response

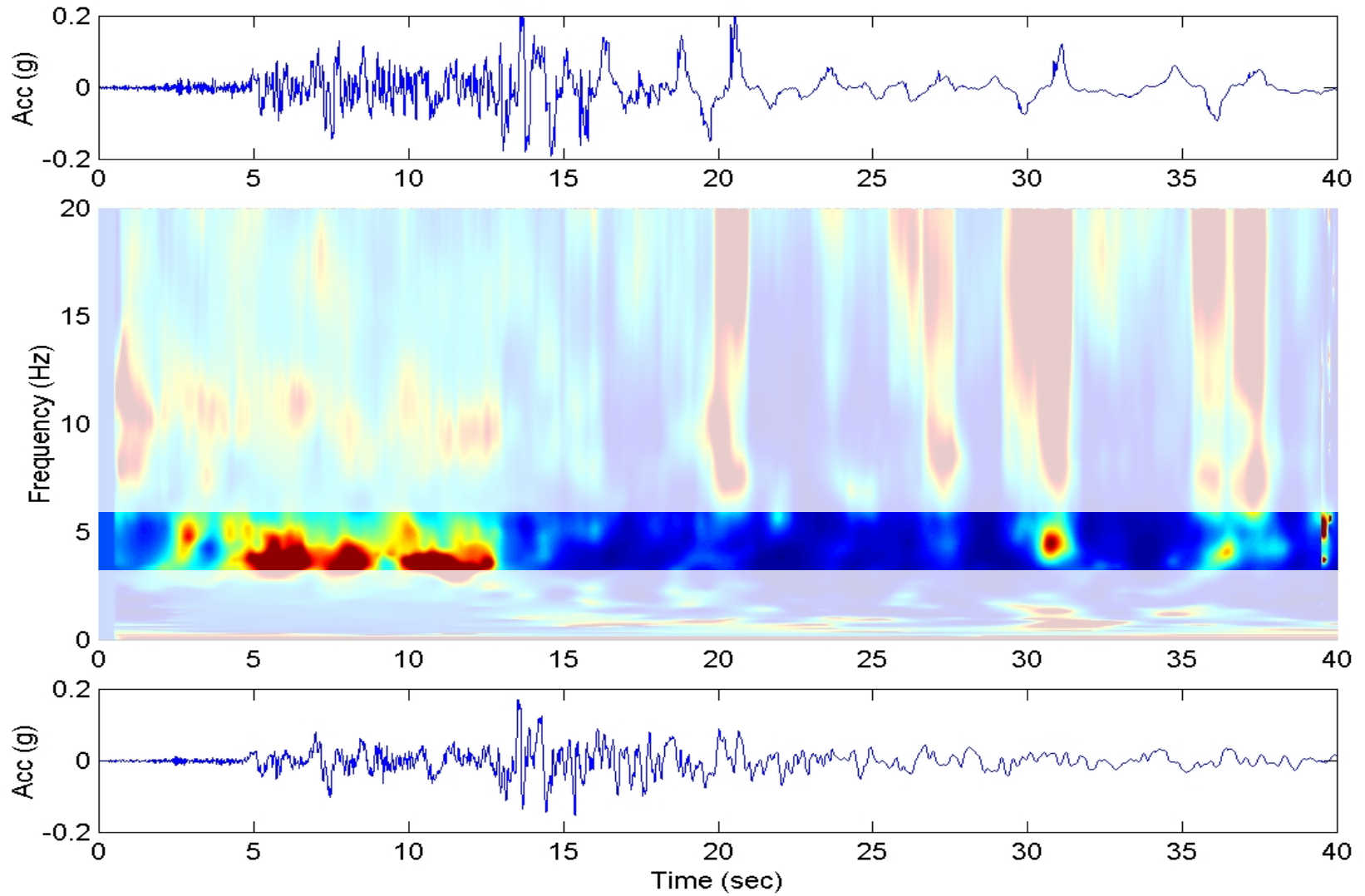


*Frequency content of surface motion is influenced by frequency content of underlying motion*



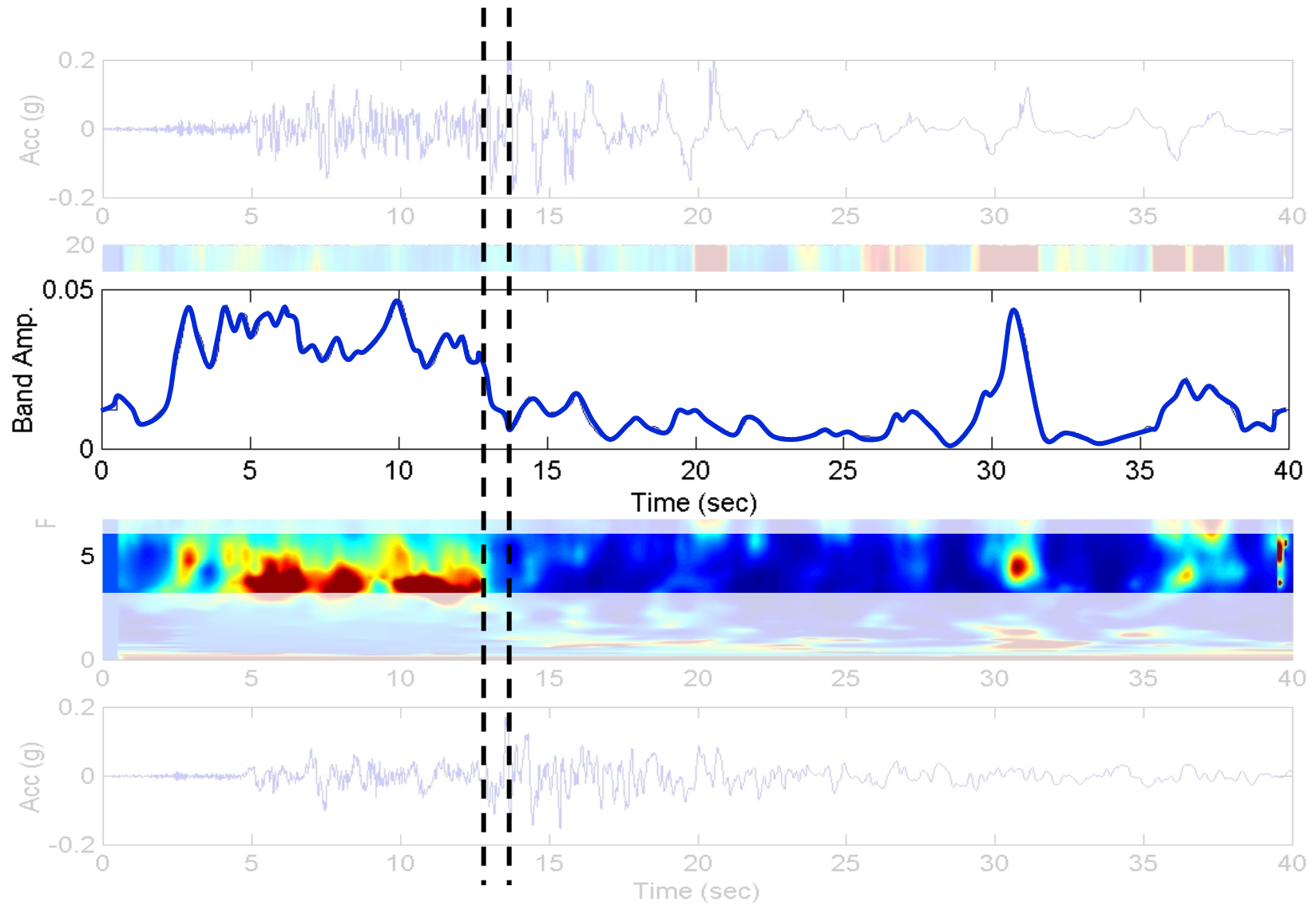
# Effects of Liquefaction

## Time-frequency response



# Effects of Liquefaction

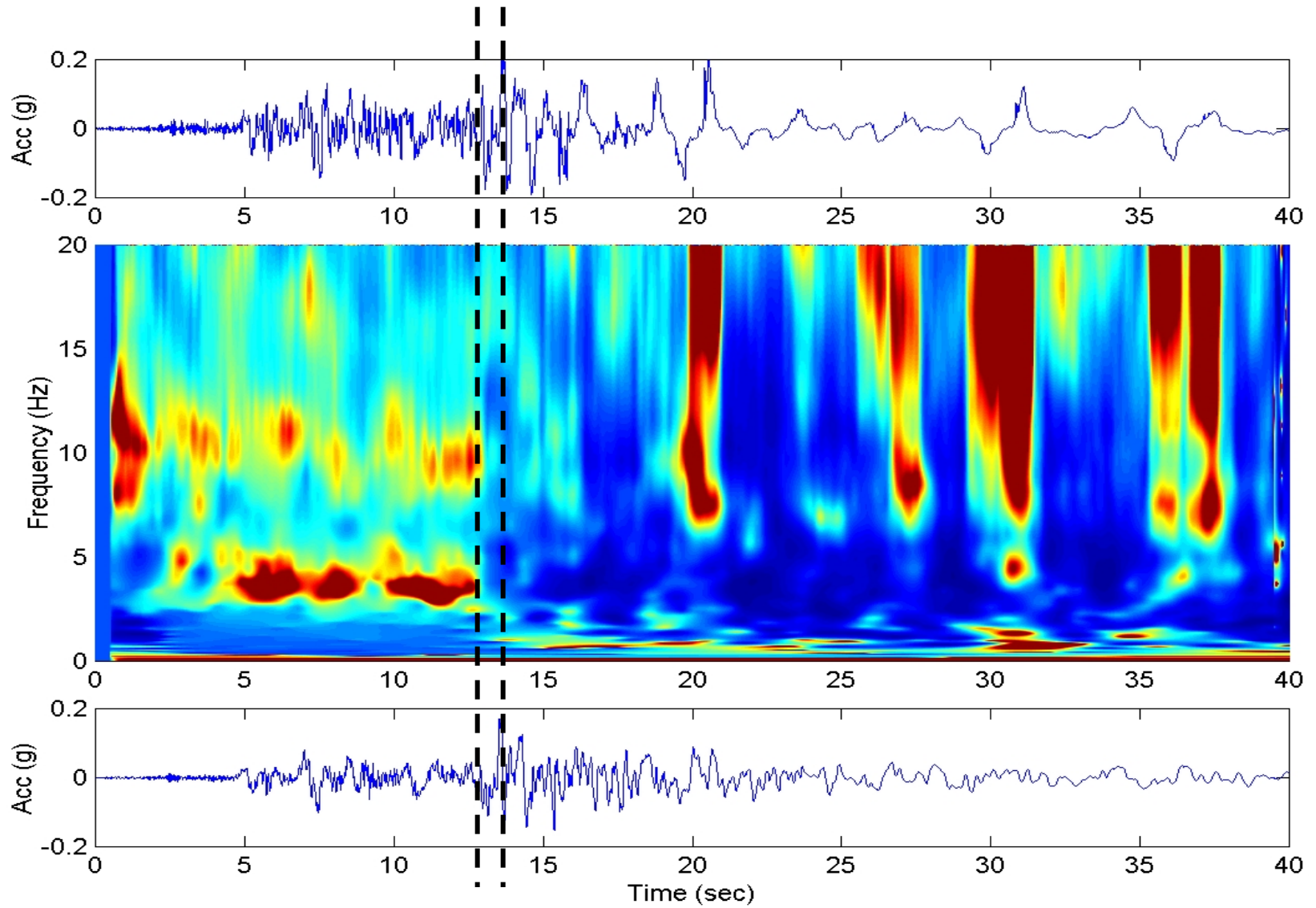
## Time-frequency response





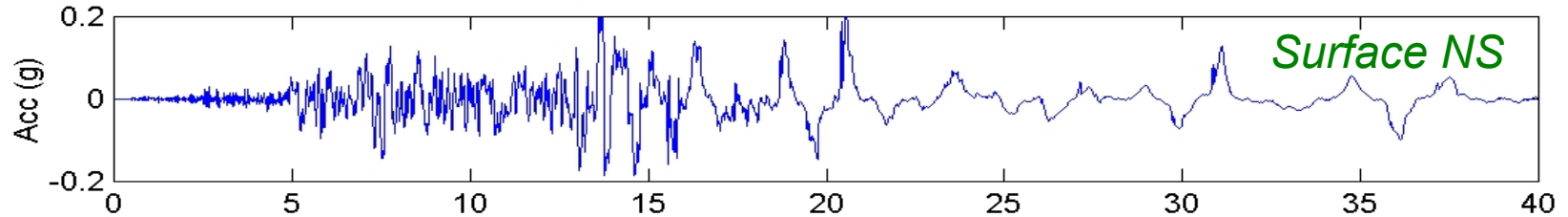
# Effects of Liquefaction

## Time-frequency response



# Effects of Liquefaction

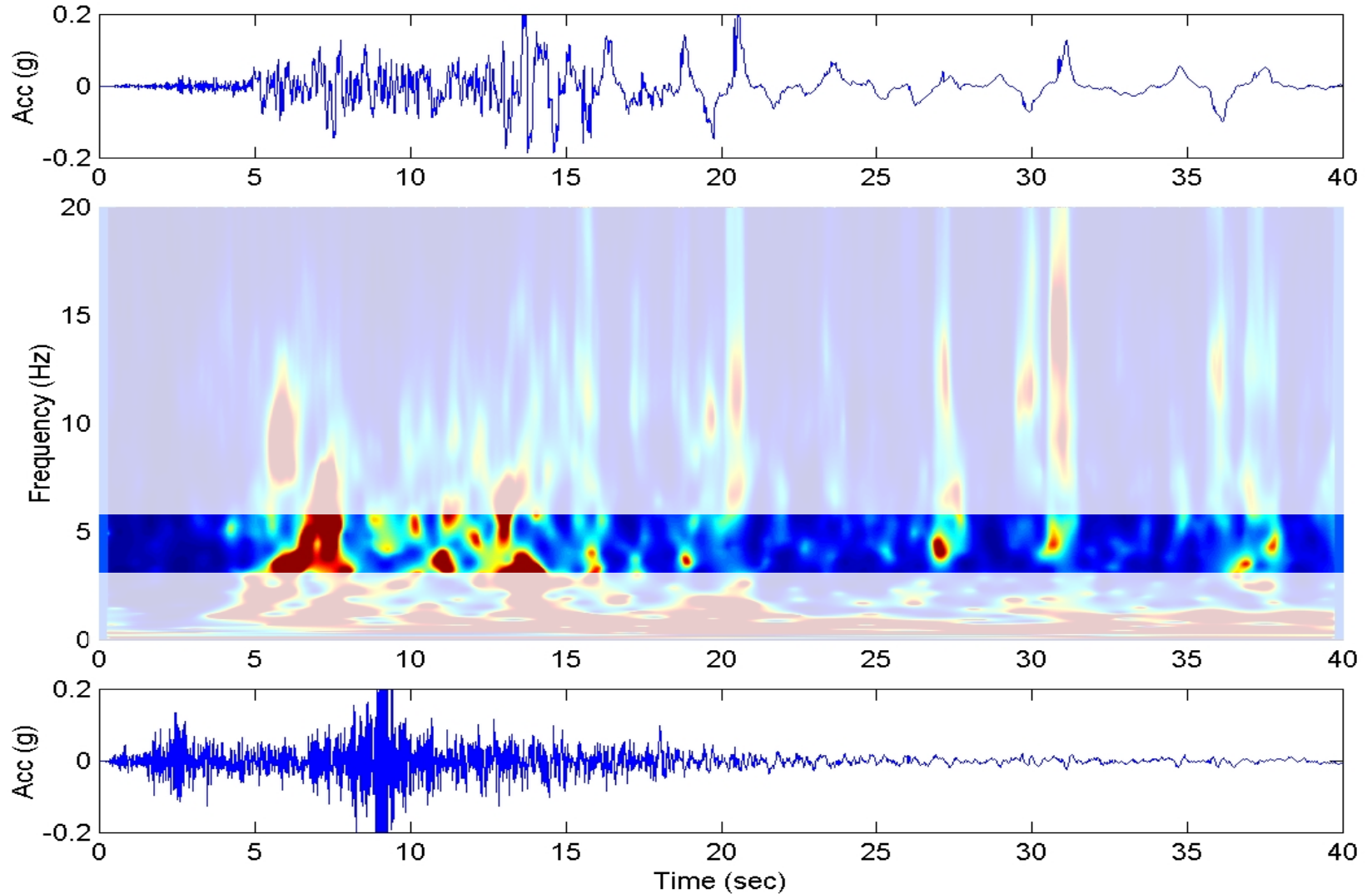
## Time-frequency response



*What if we don't have a useful downhole record?*

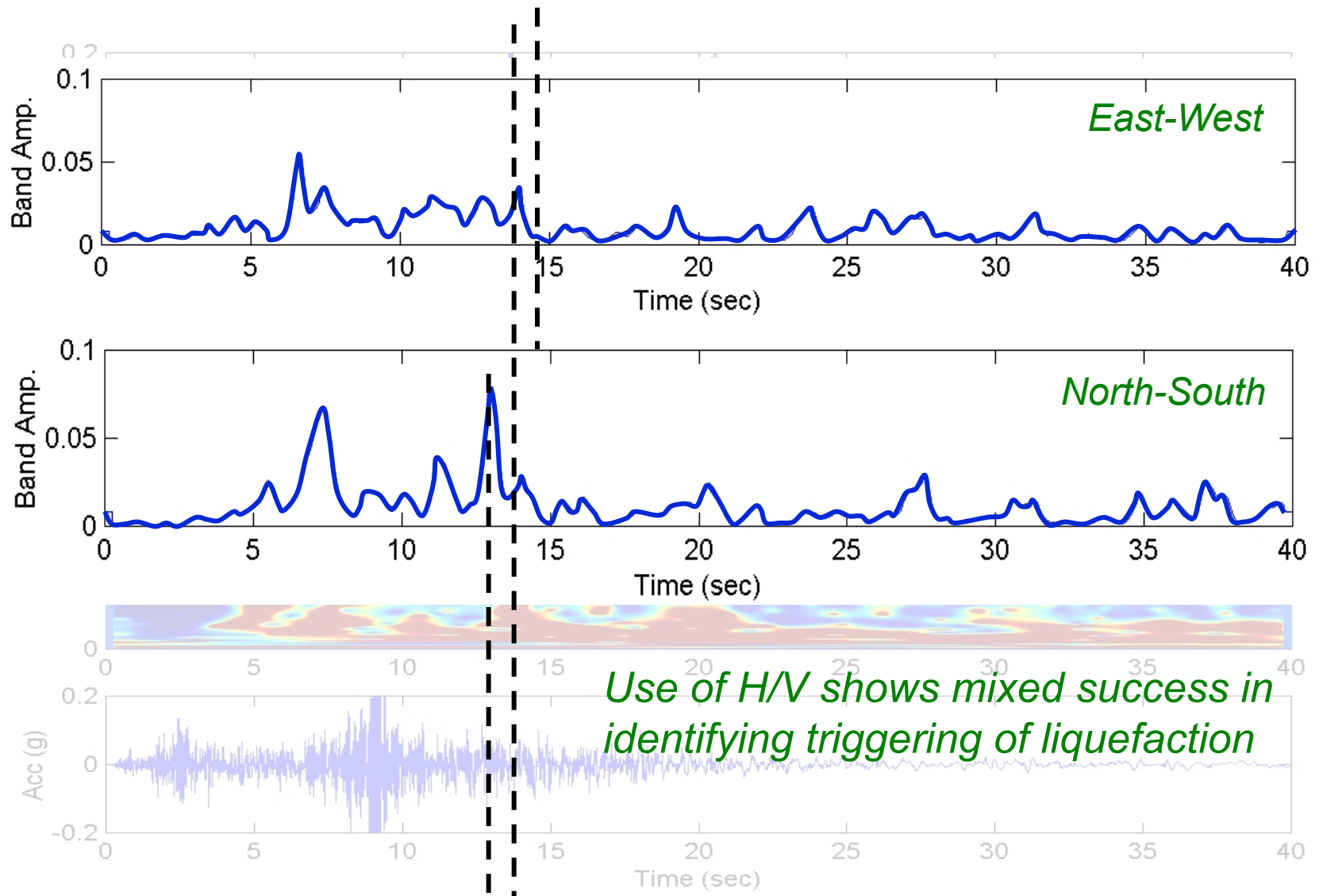
# Effects of Liquefaction

## Time-frequency response



# Effects of Liquefaction

## Time-frequency response



# Effects of Liquefaction

Can we predict this type of behavior?

Nonlinear, effective stress-based analysis

Reasonable constitutive model

Must allow pore pressure generation

Should include phase transformation behavior

Must be calibratable

# Nonlinear site response models

DMOD2000 ([www.geomotions.com](http://www.geomotions.com))

- Lumped mass MDOF system with Rayleigh damping
- Hyperbolic soil model with Masing rules
- Dobry-Vucetic strain-based pore pressure model (no PT behavior)
- Pore pressure models provided for Wildlife sands

WAVE (Horne, 1995)

- Approximately follows Seed-Idriss upper bound modulus reduction and lower bound damping curves for liquefiable layers
- Accounts for phase transformation behavior
- Calibrated to match empirical pore pressure generation and strain behavior –  $(N_1)_{60-cs}$

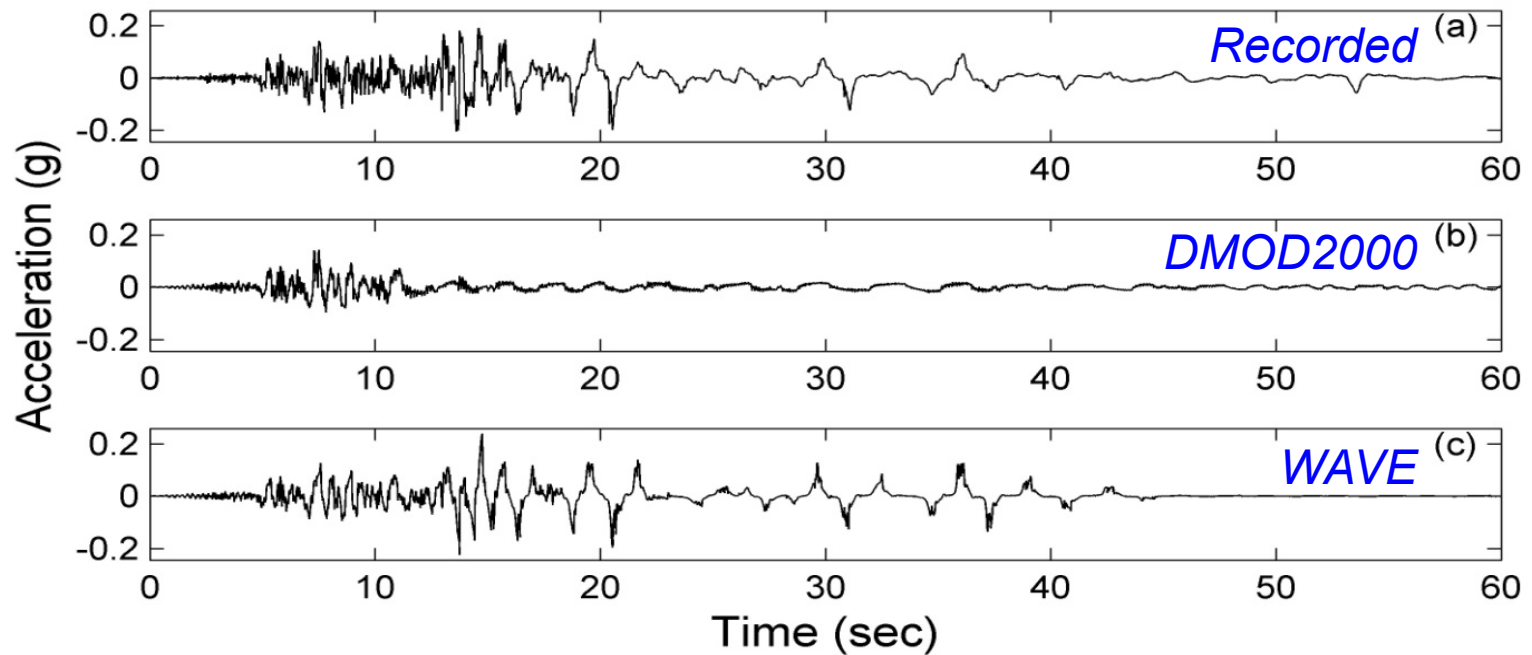
# Nonlinear site response modeling challenges

- Site characterization – different models require different parameters
- Dimensionality – 1D misses surface wave, basin effects
- Directionality – nearly all codes deal with one horizontal component
- Repeatability – models should work for weak and strong shaking
- Crust behavior – crust will distort, break ... not accounted for
- Soil-structure interaction – may affect recorded motions
- Sloping ground effects – asymmetric response

*Lots of possible ~~excuses~~ reasons for inexact predictions*

# Nonlinear site response

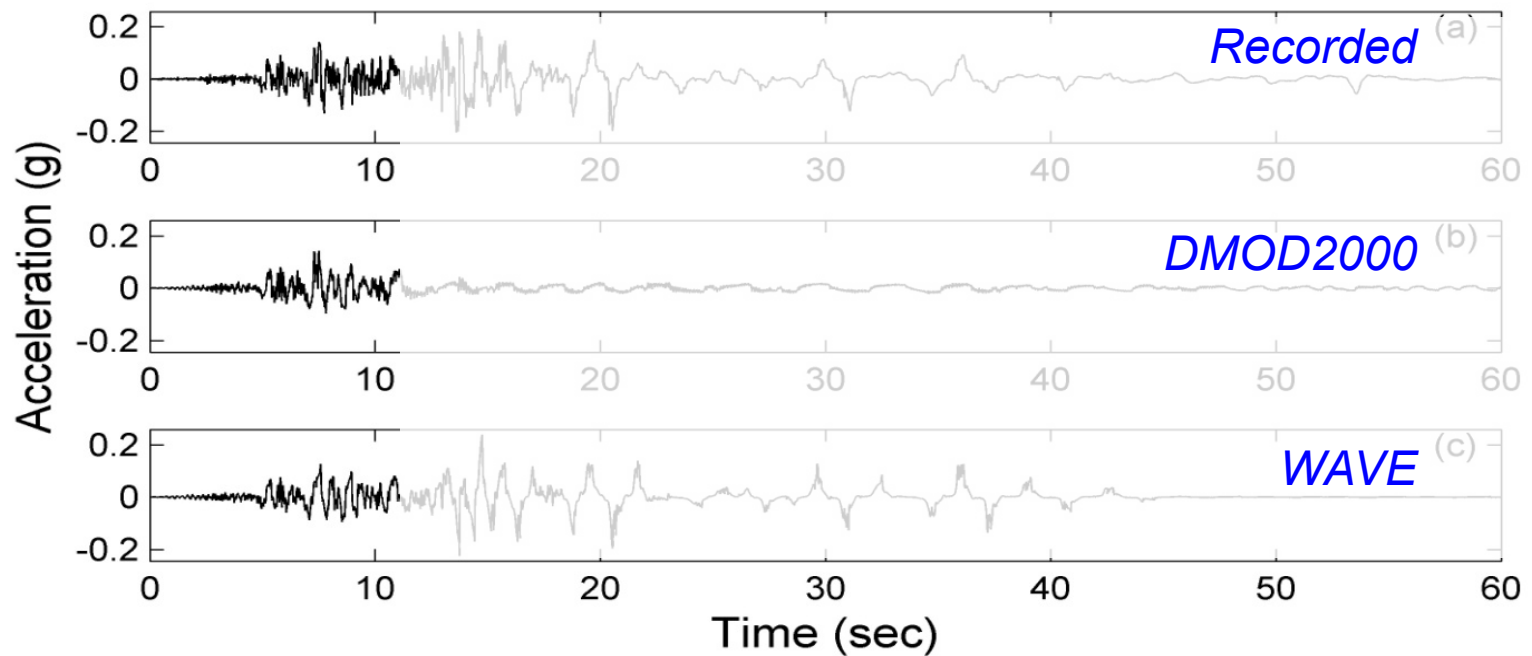
## Superstition Hills NS surface motion





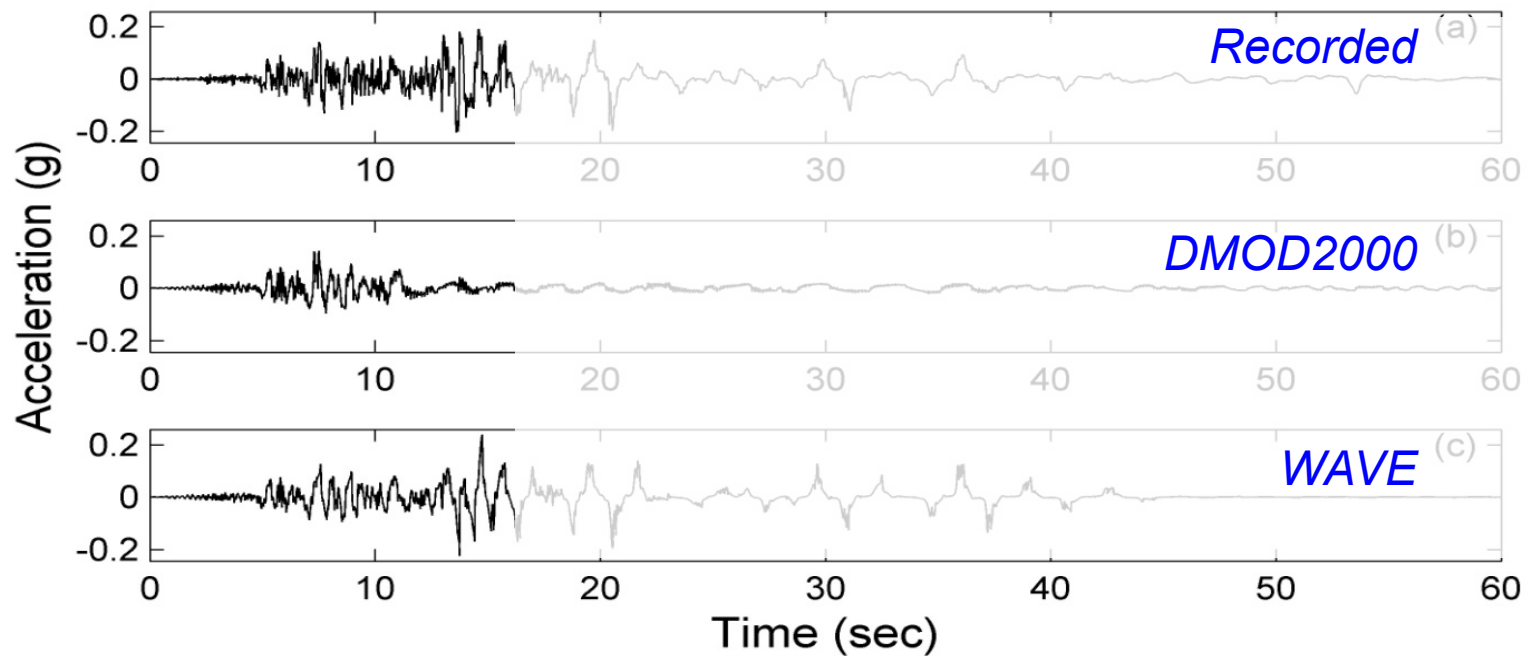
# Nonlinear site response

## Superstition Hills NS surface motion



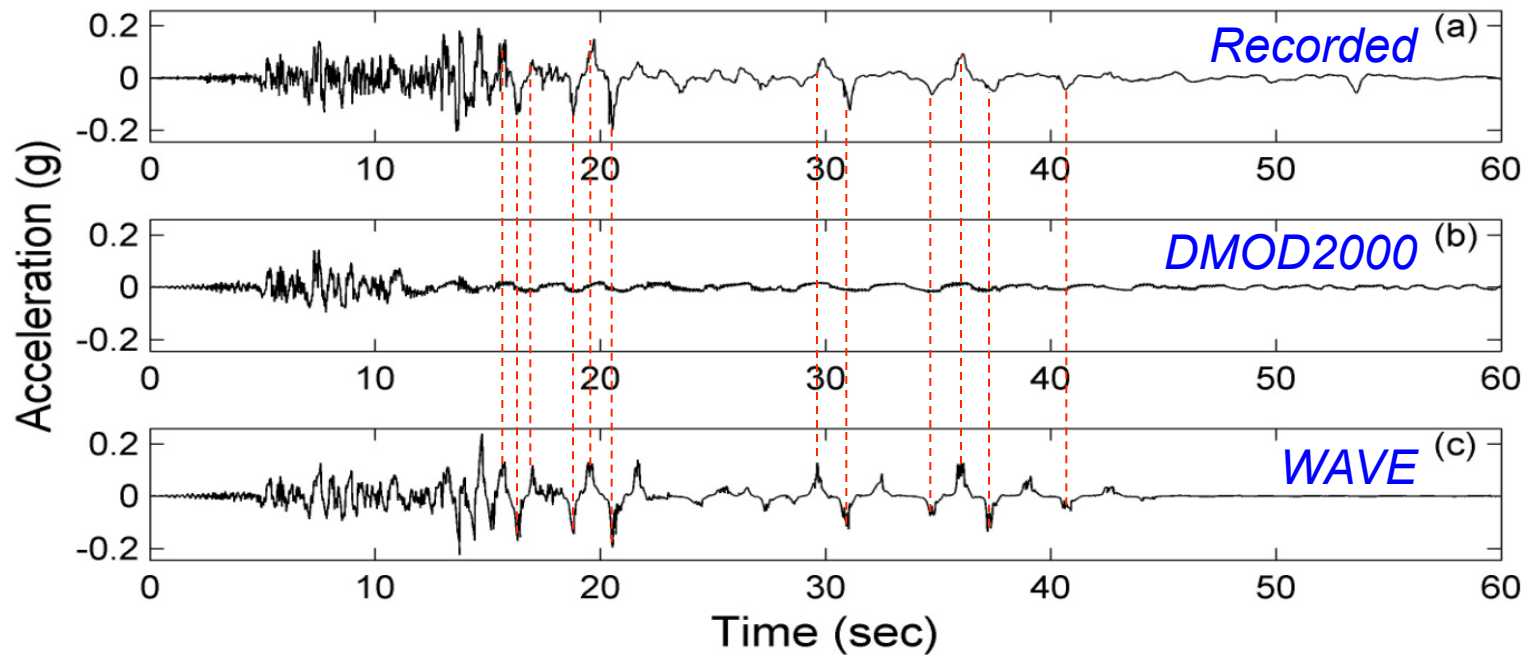
# Nonlinear site response

Superstition Hills NS surface motion



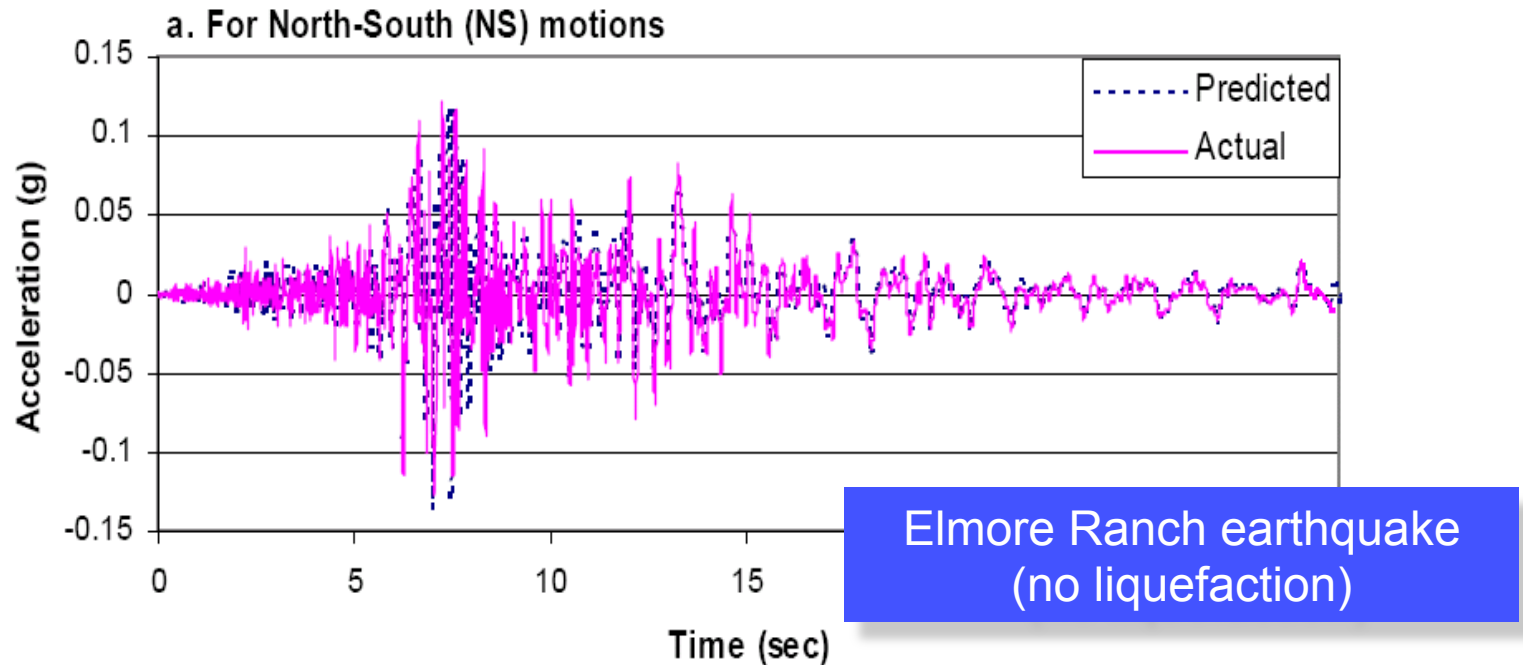
# Nonlinear site response

## Superstition Hills NS surface motion



# Effects of Liquefaction on Ground Surface Motions

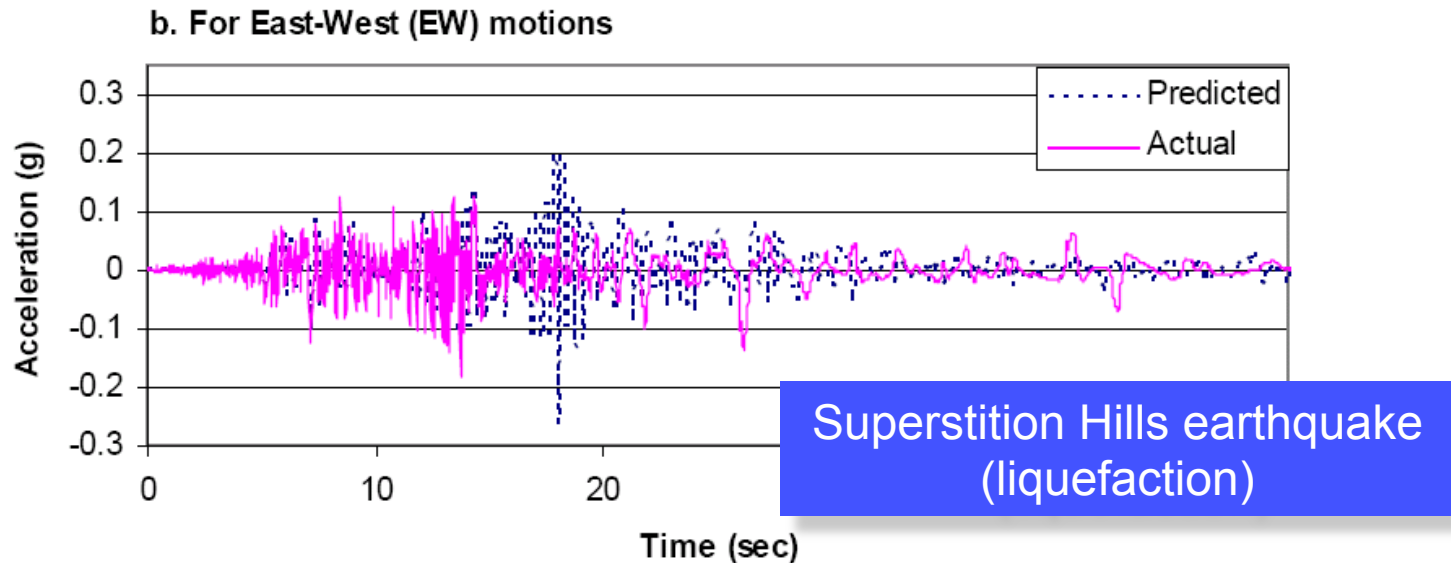
Youd and Carter (2005)



Validated equivalent linear model by comparing SHAKE time history to the actual recorded time history – good agreement

# Effects of Liquefaction on Ground Surface Motions

Youd and Carter (2005)

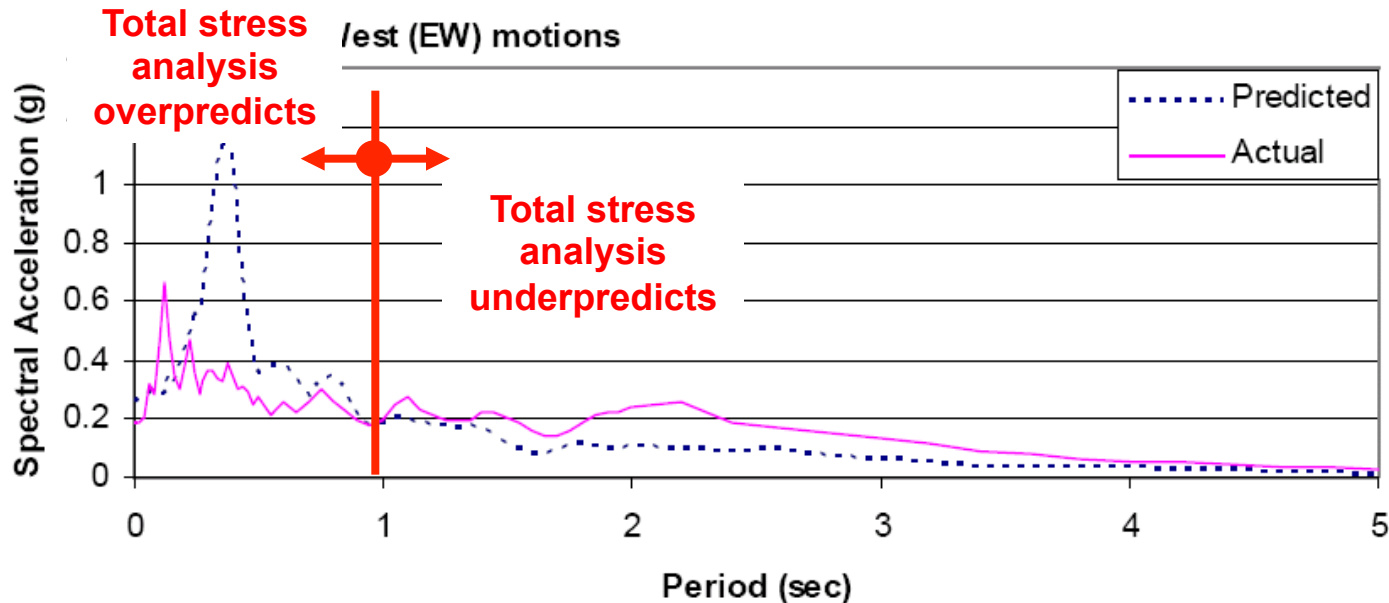


Compared equivalent linear model predictions to actual record – good agreement in first 13 sec, poor after.

Equivalent linear analyses maintained high frequency content after 13 sec due to constant stiffness. Stiffness of actual profile apparently reduced due to liquefaction.

# Effects of Liquefaction on Site Response

Youd and Carter (2005)



**Analysis of five case histories taken to show:**

- There is generally a reduction in short period spectral response (< 0.7-1.0 sec)
- There is generally an amplification of long period spectral response (> 0.7 - 1.0 sec)

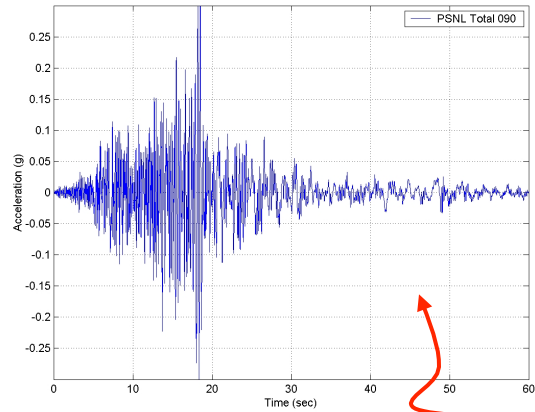
# Effects of Liquefaction on Site Response

More detailed investigation

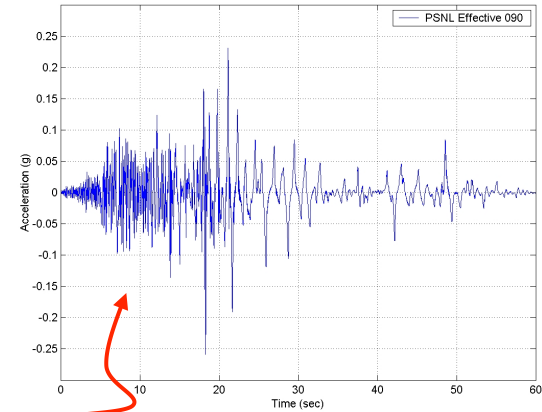
- Develop trial soil profiles
- Propagate ground motions through soil profiles to obtain surface motions
  - Once using total stress analysis, i.e. not allowing liquefaction, (no pore pressure generation)
  - Once using effective stress analysis allowing liquefaction, (with pore pressure generation)
- Compute ratios of response spectral accelerations at all periods

# Effects of Liquefaction on Site Response

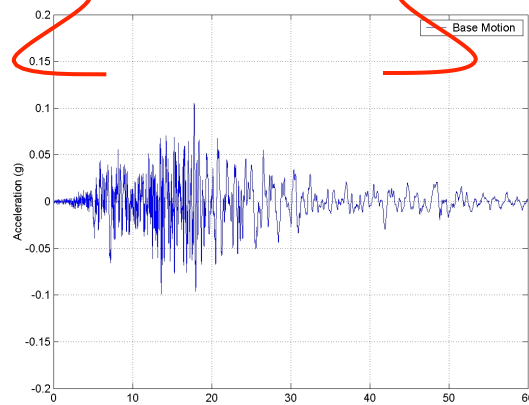
## Total Stress Case



## Effective Stress Case



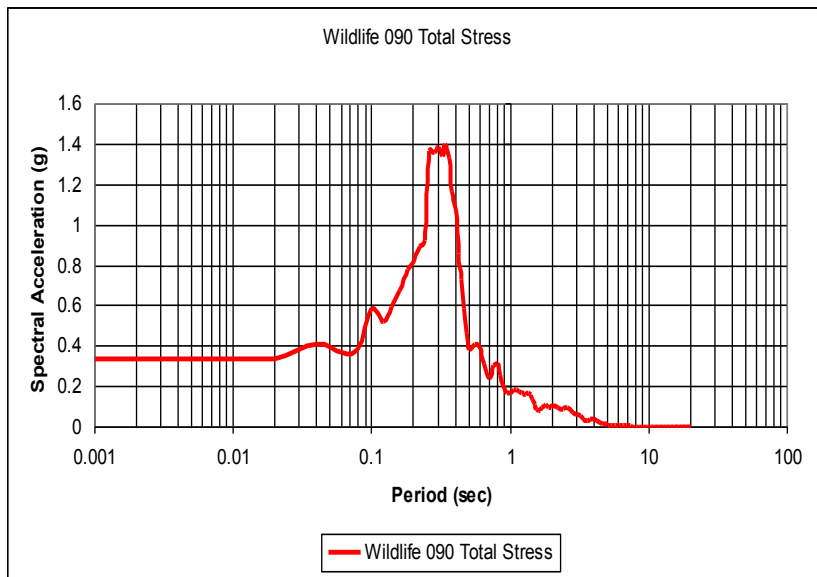
## Input Base Motion



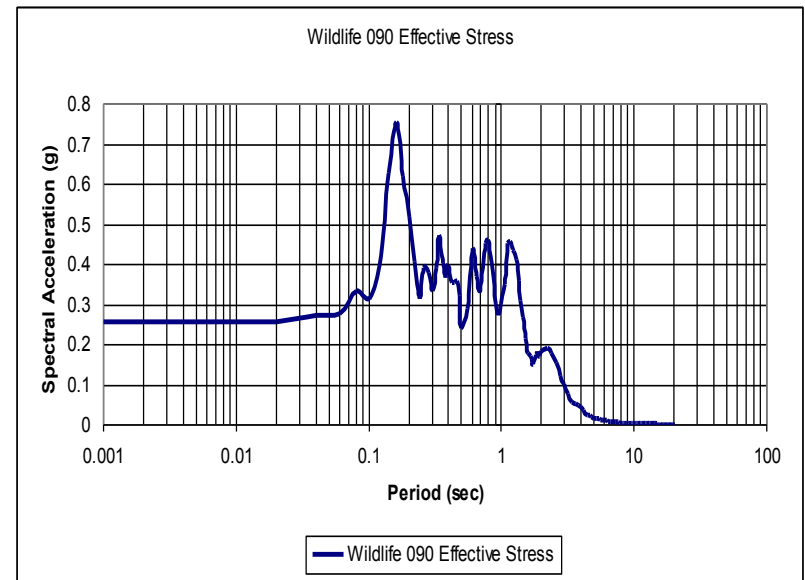


# Effects of Liquefaction on Site Response

## Total Stress Case



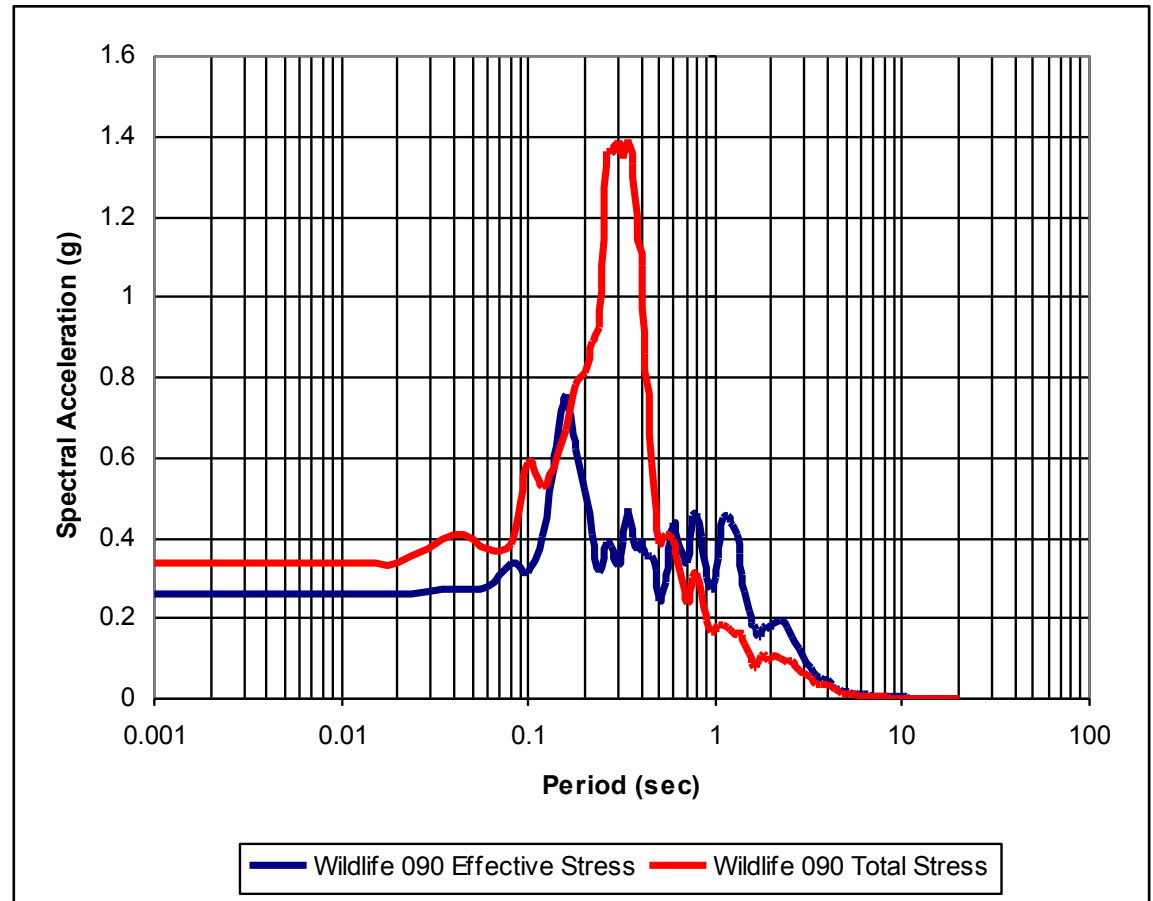
## Effective Stress Case



# Effects of Liquefaction on Site Response

Spectral ratio  
defined as

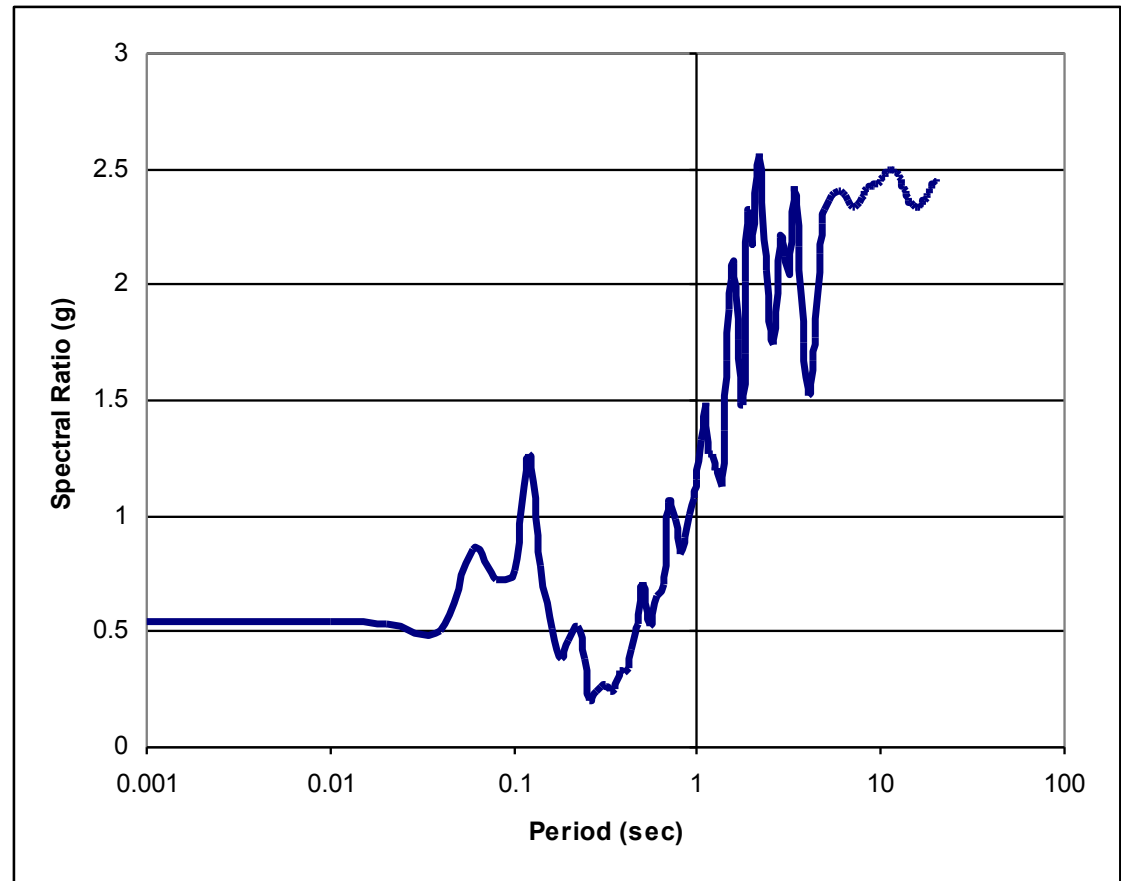
$$R(T) = \frac{S_a^{eff}}{S_a^{tot}}$$



# Effects of Liquefaction on Site Response

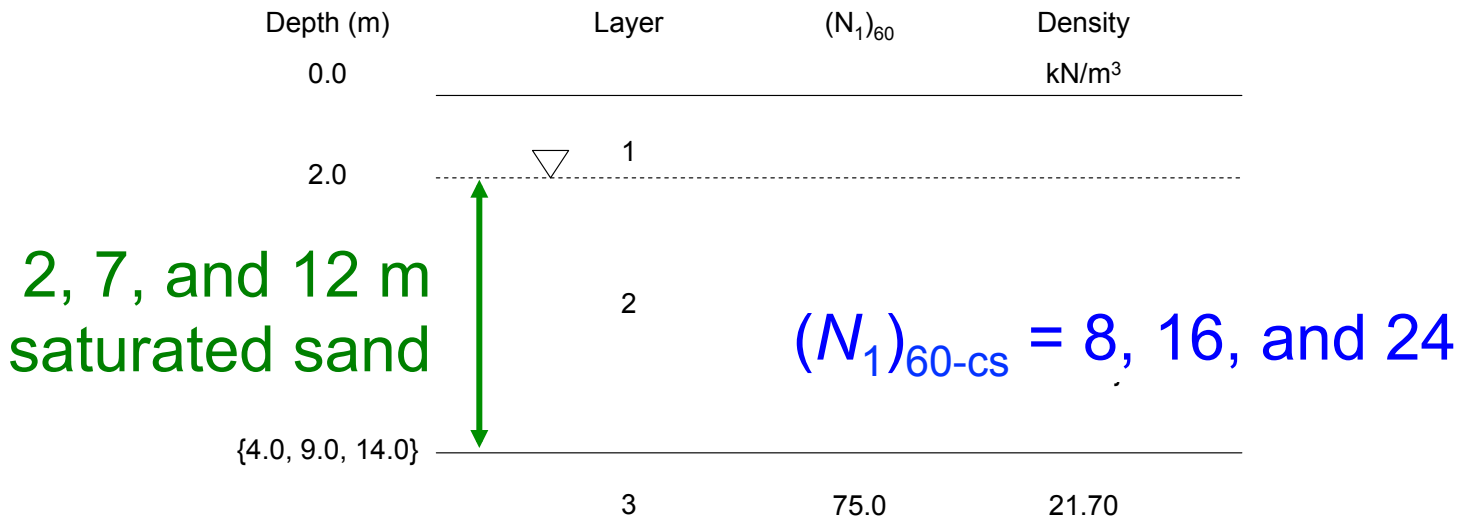
Spectral ratio  
defined as

$$R(T) = \frac{S_a^{eff}}{S_a^{tot}}$$



# Effects of Liquefaction on Site Response

- Binned database of 140 motions
  - Magnitudes range from 4.9 to 7.6
  - Distances range from 10 to 100 km
- Suite of nine idealized soil profiles

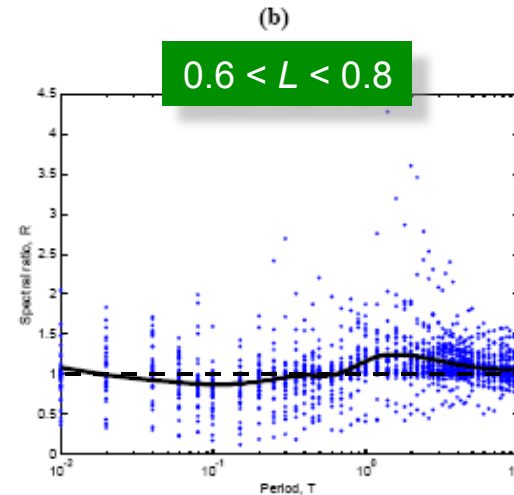
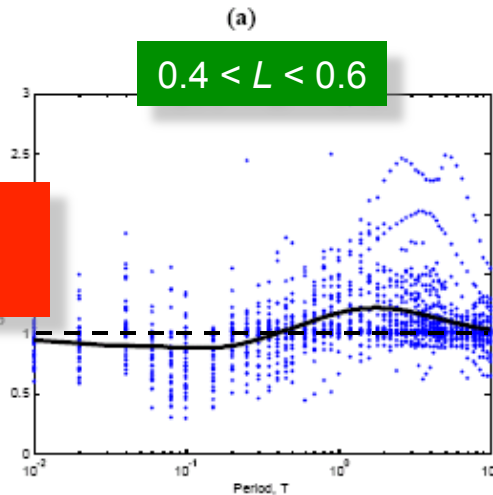


Pore pressure potential characterized in terms of loading factor,  $L = 1/FS_{\min}$

Plasticity Index = 0

# Effects of Liquefaction on Site Response

## Overview of Results

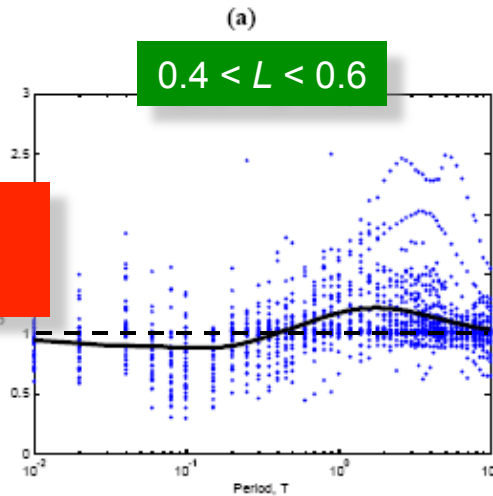


*Significant scatter*

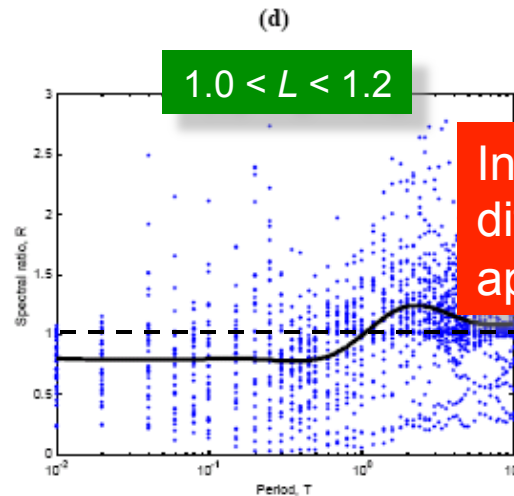
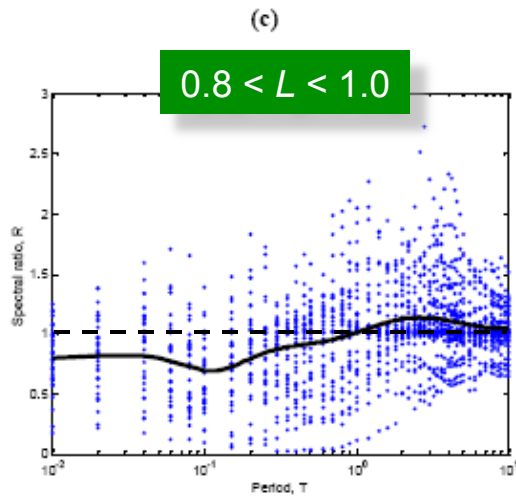
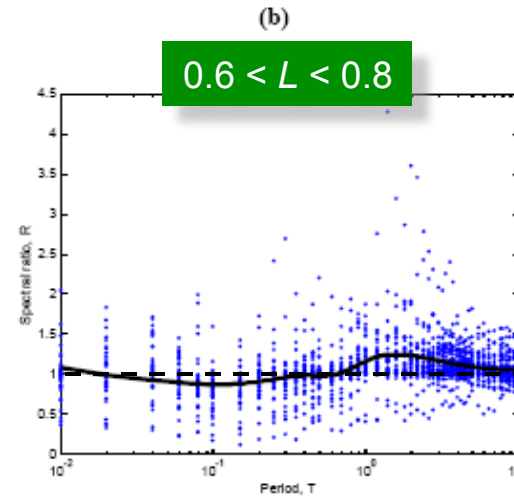
*Low correlation between periods*

# Effects of Liquefaction on Site Response

## Overview of Results



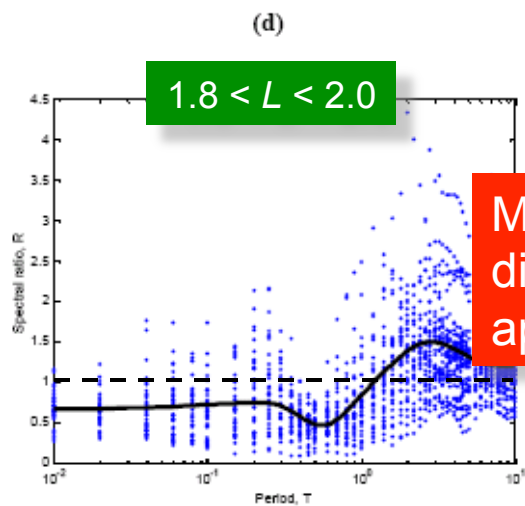
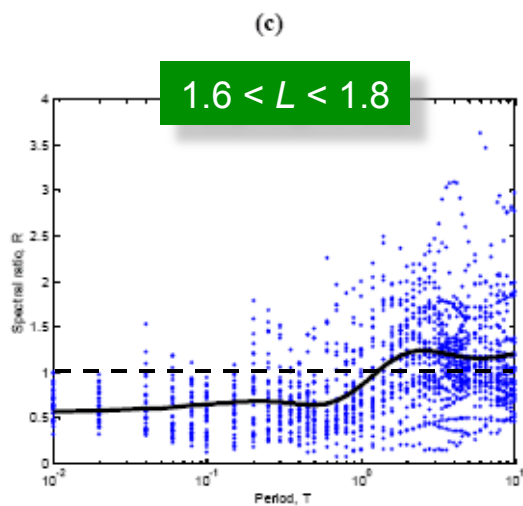
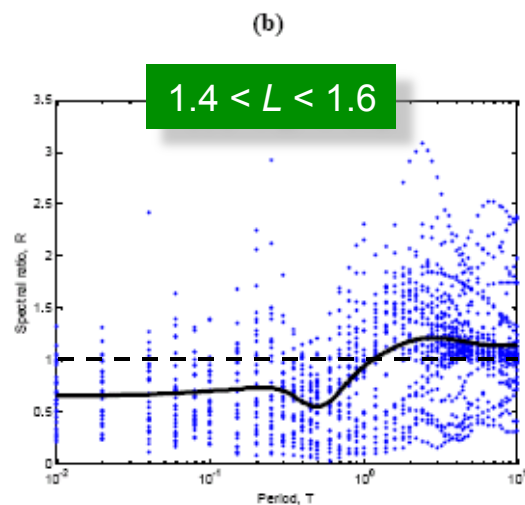
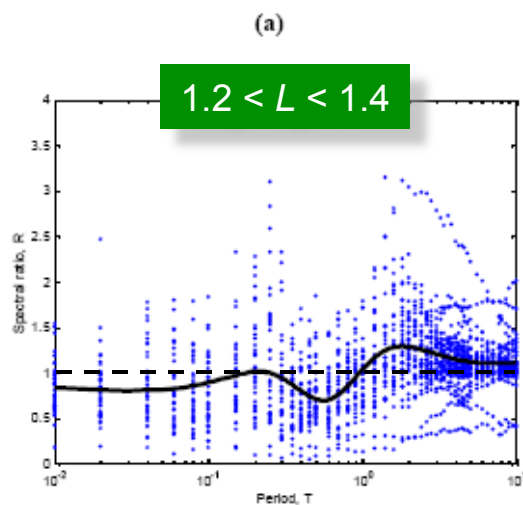
Small Changes  
for low  $L$



Increased  
differences as  $L$   
approaches 1.0

# Effects of Liquefaction on Site Response

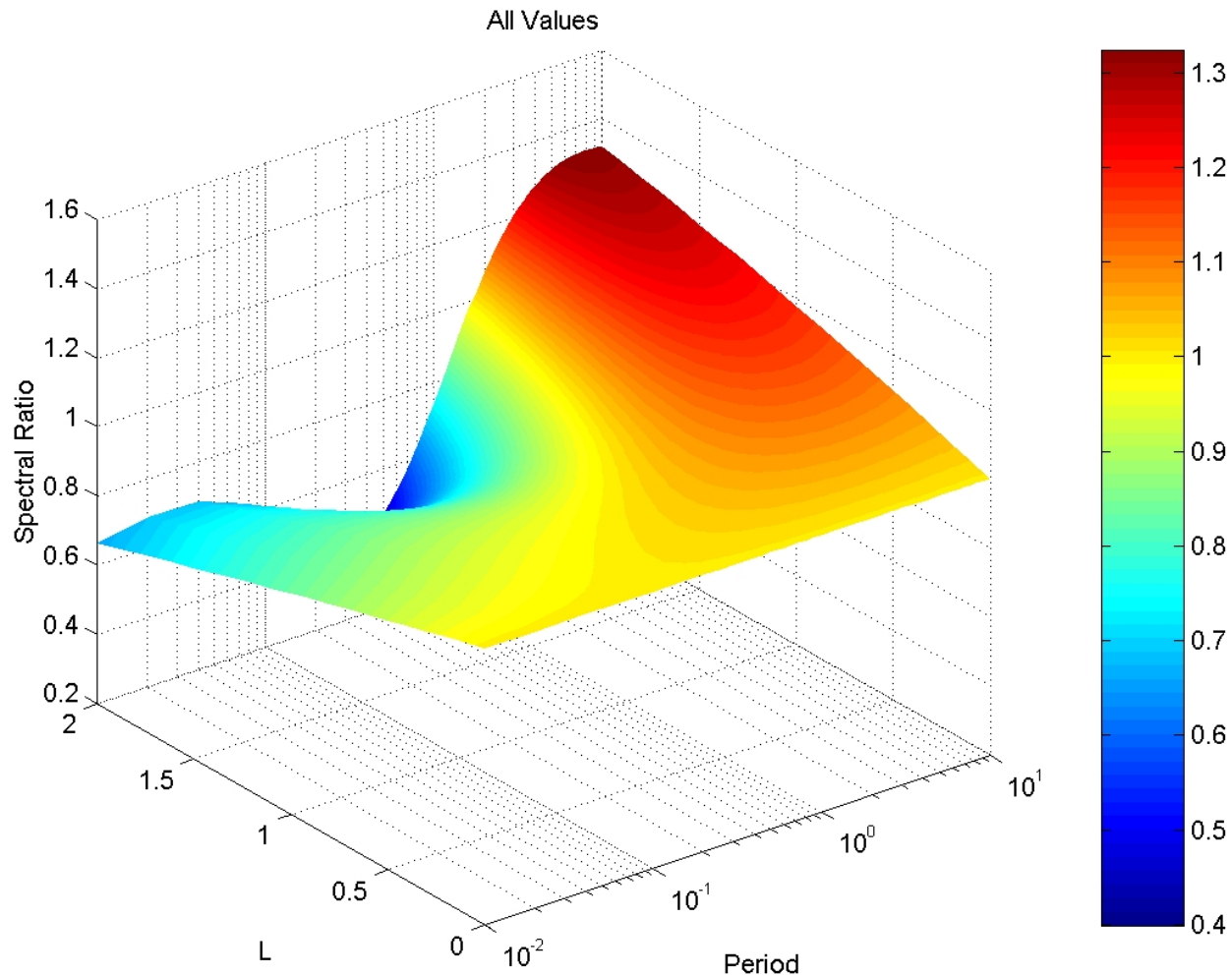
## Overview of Results



More defined differences as  $L$  approaches 2.0

# Effects of Liquefaction on Site Response

Predictive model





# Effects of Liquefaction on Site Response

## Model Validation

Accomplished by computation of “actual” spectral response

For  $L < 1.0$ : Need ground motion where no pore pressure generation occurred (Elmore Ranch)

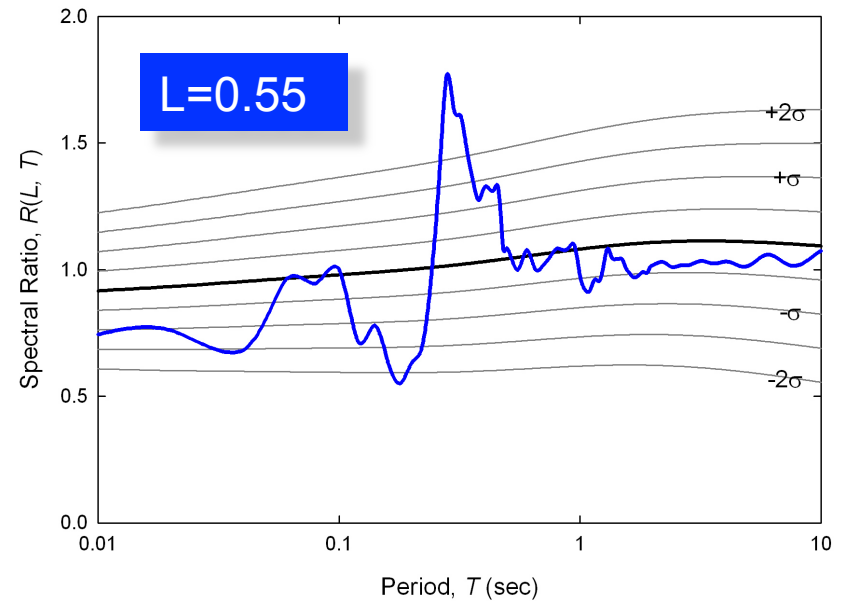
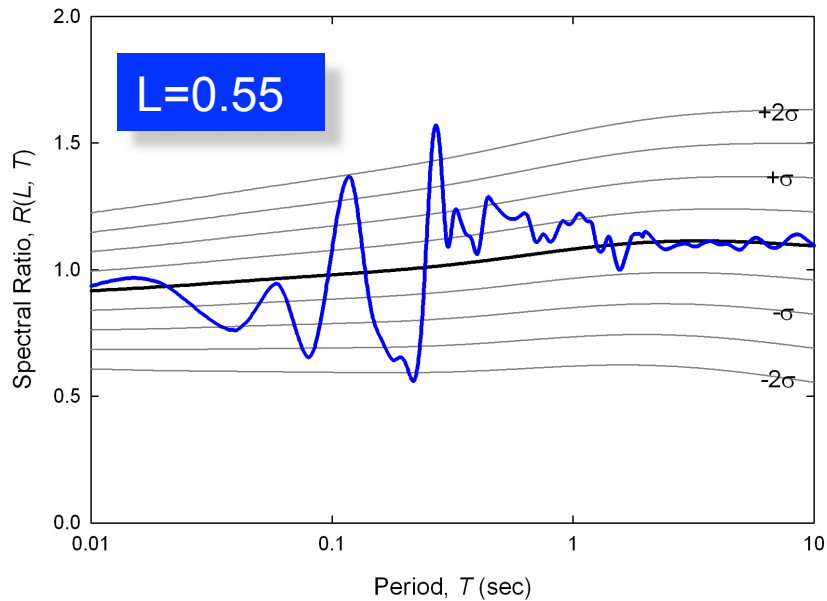
For  $L > 1.0$ : Need ground motion where pore pressure generation has occurred (Superstition Hills)

# Effects of Liquefaction on Site Response

Elmore Ranch Earthquake

“Actual” Computed as

Recorded / Total Stress Analysis

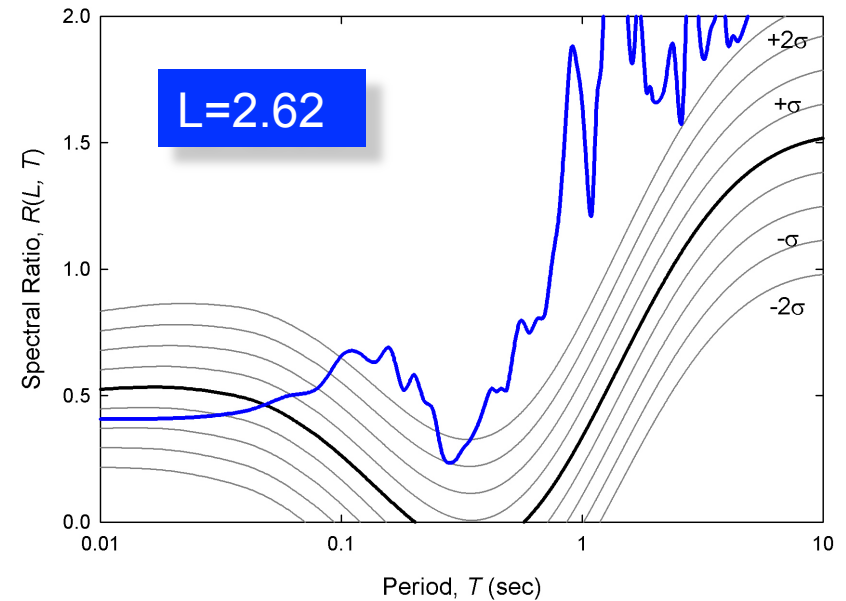
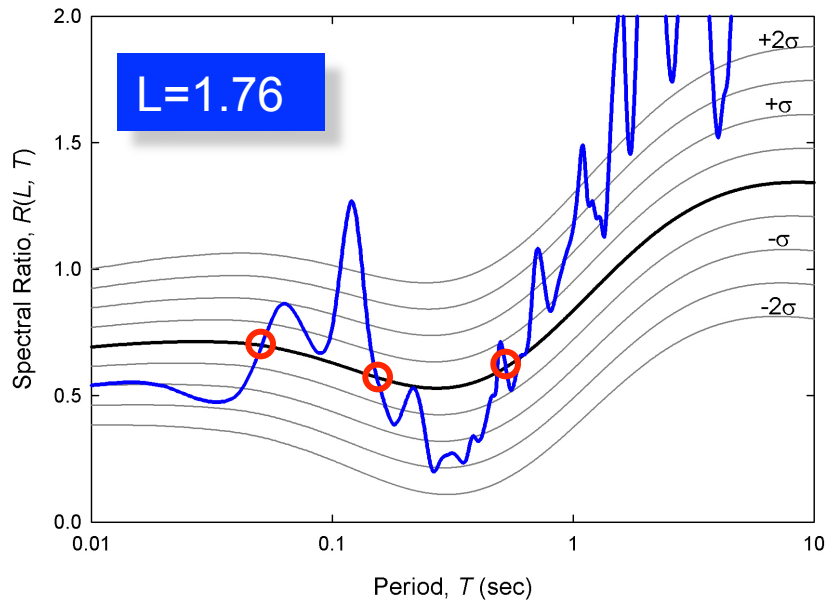


# Effects of Liquefaction on Site Response

Superstition Hills Earthquake

“Actual” Computed as

Recorded / Total Stress Analysis



# Summary

Liquefaction is a complex phenomenon, and understanding its mechanics is important in modeling response at sites underlain by liquefiable soils

Significant advances have been made in modeling the behavior of liquefiable soils up to and beyond the point of initial liquefaction

Many factors that affect recorded ground motions are not accounted for in commonly used site response prediction models

# Summary

Despite challenges, recent models allow representation of many important characteristics of liquefiable soil profile behavior

- Reduction in amplitude of high frequency components

- Increase in amplitude of low frequency components

- Evolving change in frequency content

- Occurrence of dilation following triggering of liquefaction

Vertical arrays will play important role in further development and validation of site response models, particularly for profiles containing liquefiable soils

***Thank you***

